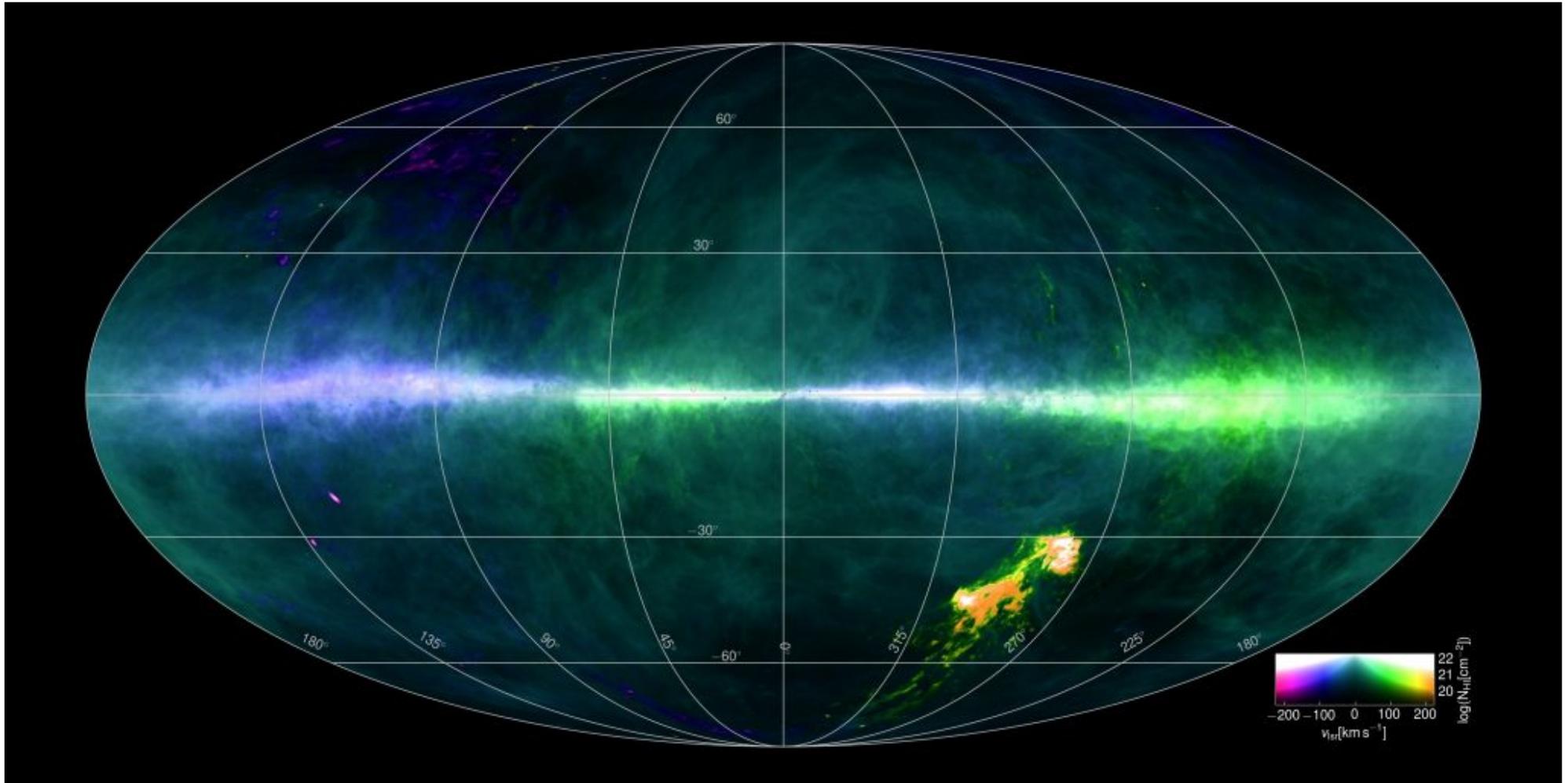


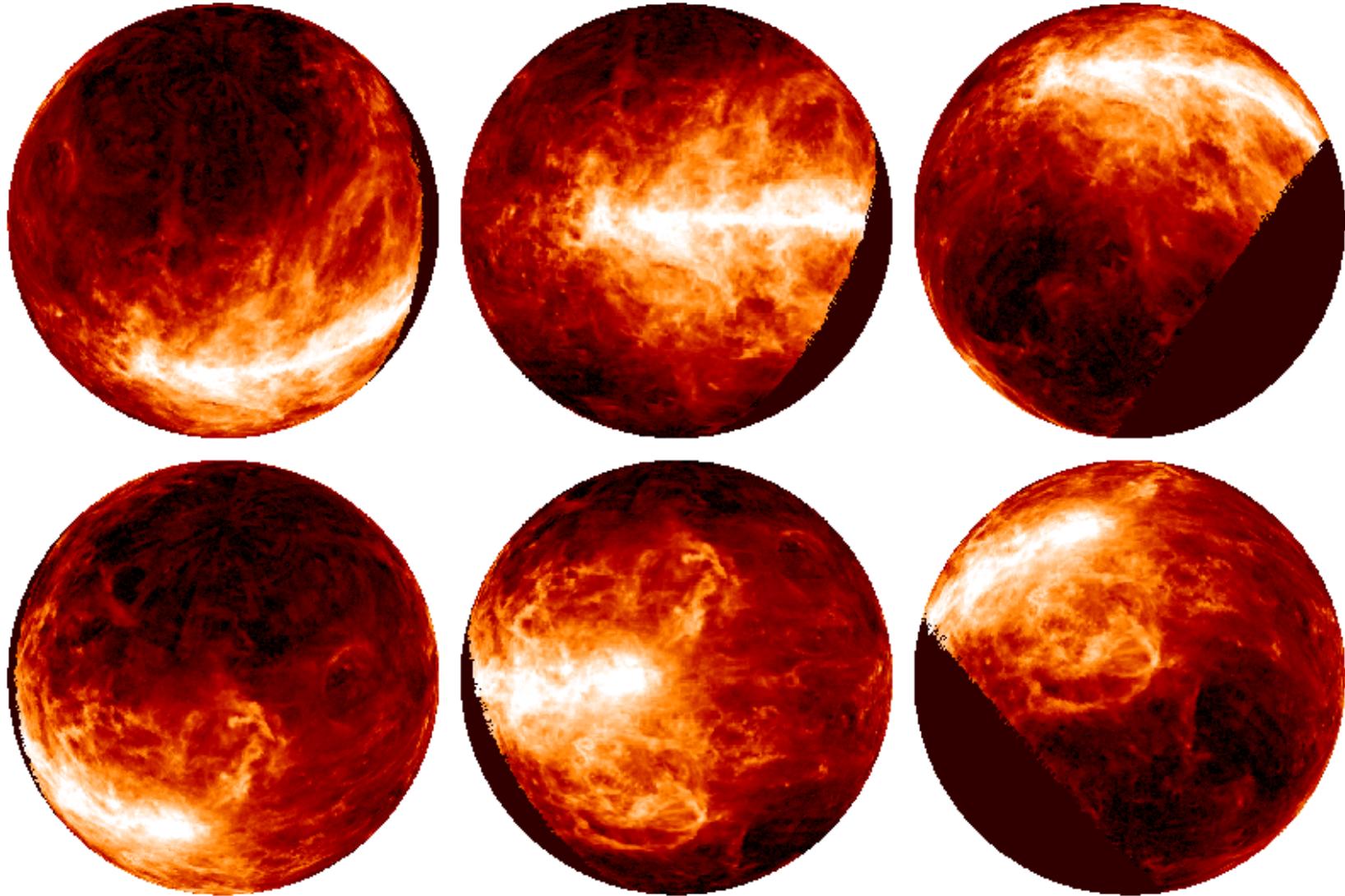
Galactic distribution HI



HI4PI collaboration: Effelsberg 100-m + Parkes 64-m

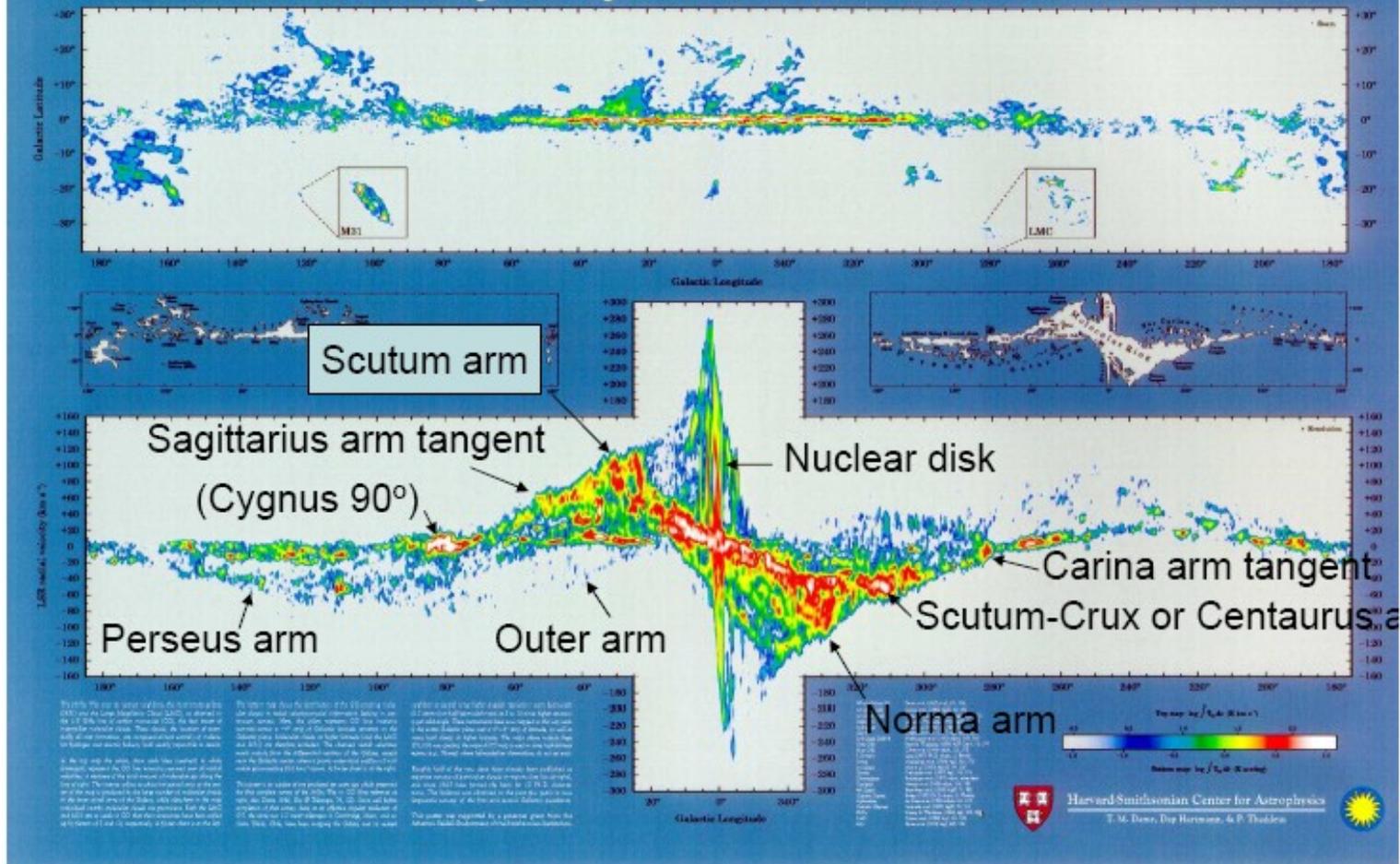
Resolution: 16.2 arcmin; rms: 43 mK. Full spatial sampling.

LAB: Galactic distribution HI



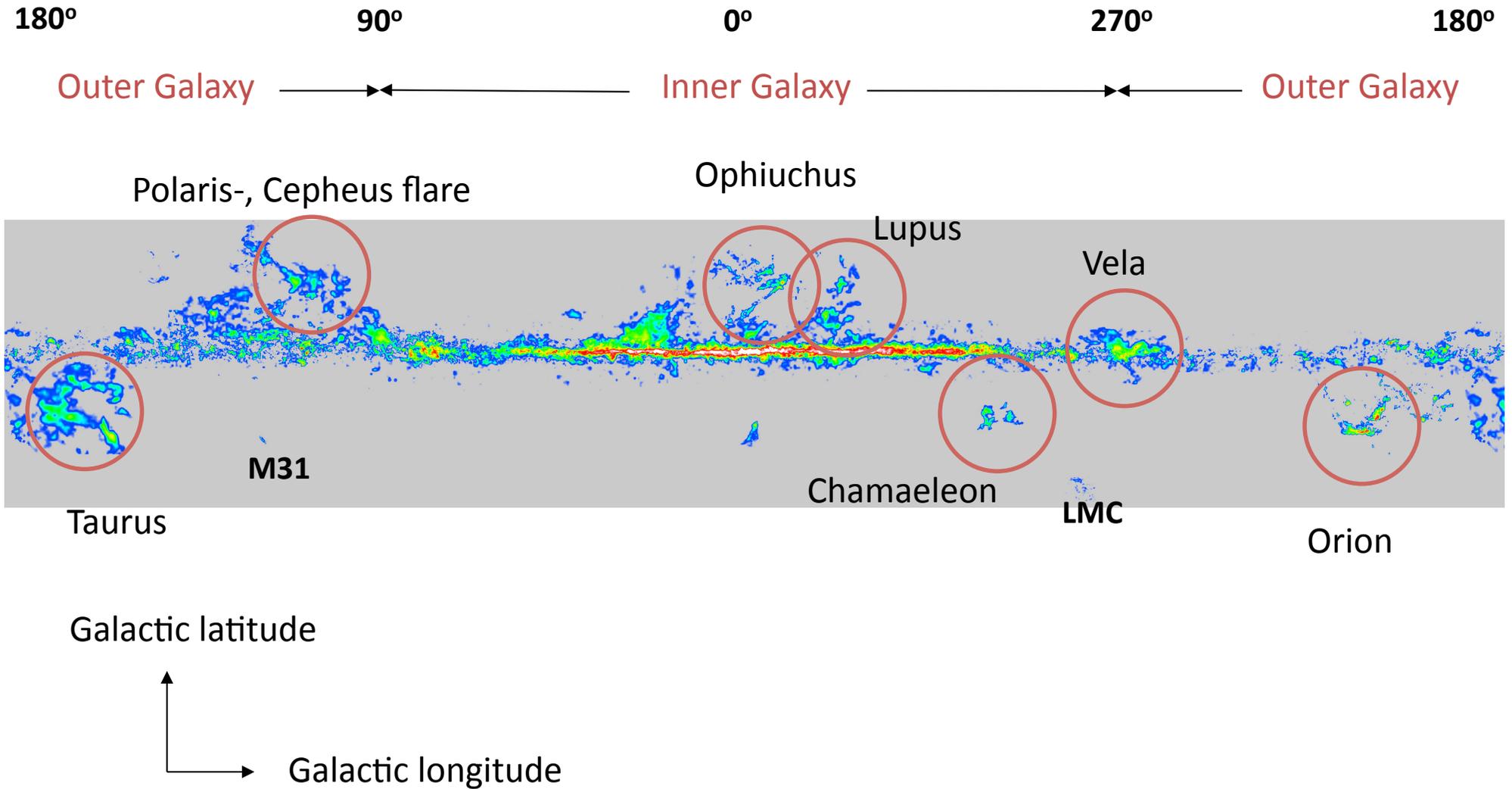
Hartmann & Burton 1994

The Milky Way in Molecular Clouds



Largest SF Regions: CFA CO survey of the Milky Way

Galactic distribution CO



CO, not H₂

ISM composed essentially of hydrogen:

H_I: 21-cm line

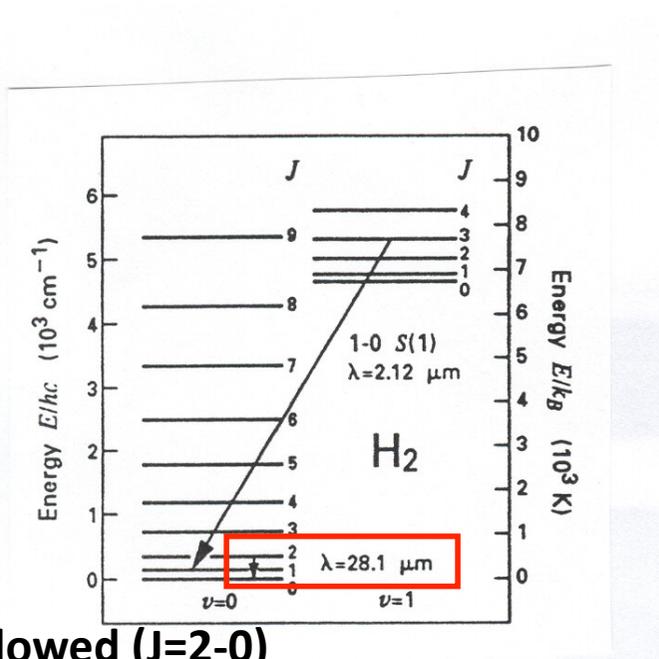
H₂: symmetric molecule ⇒ no radio emission

- UV absorption lines
- IR emission lines

CO: most abundant after H₂ : $[H_2]/[CO] \sim 1 \times 10^{-4}$.

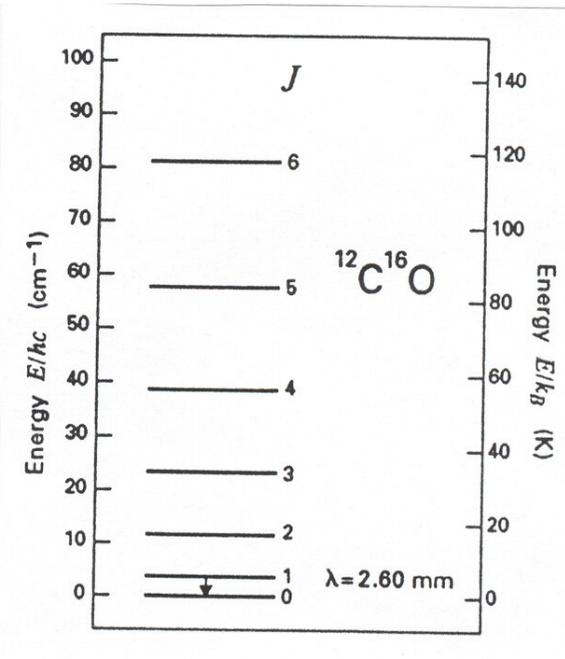
- excited by collisions with H₂
- easily observed rotational transitions at (sub-)mm wavelengths
- $n(H_2) \geq \text{a few} \times 10^3 \text{ cm}^{-3}$

Observing molecular clouds at large



Lowest allowed ($J=2-0$)

$\Delta E = 510 \text{ K}$



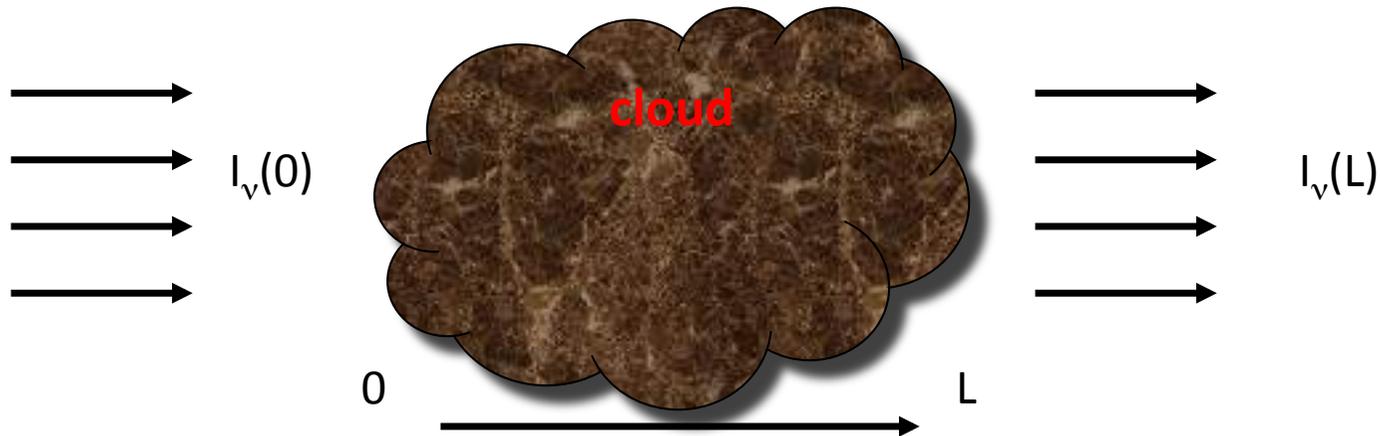
H_2 smallest diatomic molecule: widely-spaced energy levels

Even lowest excited rot. levels too far above ground state to be easily populated at normal molecular cloud T.

no dipole moment, hence quadrupole radiation (slow)

CO: more closely-spaced energy levels; easily populated also at low T

Radiation transport



$$I_\nu = I_\nu(0)e^{-\tau_\nu} + B_\nu(T_{\text{ex}})(1 - e^{-\tau_\nu}) \quad B_\nu(T) = \frac{2h\nu^3}{c^2} \frac{1}{(e^{h\nu/kT} - 1)} : \text{Planck function}$$

Define $T_A(\nu) \equiv \frac{I_\nu c^2}{2k\nu^2}$, $T_A(0) = T_{\text{bg}}$, and define $J_\nu(T) = \frac{h\nu}{k} \frac{1}{(e^{h\nu/kT} - 1)}$

Then: $T_A = J(T_{\text{ex}})(1 - e^{-\tau_\nu}) + J(T_{\text{bg}})e^{-\tau_\nu}$

Detection equation

In practice one measures $\Delta T_A = T_A - T_{\text{bg}}$ (ON-OFF) = $(T_{\text{ex}} - T_{\text{bg}})(1 - e^{-\tau_\nu})$

1) $\tau_\nu \ll 1$: $\Delta T_A \approx T \tau_\nu$ **measure column density**. All photons escape.

2) $\tau_\nu \gg 1$: $\Delta T_A \approx T$ **measure kinetic temperature**, but independent of col. dens.

Only photons at cloud surface ($\tau_\nu \leq 1$) escape.

T_{ex} , τ , and column density in LTE

For an optically thick line, e.g. CO(1-0): $\tau_\nu \gg 1$; the detection equation yields:

$$\begin{aligned} T_{ex} &= (h\nu/k) \ln^{-1}(h\nu/k [T_A + J(T_{bg})]^{-1} + 1) \\ &= 5.532 \ln^{-1}(5.532[T_A + 0.818]^{-1} + 1) \end{aligned}$$

For an optically thin line, e.g. $^{13}\text{CO}(1-0)$: $\tau_\nu \ll 1$; it follows that:

$$\tau_\nu = -\ln[1 - T_A / (J(T_{ex}) - J(T_{bg}))]^{-1}$$

Column density – derived from transition between levels J and J-1.

Detection equation: $T_A = J(T_{ex}) (1 - e^{-\tau_\nu}) + J(T_{bg}) e^{-\tau_\nu}$ and $\tau_\nu \ll 1$, solve for τ_ν .

From definition of T_{ex} , the definitions of the Einstein-coefficients, the equation for the absorption coefficient, and the definition of τ

$$N_{tot} = \left(\frac{3h}{8\pi^3 \mu^2} \right) \left(\frac{Z}{J} \right) e^{\frac{h\nu}{kT_{ex}}} \left[1 - e^{-\frac{h\nu}{kT_{ex}}} \right]^{-1} [J(T_{ex}) - J(T_{bg})] \int T_A dv$$

with Z the partition function (linking N_1 to N_{tot}).

$$\text{or: } N_{tot} = f(T_{ex}) \int T_A dv$$

Total column density

$$N_{\text{tot}} = f(T_{\text{ex}}) \int T_A dv$$

For $^{13}\text{CO}(1-0)$ and $\text{C}^{18}\text{O}(1-0)$ and $T_{\text{ex}} \approx 5 - 20 \text{ K}$:

$$f(T_{\text{ex}}) \approx (1.1 \pm 0.2) \times 10^{15} \text{ cm}^{-2} / (\text{Kkm/s})$$

Hence:

$$N_{\text{tot}} = (1.1 \pm 0.2) \times 10^{15} \int T_A dv \text{ cm}^{-2} \Rightarrow \text{Mass!}$$

If $\tau_v \leq 2$ then correction factor $\tau_0 / [1 - \exp(-\tau_0)]$, with τ_0 the opt. depth at line center
 $\tau_0 = -\ln(1-1/R)$ and $R = T_A(^{12}\text{CO}) / T_A(^{13}\text{CO})$.

Therefore:

$$N_{\text{tot}} = (1.1 \pm 0.2) \times 10^{15} \times \tau_0 / [1 - \exp(-\tau_0)] \times \int T_A dv \text{ cm}^{-2}$$

Mass follows via abundances: $N(^{12}\text{CO})/N(^{13}\text{CO}) \sim 90$ and $N(^{12}\text{CO})/N(\text{H}_2) \sim 1 \times 10^{-4}$

Deriving $N(\text{H}_2)$, total mass

1. Lines (Planck & Boltzmann)

Detection eqn., LTE, $\tau(^{12}\text{CO}) \gg 1$ ($\Rightarrow T_{\text{ex}}$), $\tau(^{13}\text{CO}) \ll 1$

$$N(^{13}\text{CO}) = f(\tau_{13}, T_{\text{ex}}, \Delta v_{13}) + [\text{H}_2]/[^{13}\text{CO}] = \dots \Rightarrow N(\text{H}_2)_{\text{LTE}}$$

$^{12}\text{C}/\text{H}$, $^{12}\text{C}/^{13}\text{C}$ gradients $\Rightarrow [\text{H}_2]/[^{13}\text{CO}] = f(R)$

Non-LTE transitions: LVG model (full radiation transport eqns.)

2. Virial theorem

Cloud radius (r), linewidth (Δv), assumptions about density distribution. For spherical cloud, $n \propto r^{-2} \Rightarrow M_{\text{vir}} = 126 r \Delta v^2$

Exclude non-bound motions (e.g. outflows); actual density distribution?

3. Dust continuum

$$M = (g S_{\nu} d^2) / \kappa_{\nu} B(T_{\text{dust}})$$

κ_{ν} , T-structure, gas-to-dust ratio (g) uncertain

4. Extinction mapping $N(\text{HI}) + 2N(\text{H}_2) \approx 1.9 \times 10^{21} \text{ cm}^{-2} A_{\nu}$, I_{CO} or $N(^{13}\text{CO})$

5. Lines (empirical)

$$N(\text{H}_2) / \int T(^{12}\text{CO}) dv \equiv X \Rightarrow N(\text{H}_2)_{\text{WCO}}$$

$X = \text{constant}$ or $f(R)$?

$$N(\text{H}_2) = X_{\text{CO}} W_{\text{CO}} \text{ with } W_{\text{CO}} = \int T(^{12}\text{CO}) dv$$

In Milky Way $X_{\text{CO}} = 2 \times 10^{20} (\text{K kms}^{-1})^{-1} \text{ cm}^{-2}$ with 30% uncertainty (Bolatto+ 2013 ARAA)

$$\begin{aligned} M &= \pi R^2 \times N(\text{H}_2) \times m(\text{H}_2) \times \text{He-corr} = \pi R^2 X_{\text{CO}} W_{\text{CO}} \times m(\text{H}_2) \times \text{He-corr} = \\ &= [X_{\text{CO}} \times m(\text{H}_2) \times \text{He-corr}] \times L_{\text{CO}} \end{aligned}$$

$$\begin{aligned} M_{\text{mol}} &= \alpha_{\text{CO}} L_{\text{CO}} \text{ with } L_{\text{CO}} = \pi R^2 W_{\text{CO}}, \text{ in } \text{K km s}^{-1} \text{ pc}^2 \\ &\dots \text{ Plugging in values, } \text{pc}^2 \rightarrow \text{cm}^2, \text{ g} \rightarrow M_{\odot} \dots \end{aligned}$$

$$\Rightarrow M(M_{\odot}) = 4.3 L_{\text{CO}} \text{ for the galactic value of } X_{\text{CO}}$$

The value of X_{CO} is determined by calibrating empirical N or M with other methods.

Original derivation of X_{CO} was by using diffuse γ -ray emission (Lebrun+ 1983)

Based on fact that diffuse γ -ray emission is mostly due to collisions between cosmic rays and the ISM: $I_{\gamma} = \epsilon_{\gamma} [N(\text{HI}) + 2X_{\text{CO}} W_{\text{CO}}]$ (Bloemen 1989)
compare maps of diffuse γ -emission, HI and CO to find X_{CO} .

Values for other types of galaxies

- Normal galaxies: $X_{CO} \approx 2 \times 10^{20}$ with factor 2 uncertainty

Increases sharply in systems with metallicity ca. 0.5 solar
Often smaller in central regions, as in MW

- * Starbursts and other luminous galaxies: $X_{CO} \approx 0.4 \times 10^{20}$ with factor 3 uncertainty

Antennae-values: see Zhu, Seaquist & Kuno 2003 ApJ 588, 243

$$M_{\text{tot}} \sim 2 \times 10^9 M_{\odot}$$

See also Herrera+ 2012 A&A 538, L9 for ALMA data (3-2 instead of 1-0!)

or Espada+ 2012 ApJL 760, L25 ALMA CO(2-1): derives Σ ($M_{\odot} \text{ pc}^{-2}$), uses units like $\text{Jy kms}^{-1} \text{ arcsec}^{-2}$!

- * At high redshifts:

In massive merger-driven starbursts such as SMGs, most consistent with low X_{CO}
(cf. local ULIRGs)

In blue-sequence galaxy disks, likely higher X_{CO} (cf. local disks)