

Interferometry @ mm

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Italian Node of ALMA Regional Center

Slides & contributions from
Arturo Mignano

<http://www.alma.inaf.it/index.php/Courses>

Ideas and slides borrowed from
IRAM interferometry school

<http://www.iram-institute.org/EN/content-page-248-7-67-248-0-0.html>

NRAO interferometry school

<https://science.nrao.edu/science/meetings/2016/15th-synthesis-imaging-workshop>

LOFAR school

<http://www.astron.nl/lofarschool2014/>

European Radio interferometry (ERIS) school

<https://www.eso.org/sci/meetings/2015/eris2015.html>

Synthesis Imaging in Radio Astronomy: II - The “White Book”

Virtual Radio Interferometer

<http://www.narrabri.atnf.csiro.au/astronomy/vri.html>

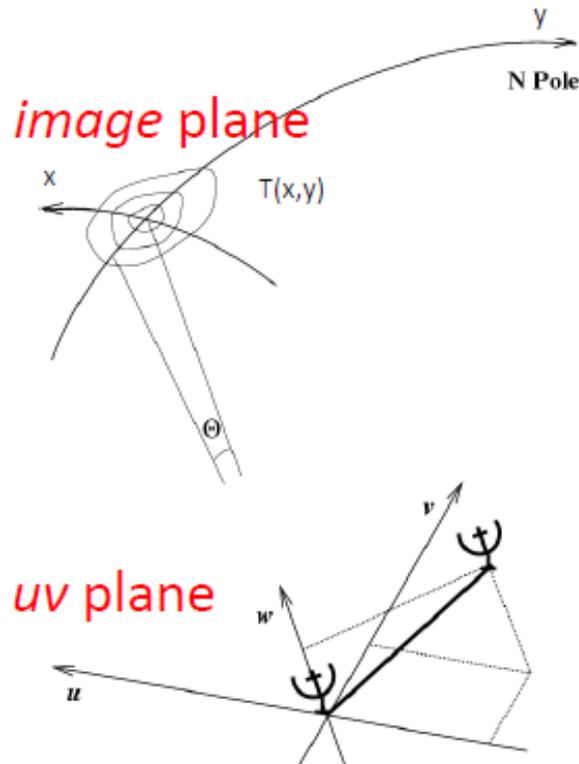
https://casaguides.nrao.edu/index.php?title=M100_Band3

Interferometry basics

Indeed the **CORRELATOR** performs a more complicated operation (i.e. the true cross-correlation) to deliver **VISIBILITIES**:

$$V^{ij}(\tau_g) = (V^i V^j) = \lim_{T \rightarrow \infty} \int_{-T/2}^{T/2} V^i(t) V^{j*}(t + \tau_g) dt$$

In the (2-D) uv -plane each visibility samples the FT of the (2-D) $B(\theta, \phi)$



(van Cittert-Zernike theorem)

Fourier space/domain

$$V(u, v) = \iint T(x, y) e^{2\pi i(ux + vy)} dx dy$$

$$T(x, y) = \iint V(u, v) e^{-2\pi i(ux + vy)} du dv$$

Image space/domain

Interferometry basics

In the next two weeks we are going to deal with

visibilities and **uv plane**

To get familiar with them you can play with

★ a java applet online:

<http://www.narrabri.atnf.csiro.au/astronomy/vri.html>

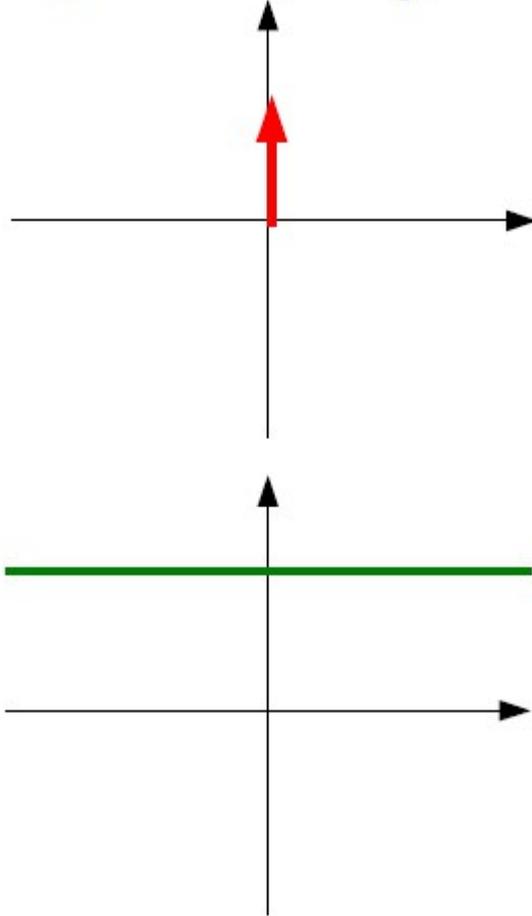
★ or a python script written by Ivan Marti-Vidal
(nordic ARC node) APSYNSIM

<https://launchpad.net/apsynsim>

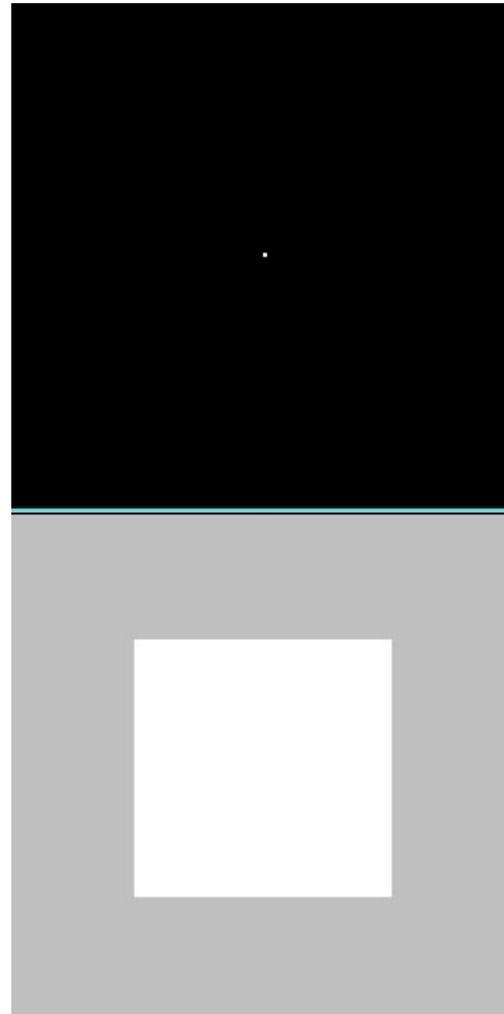
Interferometry basics

1 D

1. The pulse: $\delta(x - x_0)$



2 D

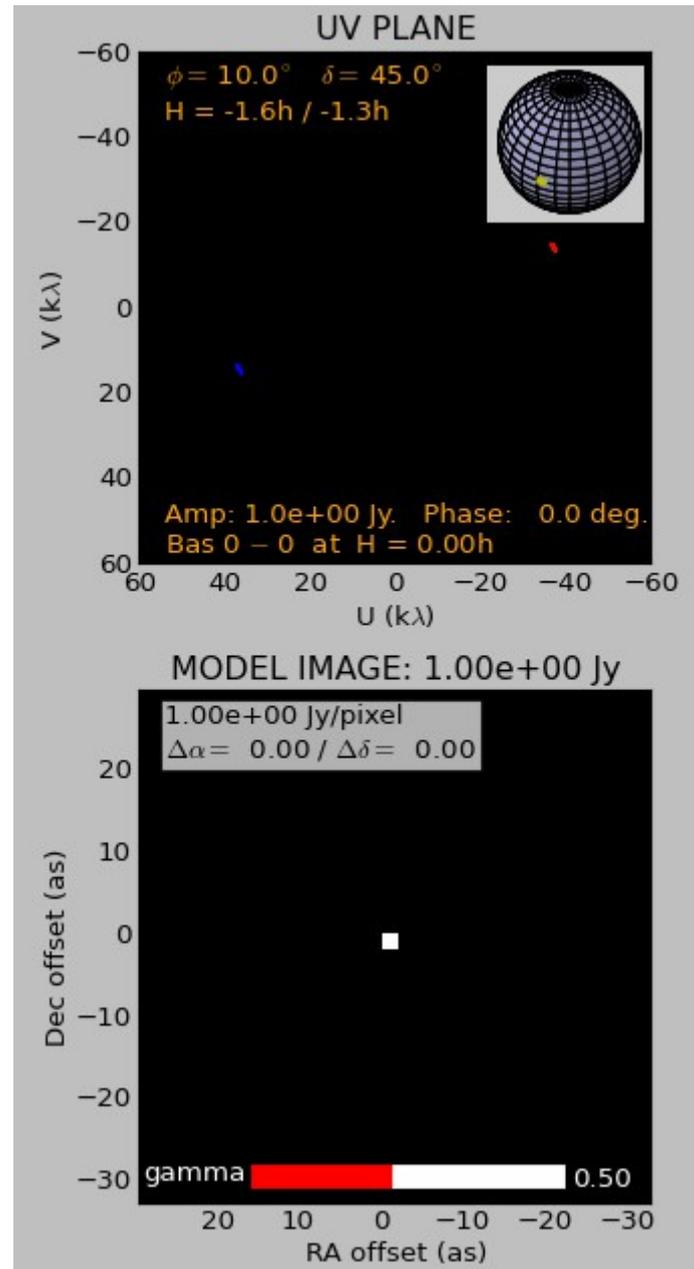
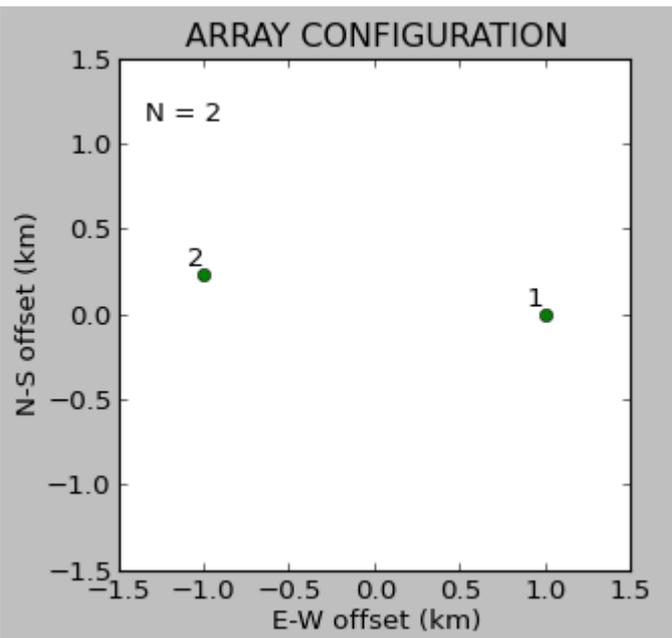


Point source
in the sky

Ideal uv plane

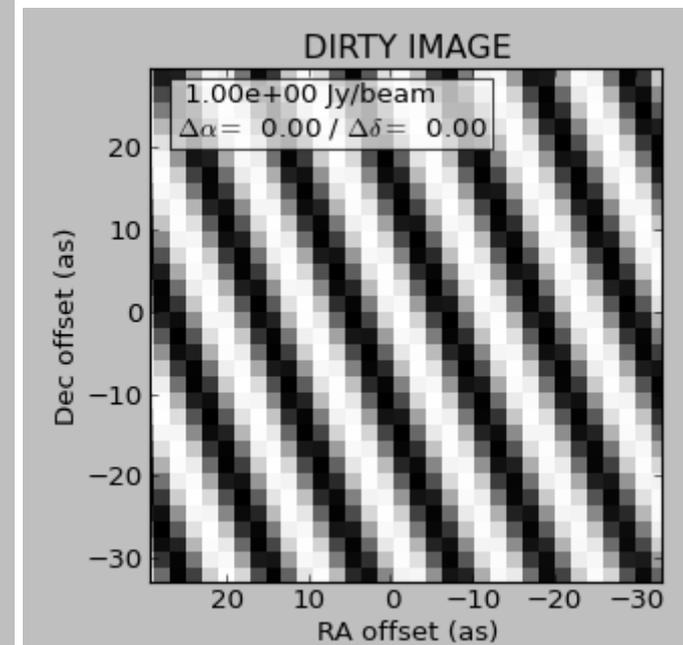
Interferometry basics

Snapshot observation
with two antennas
1 baseline



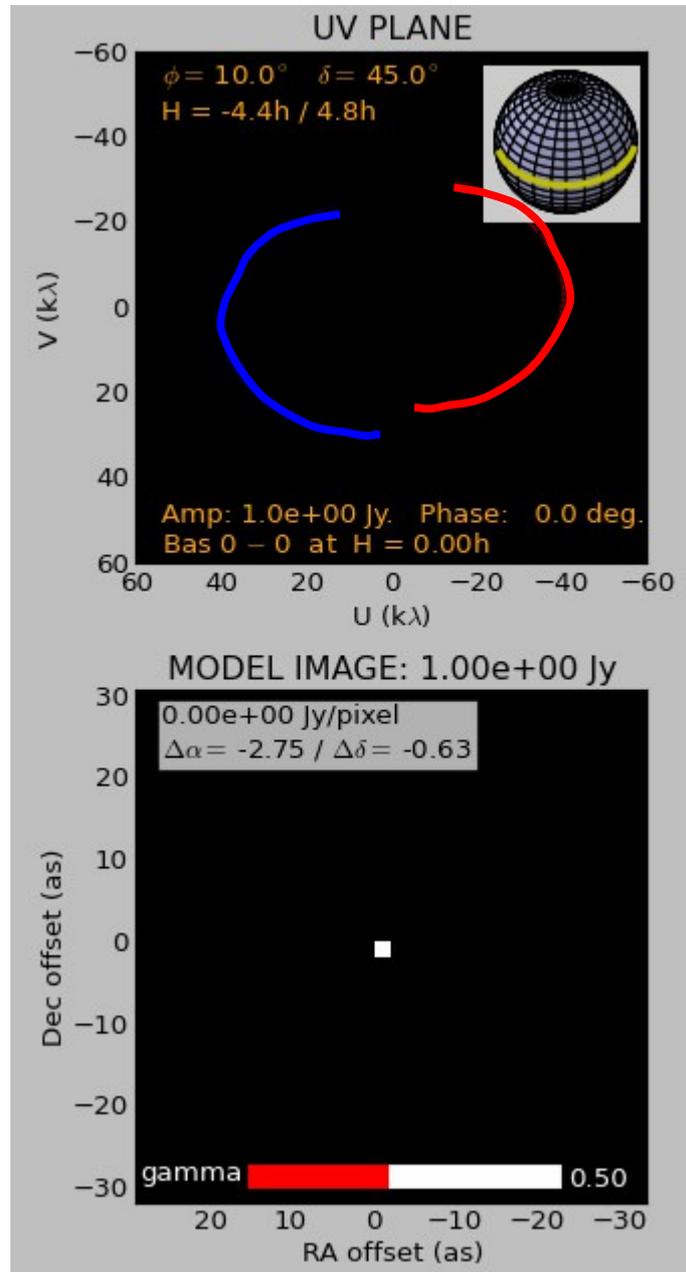
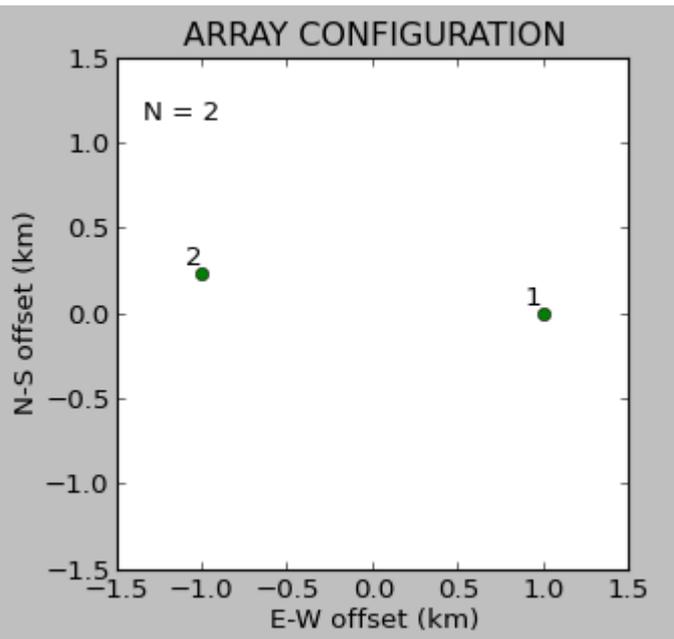
← uv-coverage

Resulting image



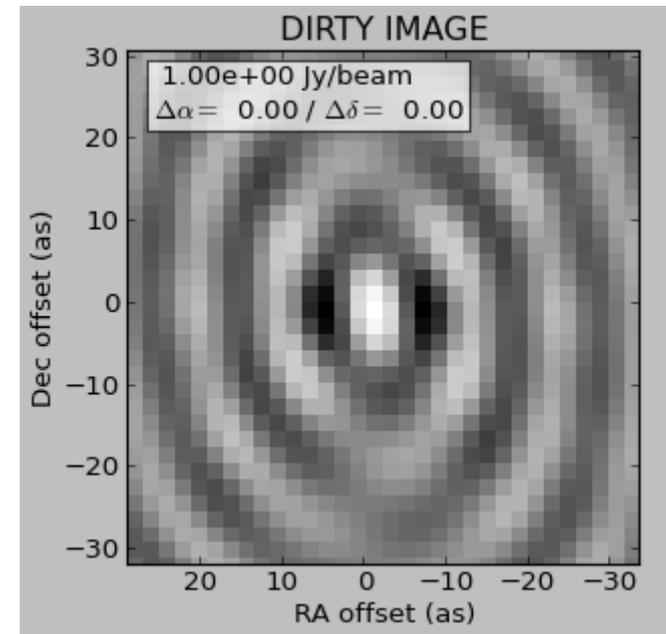
Interferometry basics

8 hrs observation
with two antennas
1 baseline (~2 km)



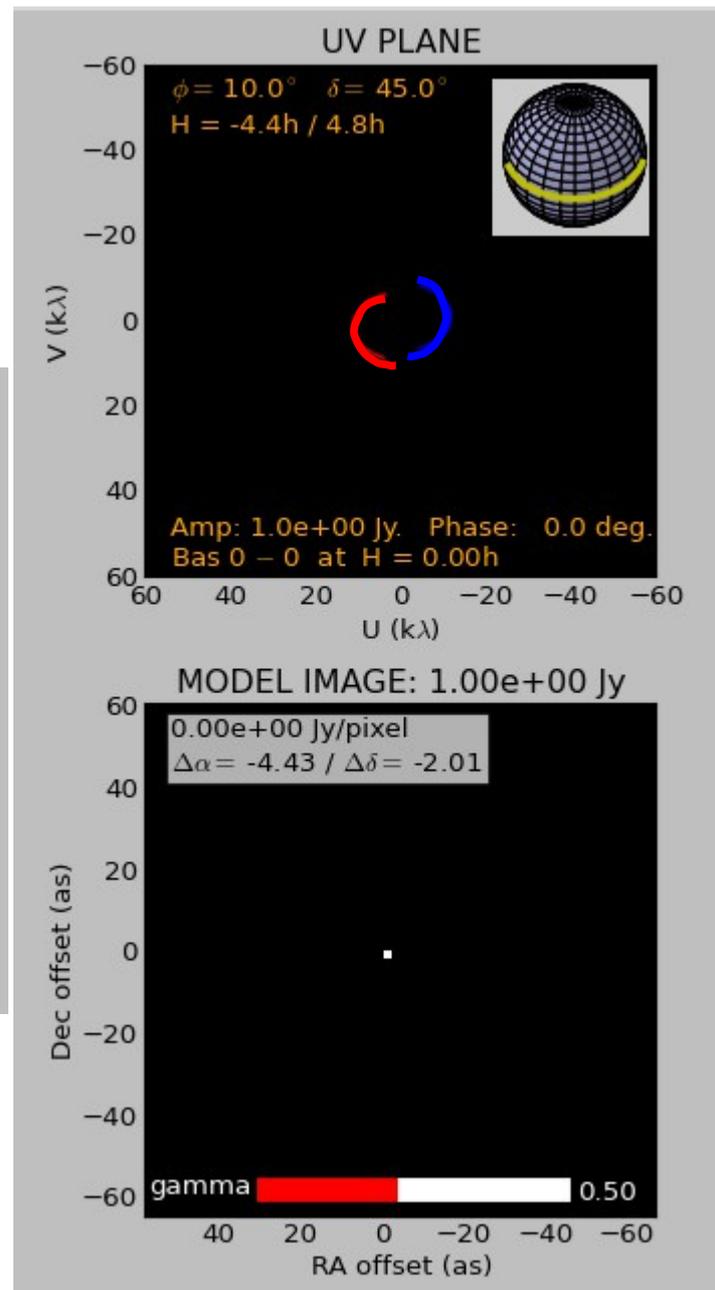
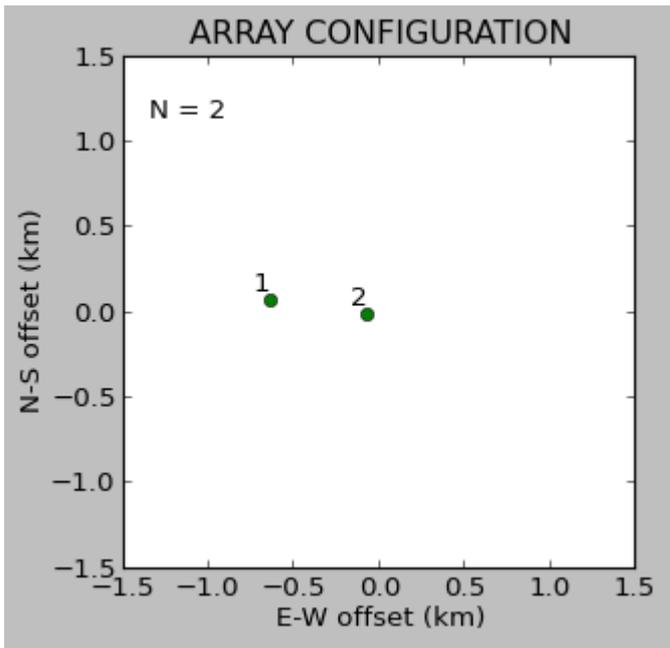
← uv-coverage

Resulting image



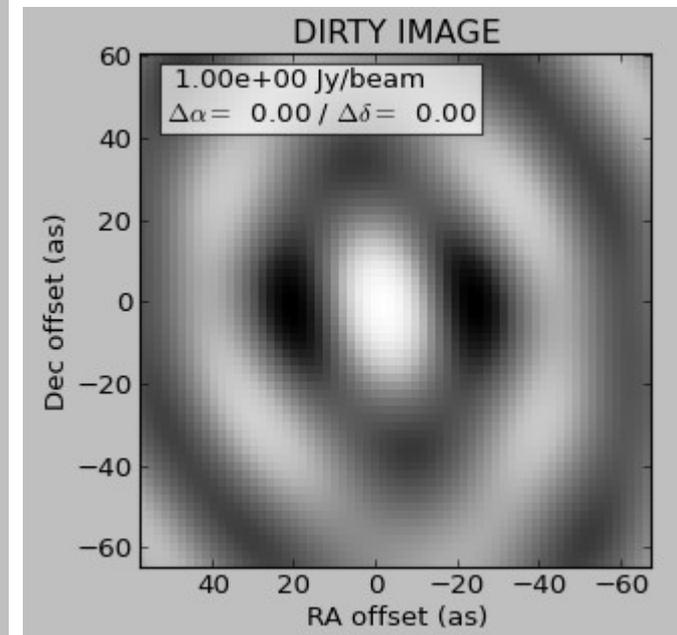
Interferometry basics

8 hrs observation
with two antennas
1 baseline (~800 m)



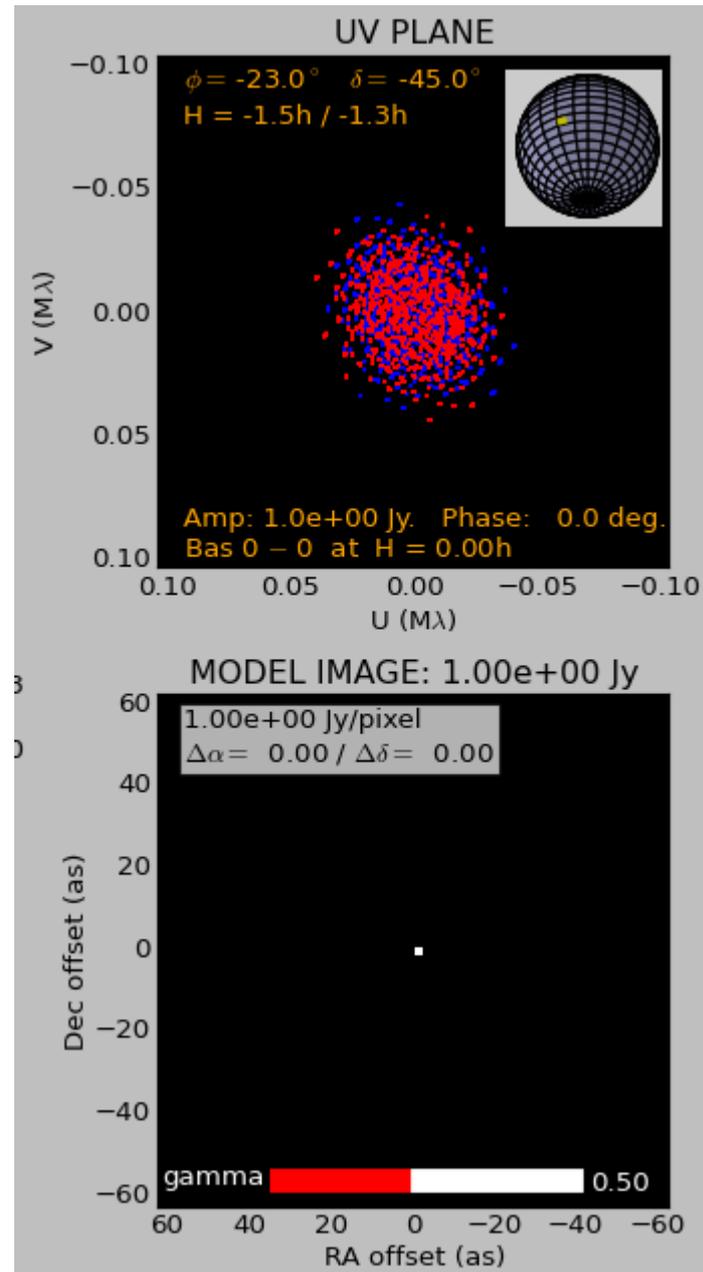
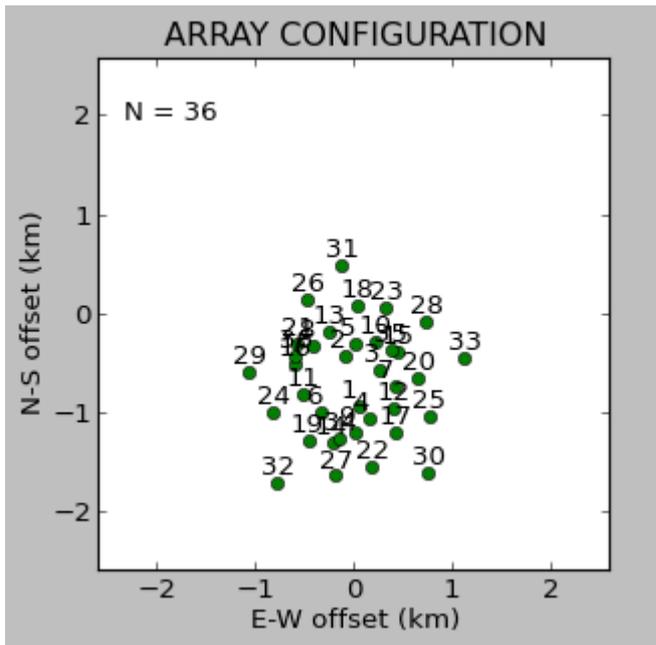
← uv-coverage

Resulting image



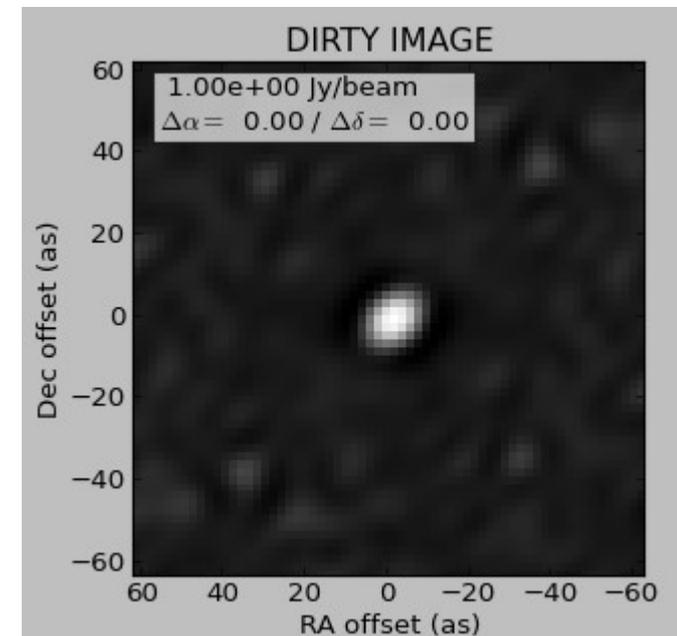
Interferometry basics

Snapshot observation
with 36 antennas
1260 baselines



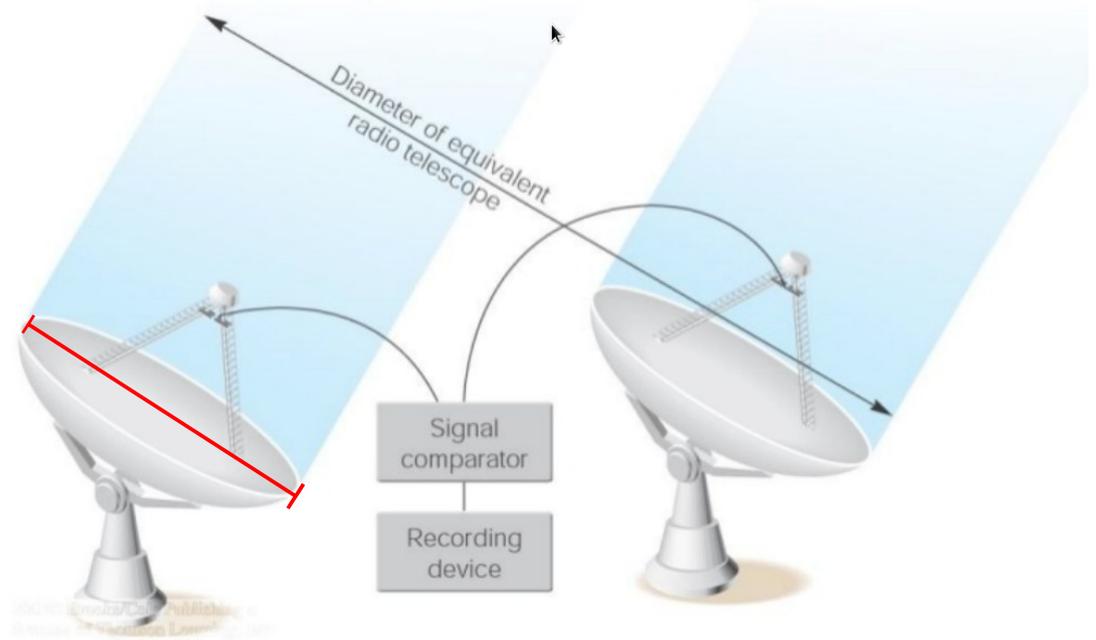
← uv-coverage

Resulting image



Interferometry basics

Field of View $FOV \propto \frac{\lambda}{D}$

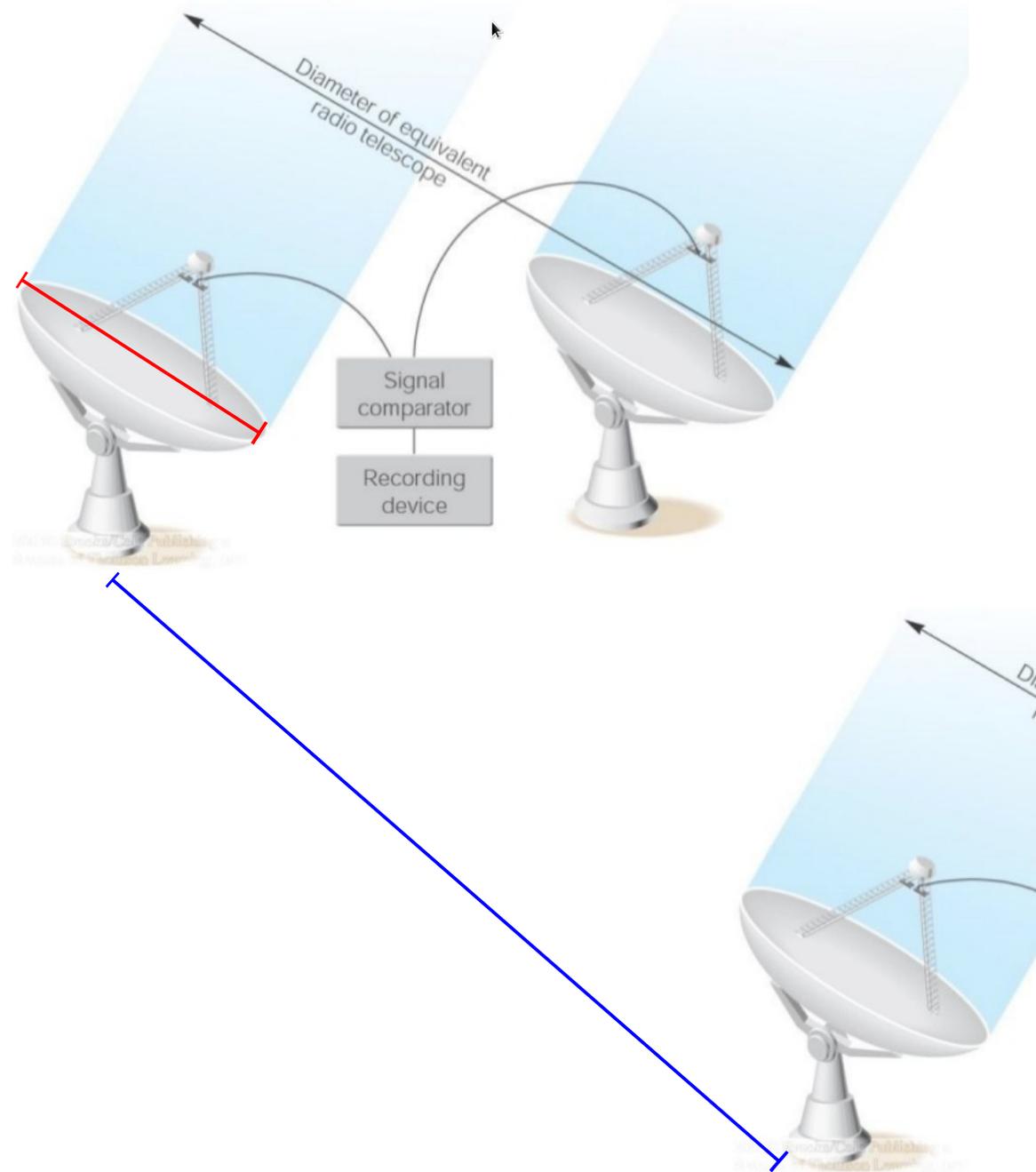


Interferometry basics

Field of View $FOV \propto \frac{\lambda}{D}$

Resolution

$$\theta_{res} \approx \frac{\lambda}{B_{max}}$$



Interferometry basics

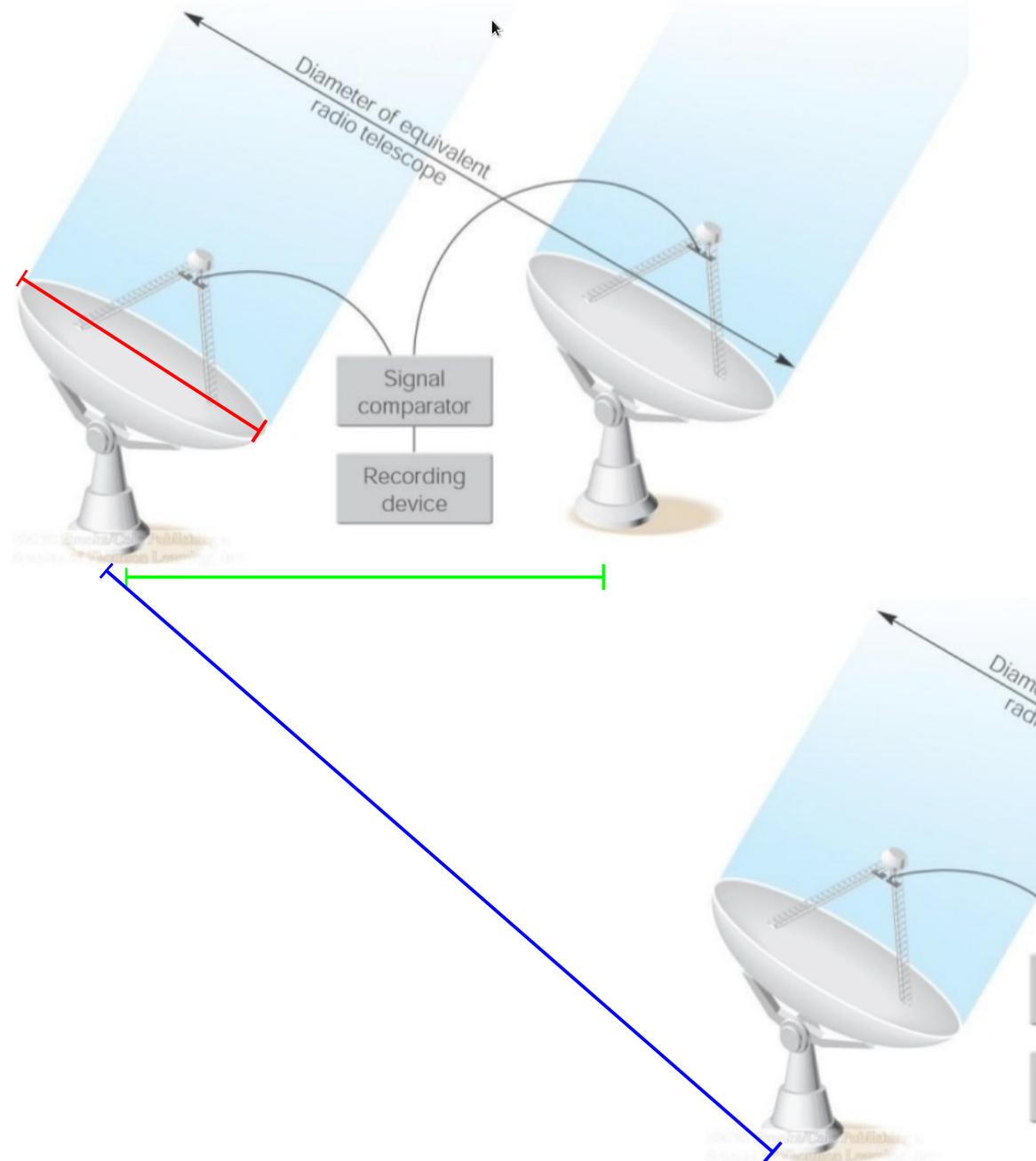
Field of View $FOV \propto \frac{\lambda}{D}$

Resolution

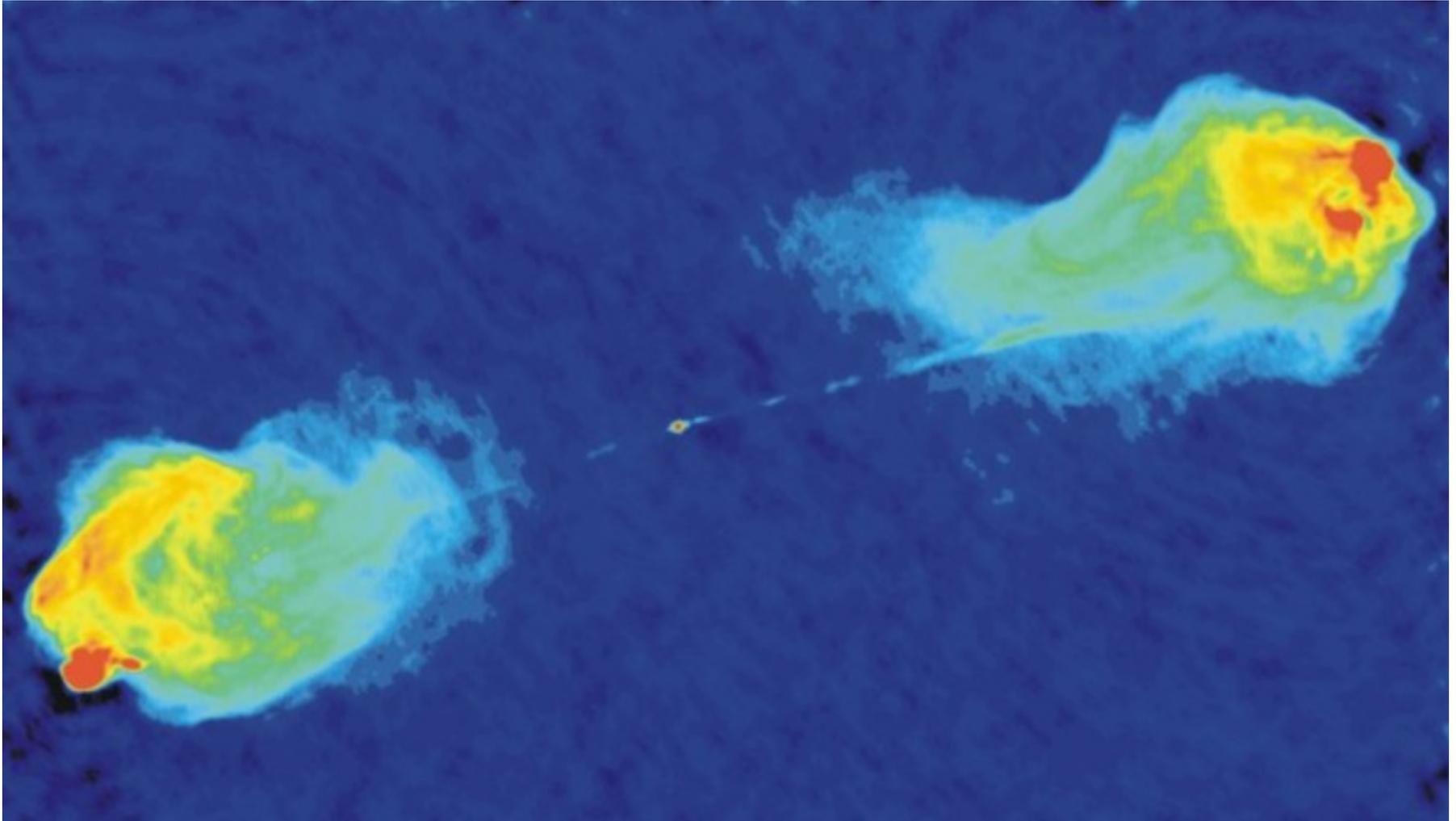
$$\theta_{res} \approx \frac{\lambda}{B_{max}}$$

Largest recoverable scale

$$\theta_{MRS} \approx \frac{\lambda}{B_{min}}$$



How to get this image of Cygnus A?



Credit: Image courtesy of NRAO/AUI; R. Perley, C. Carilli & J. Dreher

Peculiarities @ mm

With increasing frequency:

★ **No external human interferences in the data**



★ **No ionospheric effect**

★ **Tropospheric effects: absorption and delay of signal**

→ stronger weather dependency

→ T_{sys} dominated by atmosphere noise



★ **Time variability of quasar increases**

→ which flux calibrators?

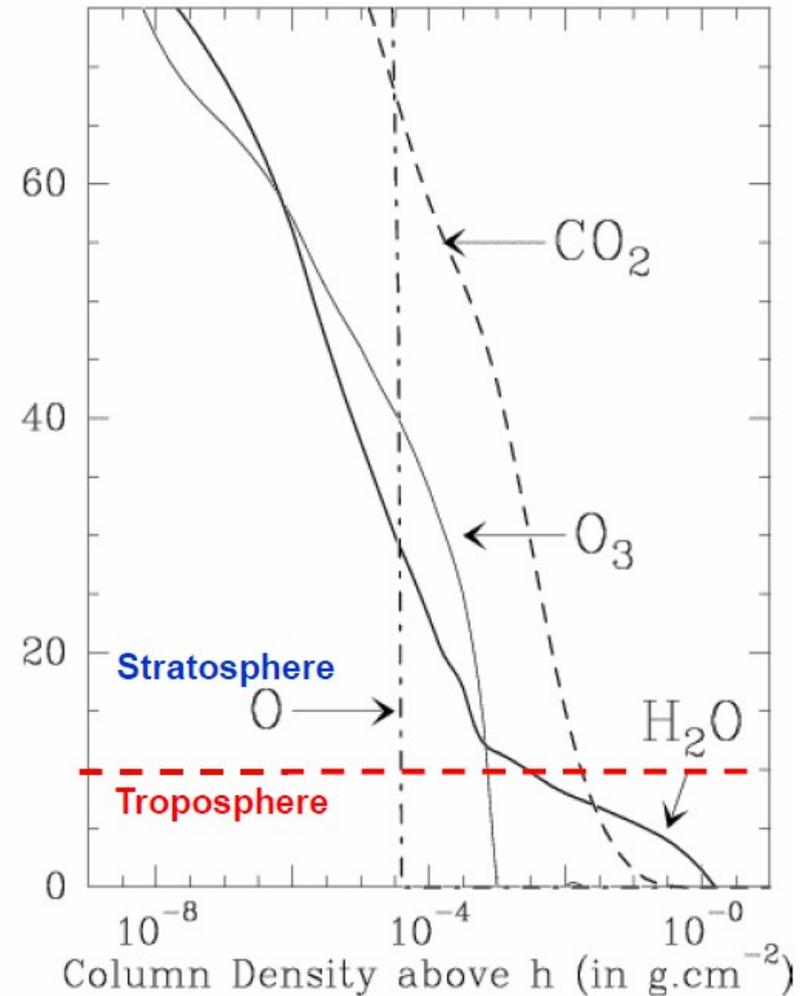
Peculiarities @ mm



The role of troposphere

- H_2O (mostly vapor)
- “Hydrosols” (water droplets in clouds and fog)
- “Dry” constituents: O_2 , O_3 , CO_2 , Ne, He, Ar, Kr, CH_4 , N_2 , H_2
- clouds & convection = time variation

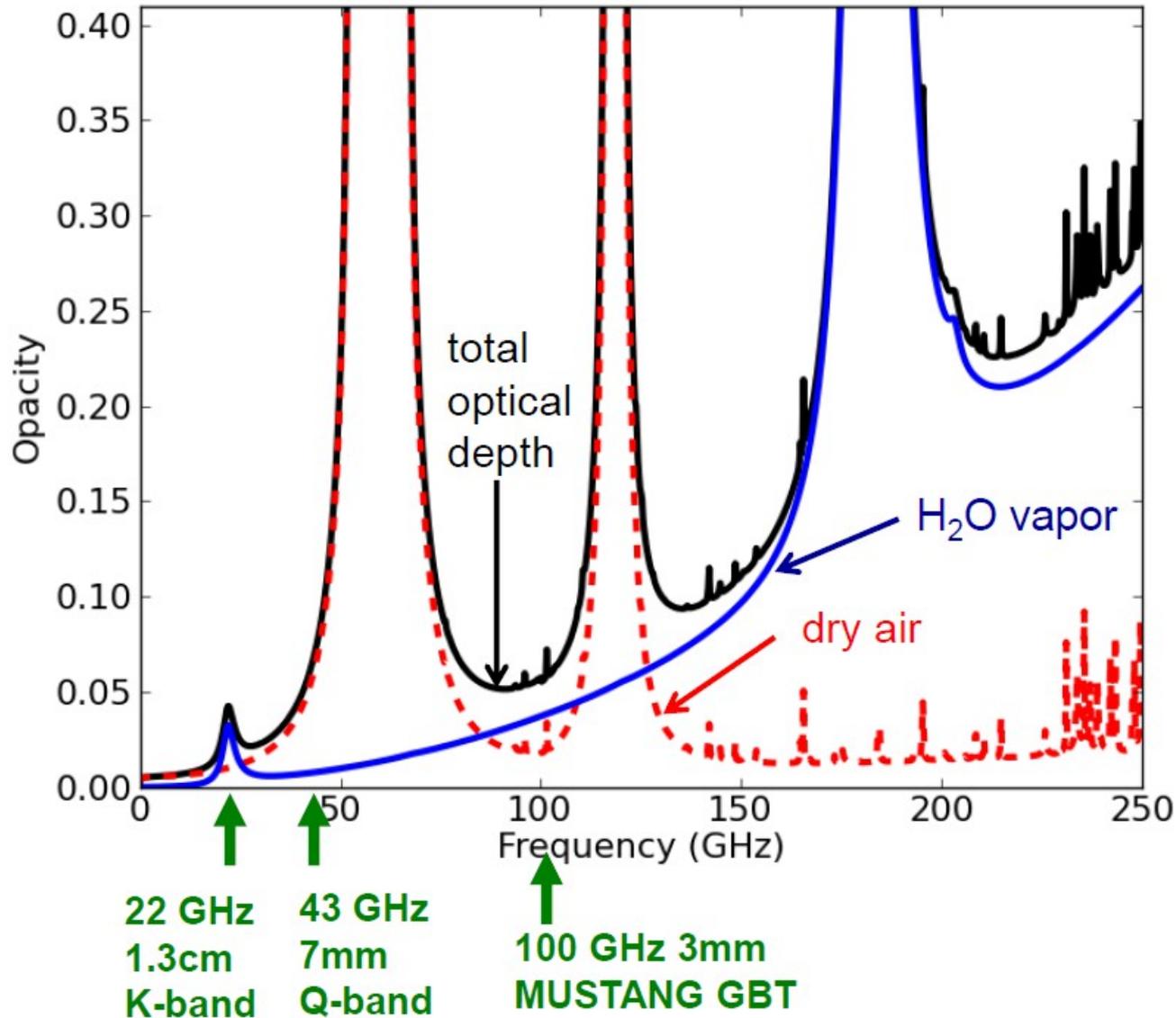
Column density as function of altitude



Peculiarities @ mm



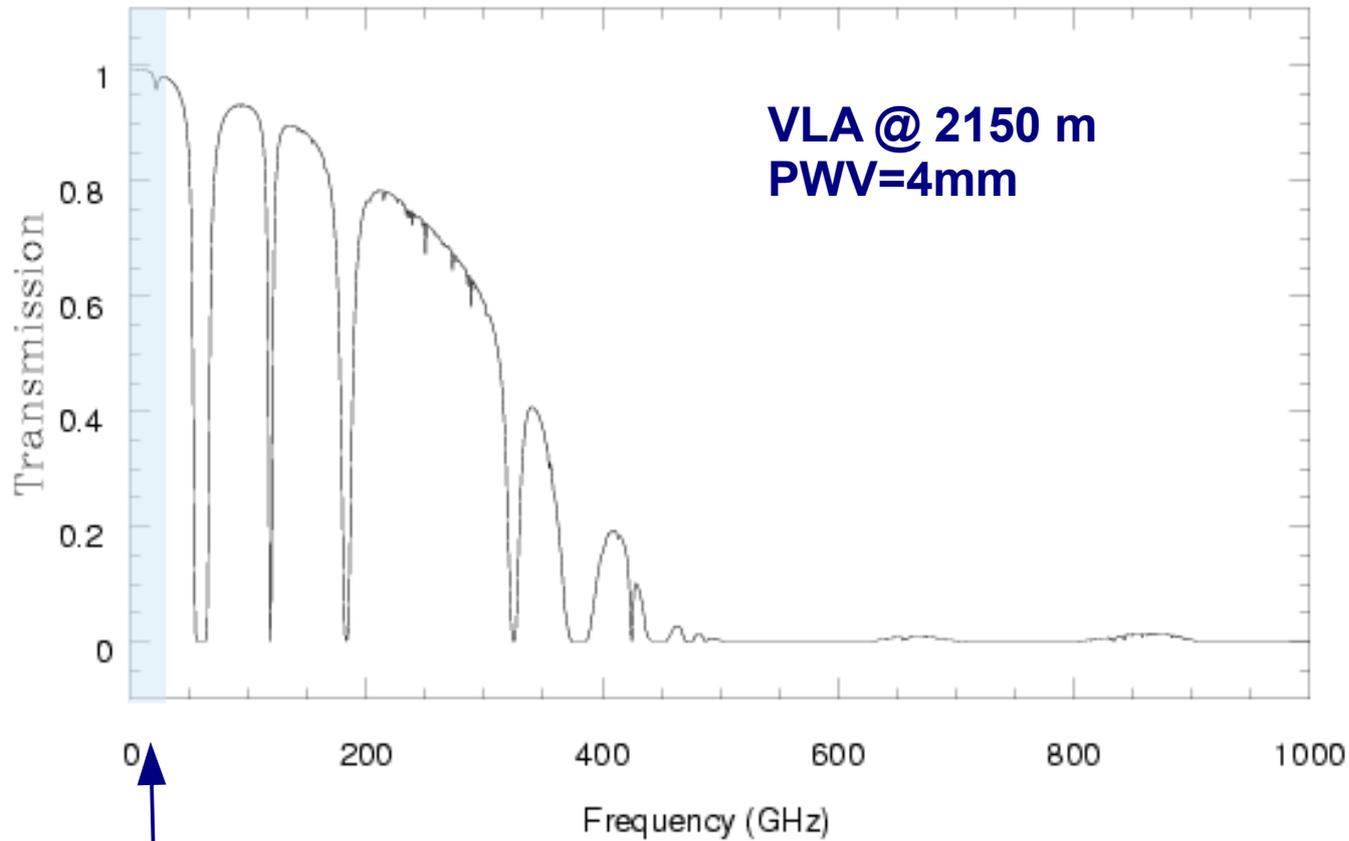
Optical depth as function of frequency



Peculiarities @ mm



Tropospheric opacity depends on altitude



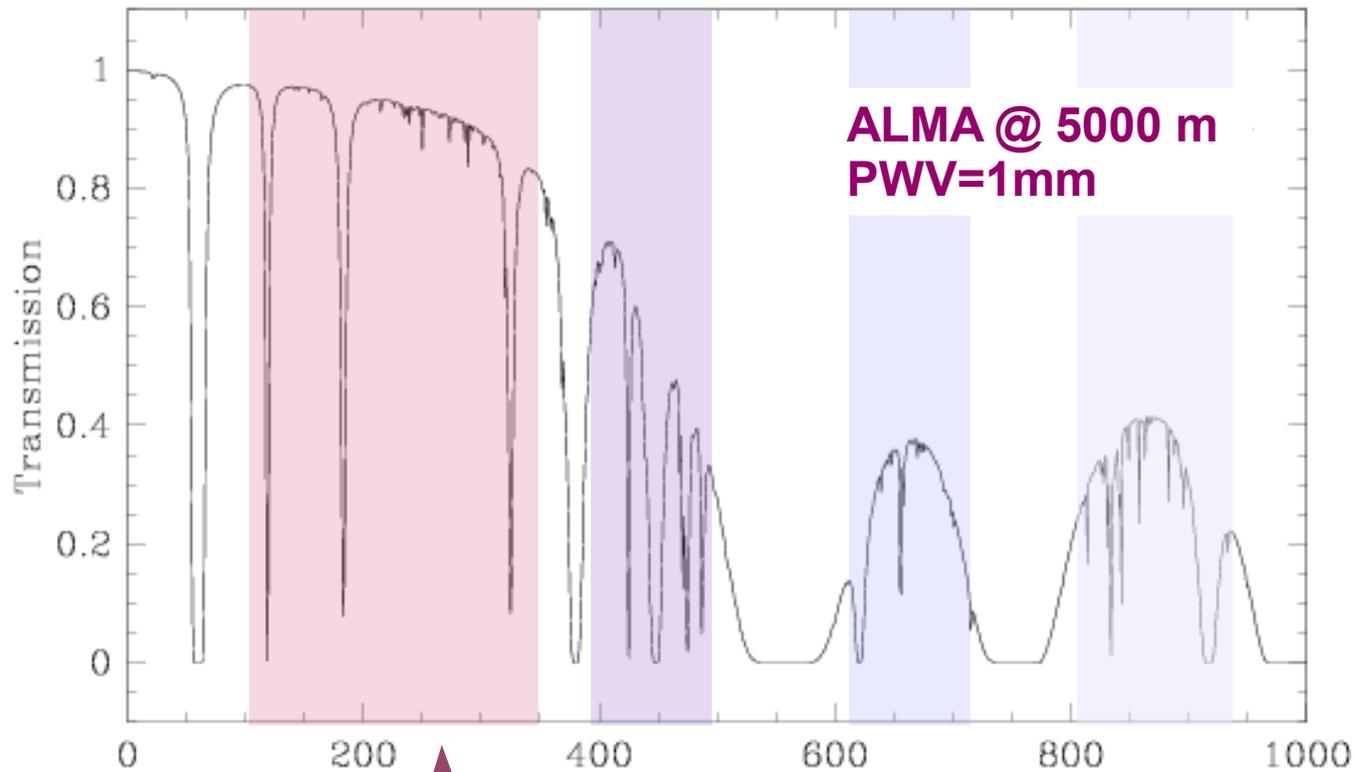
Atmospheric transmission not a problem @ $\lambda > \text{cm}$

↑
VLA bands

Peculiarities @ mm



Tropospheric opacity depends on altitude



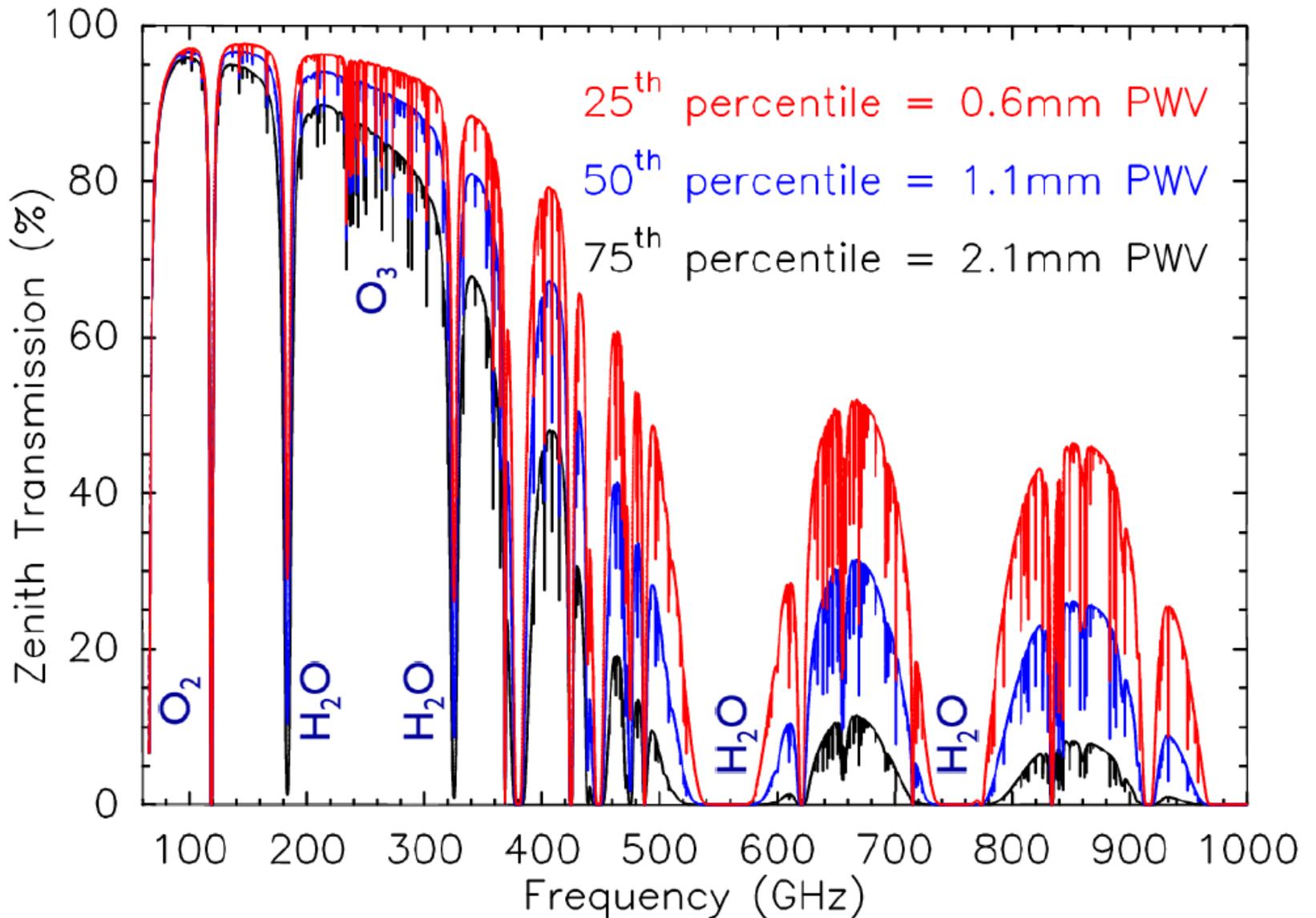
ALMA bands

Difference due to the scale height of water vapor

Peculiarities @ mm



PWV= Precipitable Water Vapour



Peculiarities @ mm



System noise temperature

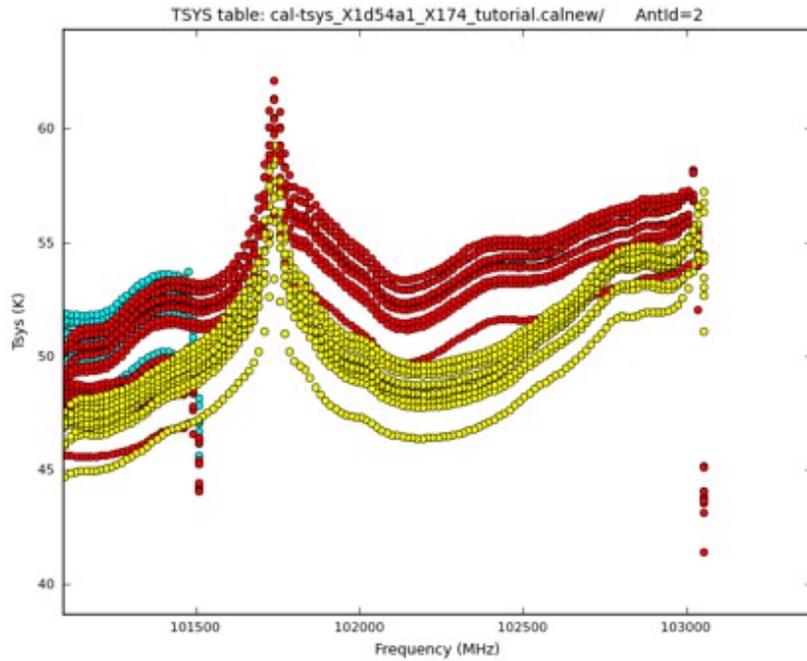
$$T_{\text{sys}} \sim T_{\text{atm}} (e^{\tau} - 1) + T_{\text{rx}} e^{\tau}$$

At lower frequencies T_{rx} is dominant

ALMA front end are equipped with an Amplitude Calibration Device (ACD)

→ T_{sys} and T_{rx}

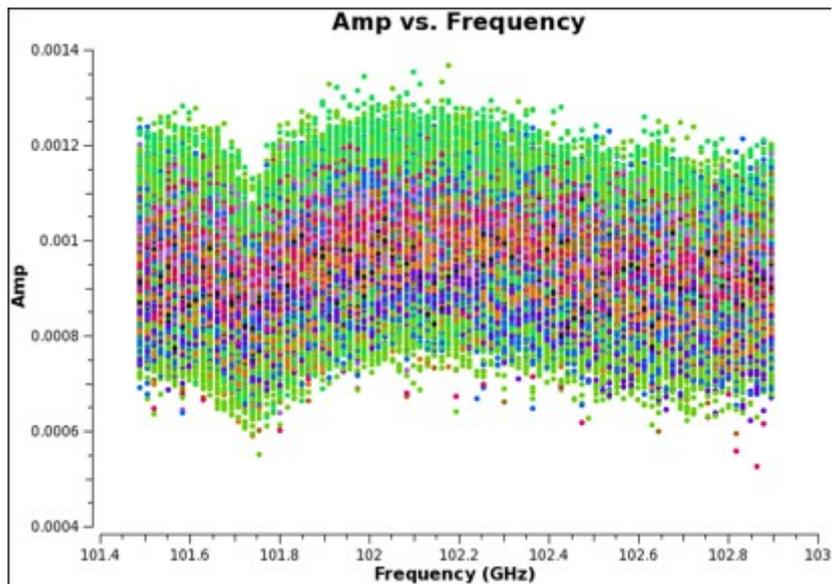
Peculiarities @ mm



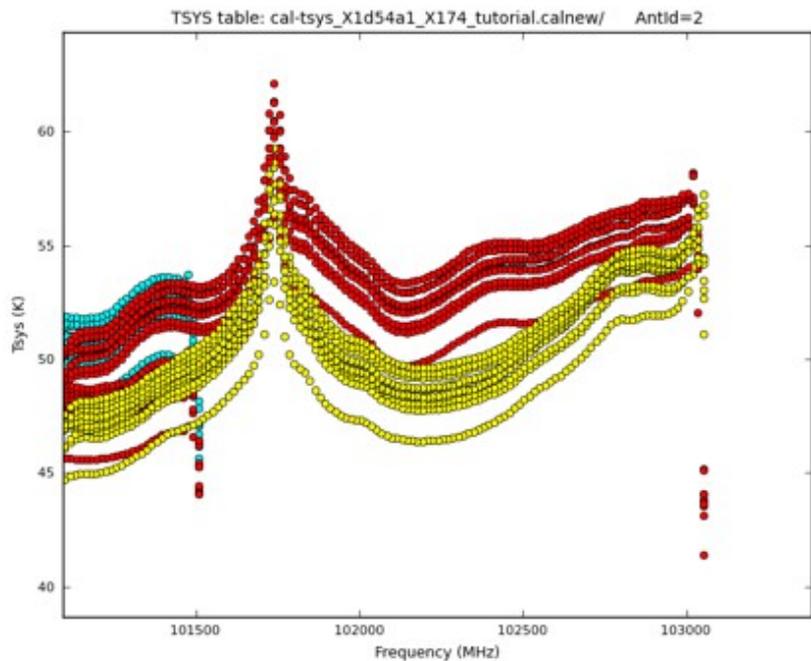
Tsys calibration

Spectral Tsys
band 3 (~100 GHz)

Before



Peculiarities @ mm

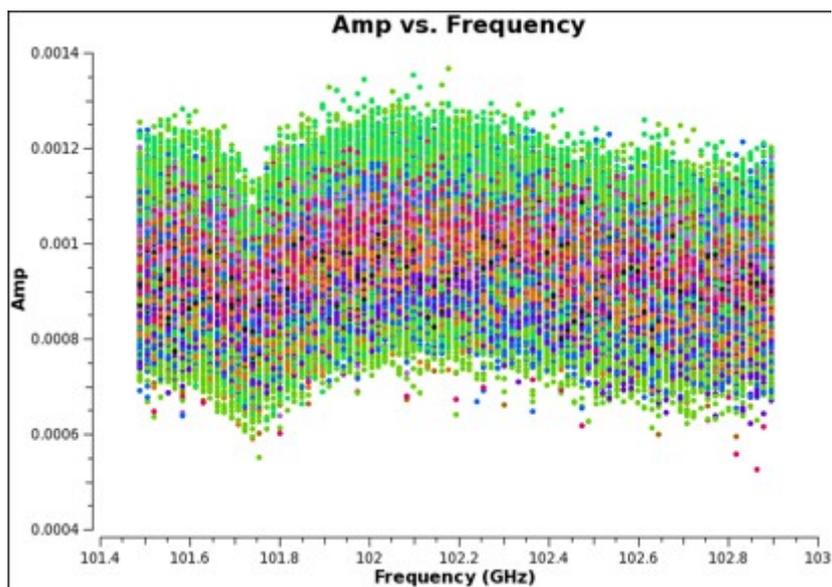


Tsys calibration

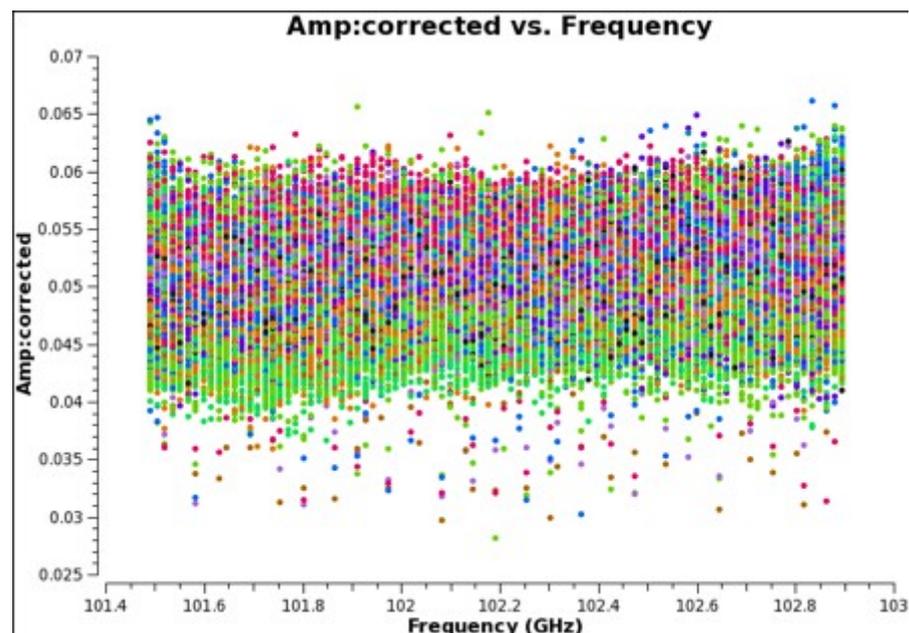


Spectral Tsys
band 3 (~100 GHz)

Before



After



Peculiarities @ mm



Mean effect of atmosphere on Phase

Variations in precipitable water vapor (PWV) cause phase fluctuations, worse at higher frequencies, resulting in:

- Phase shift due to refractive index $n \neq 1$
- Low coherence (loss of sensitivity)

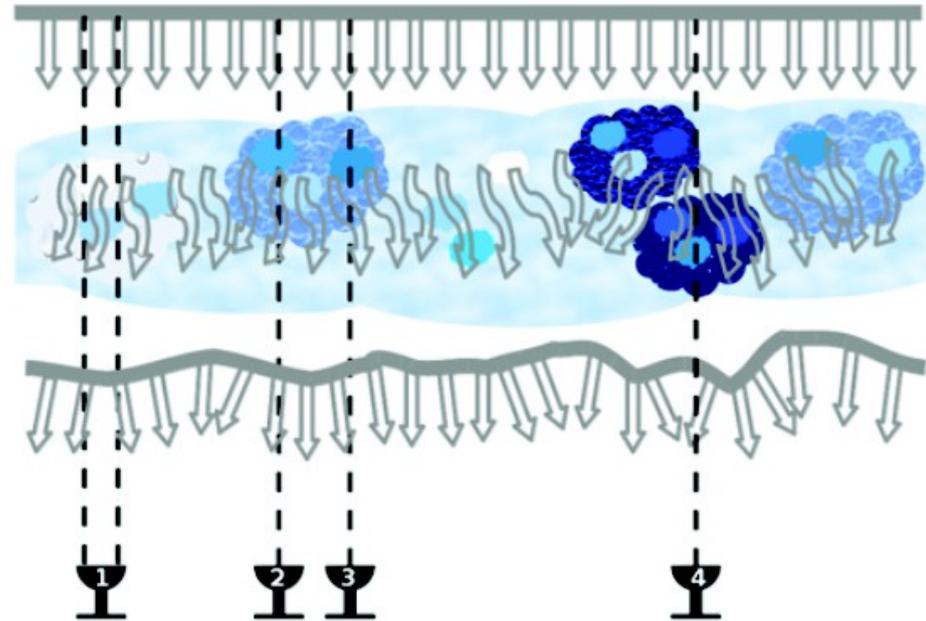
Patches of air with different pwv (and hence index of refraction) affect the incoming wave front differently.

Antenna 1, 2, 3 see slightly different disturbances

Sky above antenna 4 varies independently

The phase change experienced by an e.m. wave can be related to pwv

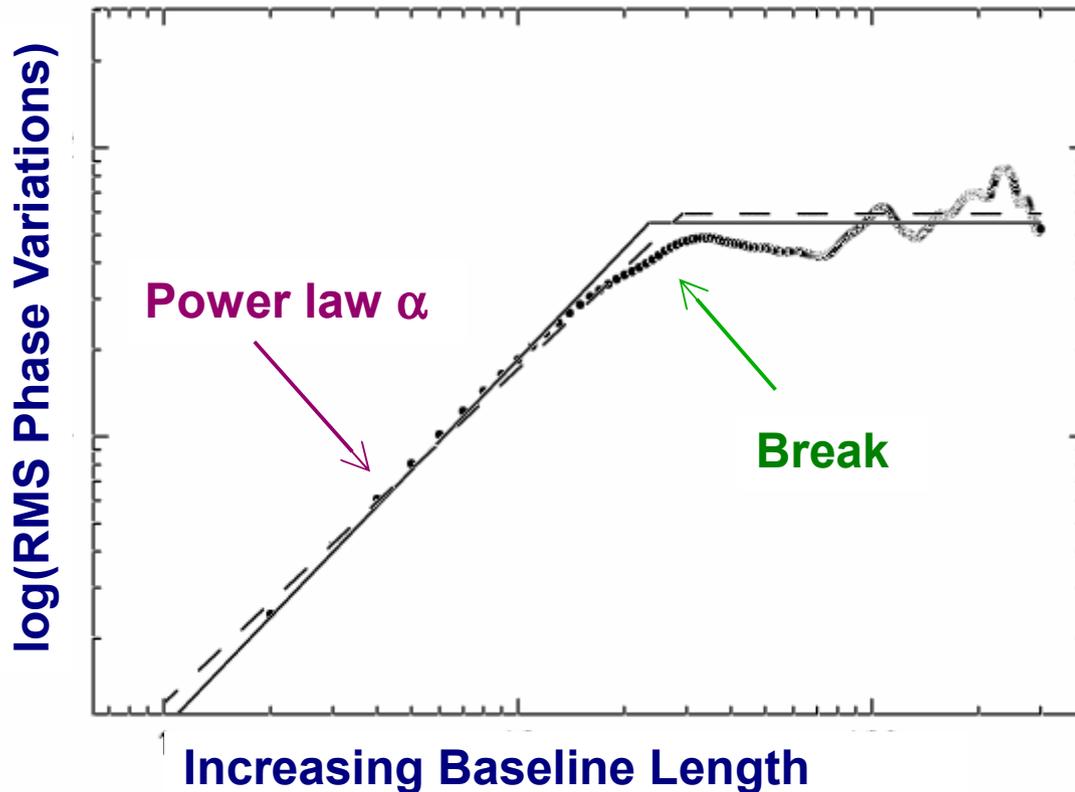
$$\varphi_e \approx \frac{12.6 \pi}{\lambda} \cdot pwv$$



Peculiarities @ mm



Atmospheric phase fluctuations



Phase noise

$$\varphi_{rms} = \frac{K b^\alpha}{\lambda}$$

Kolmogorov
turbulence
theory

b = baseline length (km)

α = 1/3 to 5/6 (thin or thick atmosphere)

λ = wavelength (mm)

K constant (~100 for ALMA)

The break is typically @ baseline lengths
few hundred meters to few km
(scale of the turbulent layers)

Break and maximum are weather
and wavelength dependent

Peculiarities @ mm



Atmospheric phase fluctuations → decorrelation

We lose integrated flux because visibility vectors partly cancel out

$$\langle V \rangle = V_0 \langle e^{i\varphi} \rangle = V_0 e^{-(\varphi_{rms}^2)/2}$$

$$\varphi_{rms} = 1 \text{ radian} \rightarrow \langle V \rangle = 0.60 V_0$$

In summary

Fluctuations in the line-of-sight pwv of an antenna cause phase variations of the order of ~30 deg / sec at 90 GHz, and scales linearly with frequency....

$$\varphi_e \approx \frac{12.6\pi}{\lambda} \cdot pwv$$

and the phase noise is worse at longer baselines...

$$\varphi_{rms} = \frac{K b^\alpha}{\lambda}$$

Peculiarities @ mm

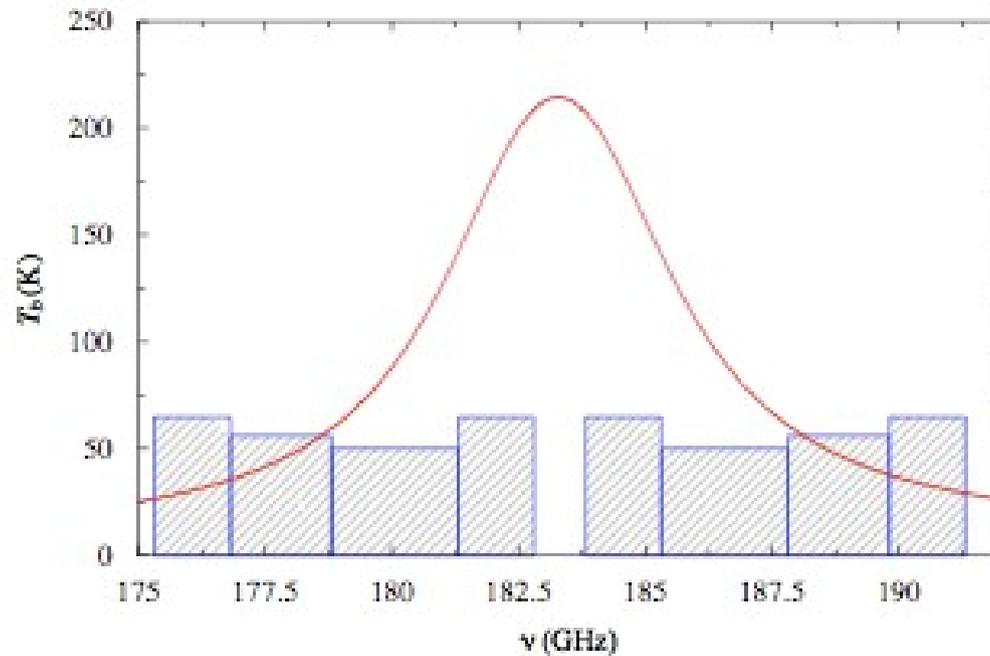


WVR correction

Each ALMA 12 m antenna has a water vapour radiometer

Four “channels” flanking the peak of the 183 GHz water line

Data taken every second



Peculiarities @ mm



WVR correction

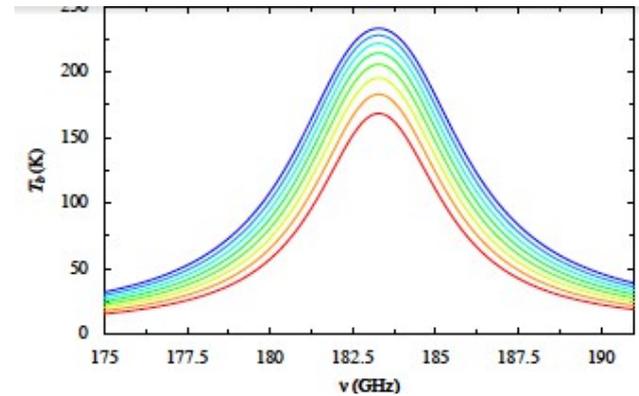
Each ALMA 12 m antenna has a water vapour radiometer

Four “channels” flanking the peak of the 183 GHz water line

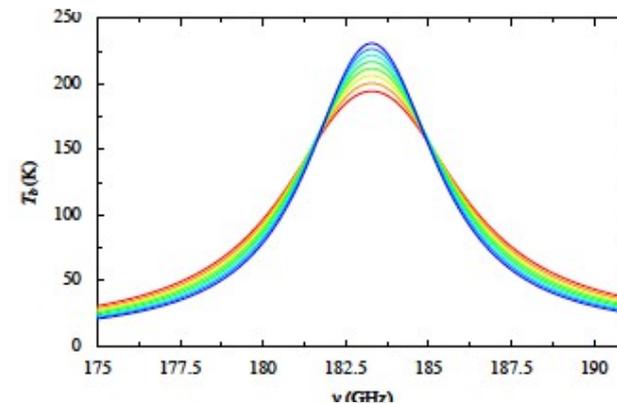
Data taken every second

Convert 183 GHz brightness to PWV (wvrgcal):
model PWV, temperature and pressure
compare to the observed “spectrum”
compute the correction:

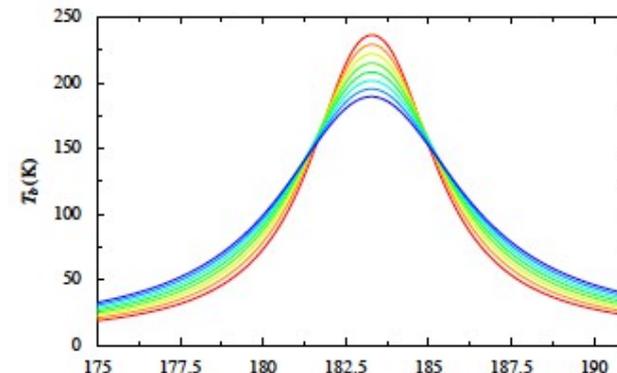
$$\varphi_e \approx \frac{12.6 \pi}{\lambda} \cdot pwv$$



PWV from 0.6 to 1.3 mm



Temperature 230-300 K



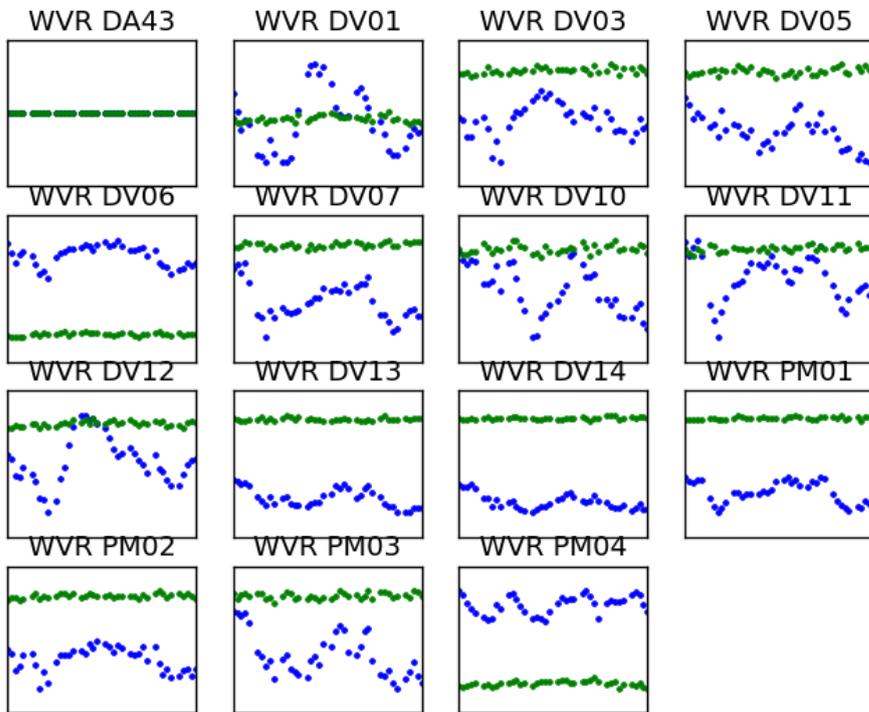
Pressure 400-750 mBar

Peculiarities @ mm



WVR correction

Band 6 (230 GHz)



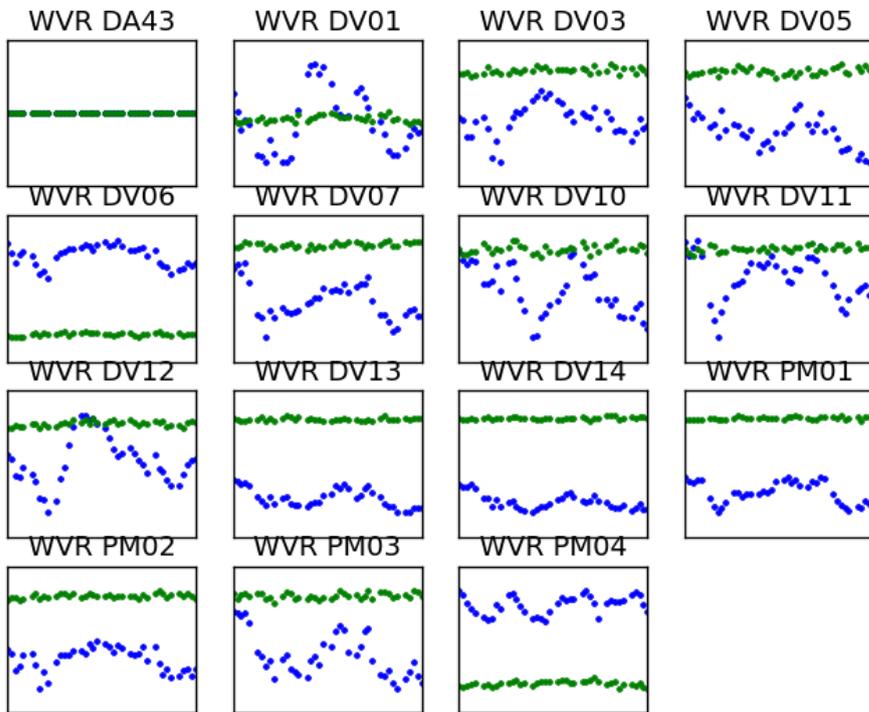
Raw phases & WVR corrected phases

Peculiarities @ mm

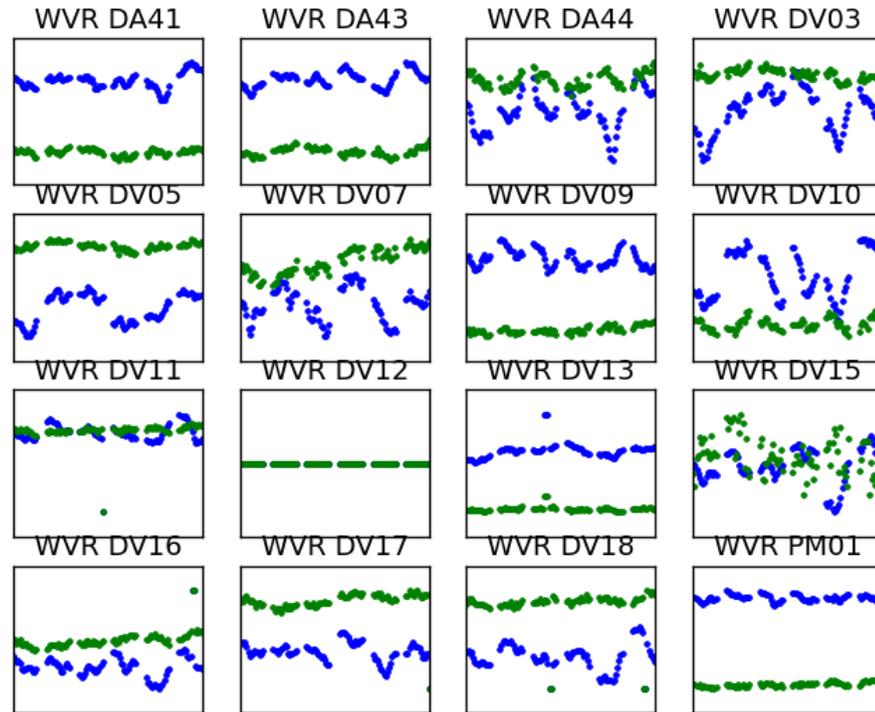


WVR correction

Band 6 (230 GHz)



Band 7 (340 GHz)



Raw phases & WVR corrected phases

Peculiarities @ mm

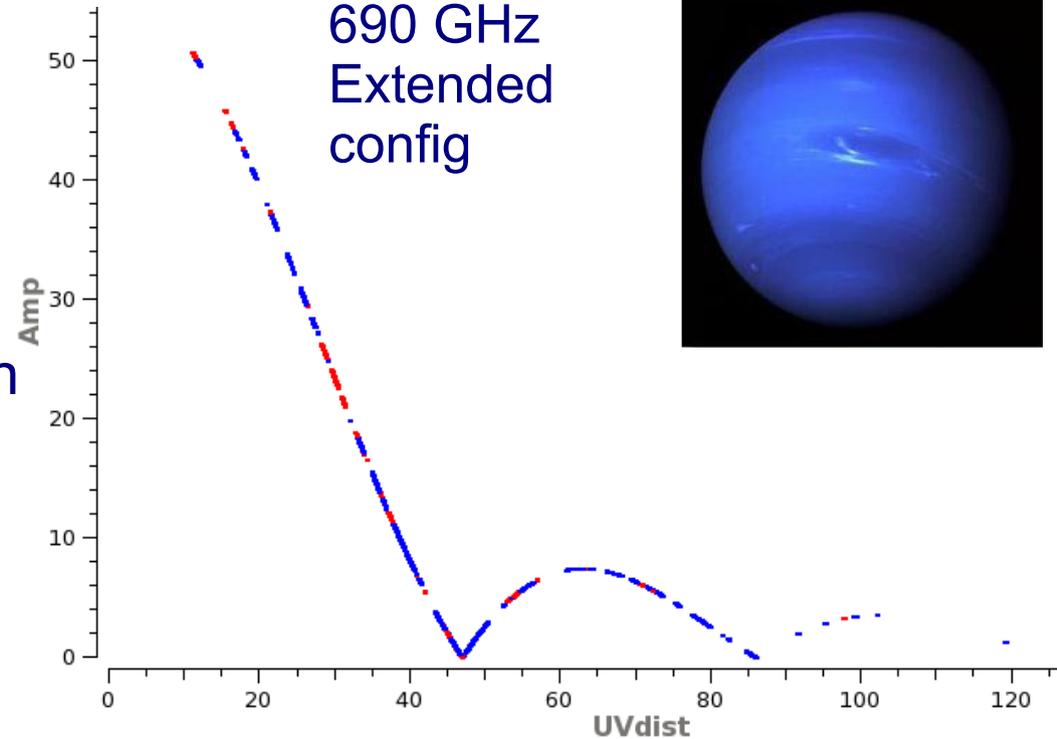


Flux calibrators

- Quasars are strongly time-variable and good models do not exist at high frequencies
- Solar System bodies are used as primary flux calibrators (Neptune, Jovian moons, Titan, Ceres) but with many challenges:
 - **all are resolved on long baselines**
 - **brightness varies with distance from Sun and Earth**
 - **line emission present → need models**

Other possibilities: asteroids,
red giant stars...
Monitoring of point-like quasars

Neptune
690 GHz
Extended
config



Peculiarities @ mm

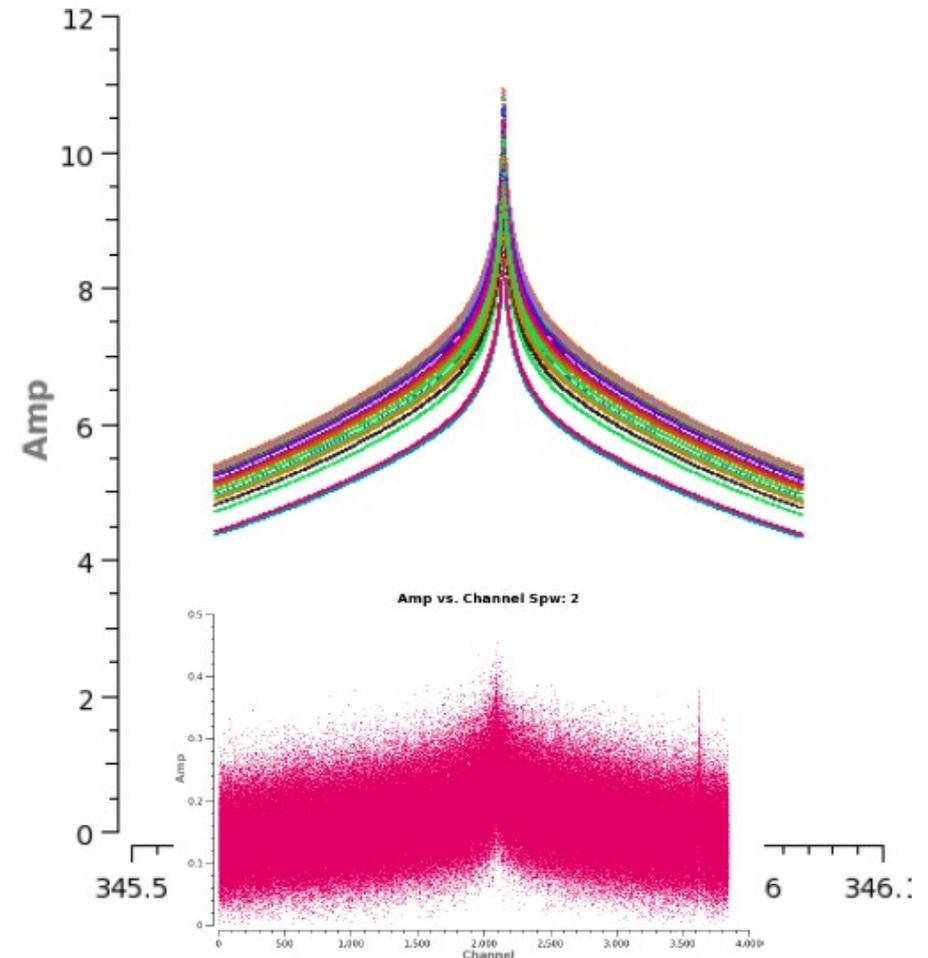


Flux calibrators

Model spectral lines: CO in Titan

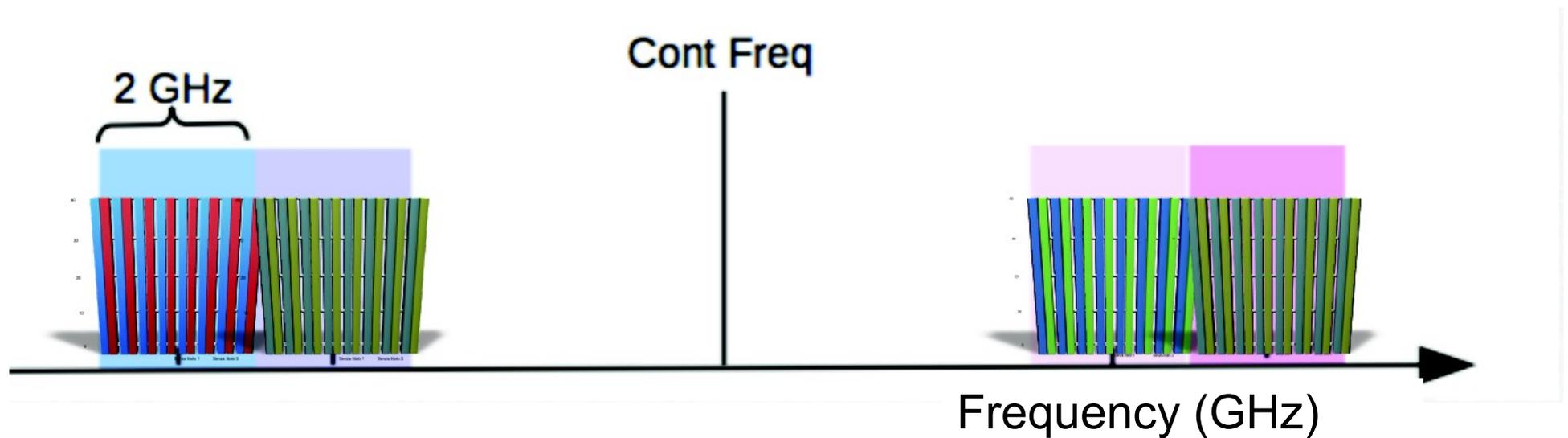


Amp vs. Frequency



Interferometric data

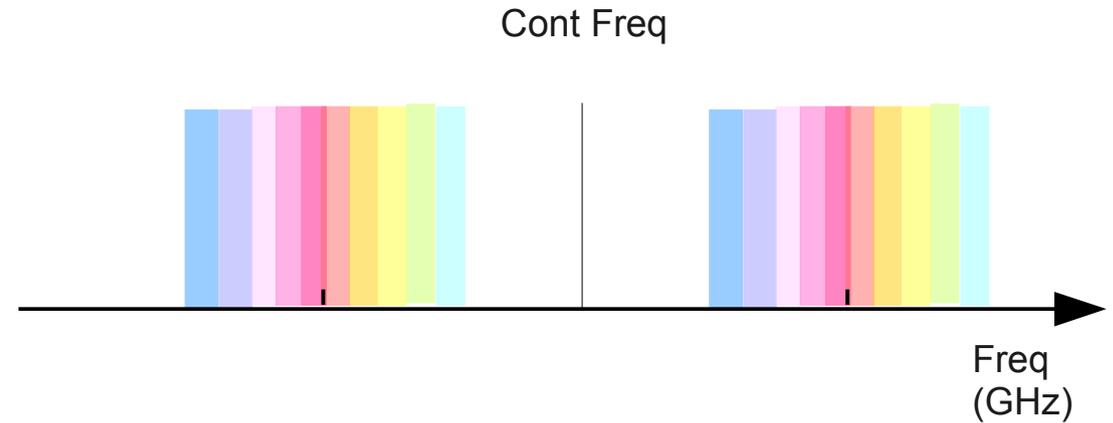
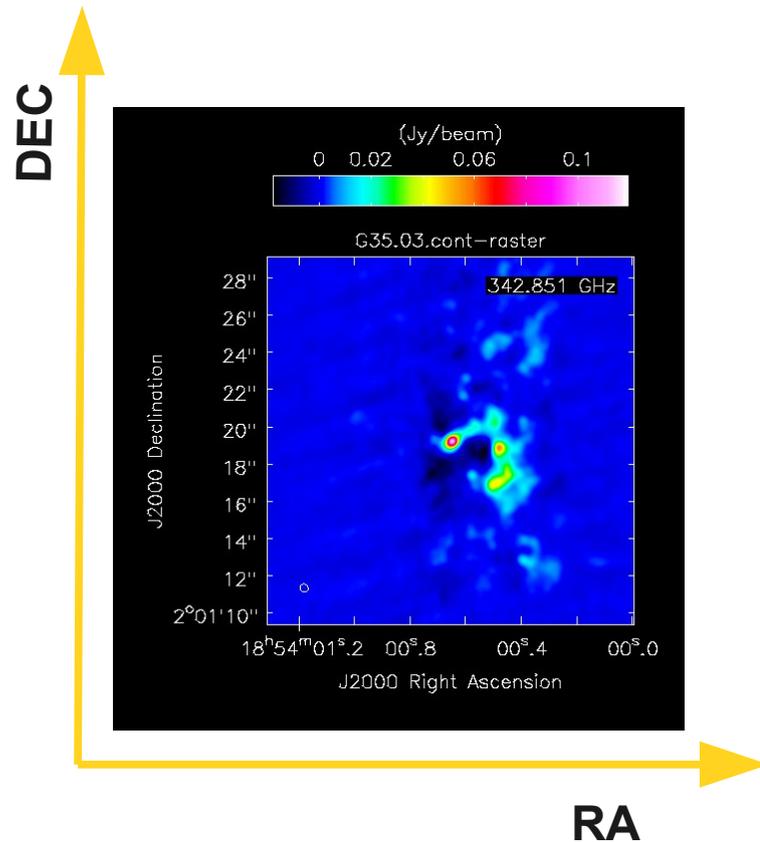
Modern interferometric observations are taken in multi-channel mode regardless if they are continuum or line observations



Data are actually **data cube**:
from each channel (freq, velocity) 1 uv-plane

Interferometric data

Continuum images are obtained combining all the (line-free) channels.

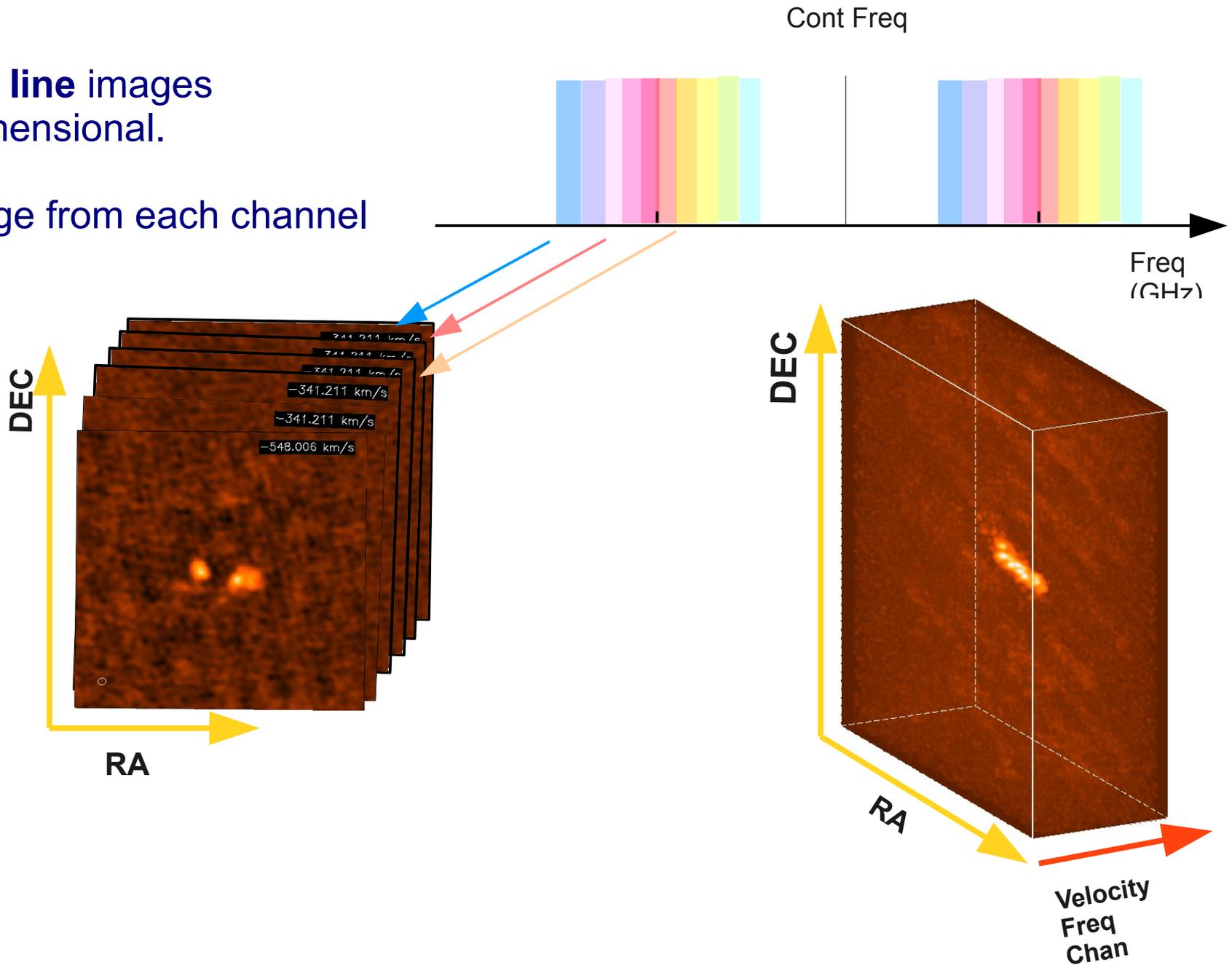


The resulting image is a 2-Dimensional image at the central frequency.

Interferometric data

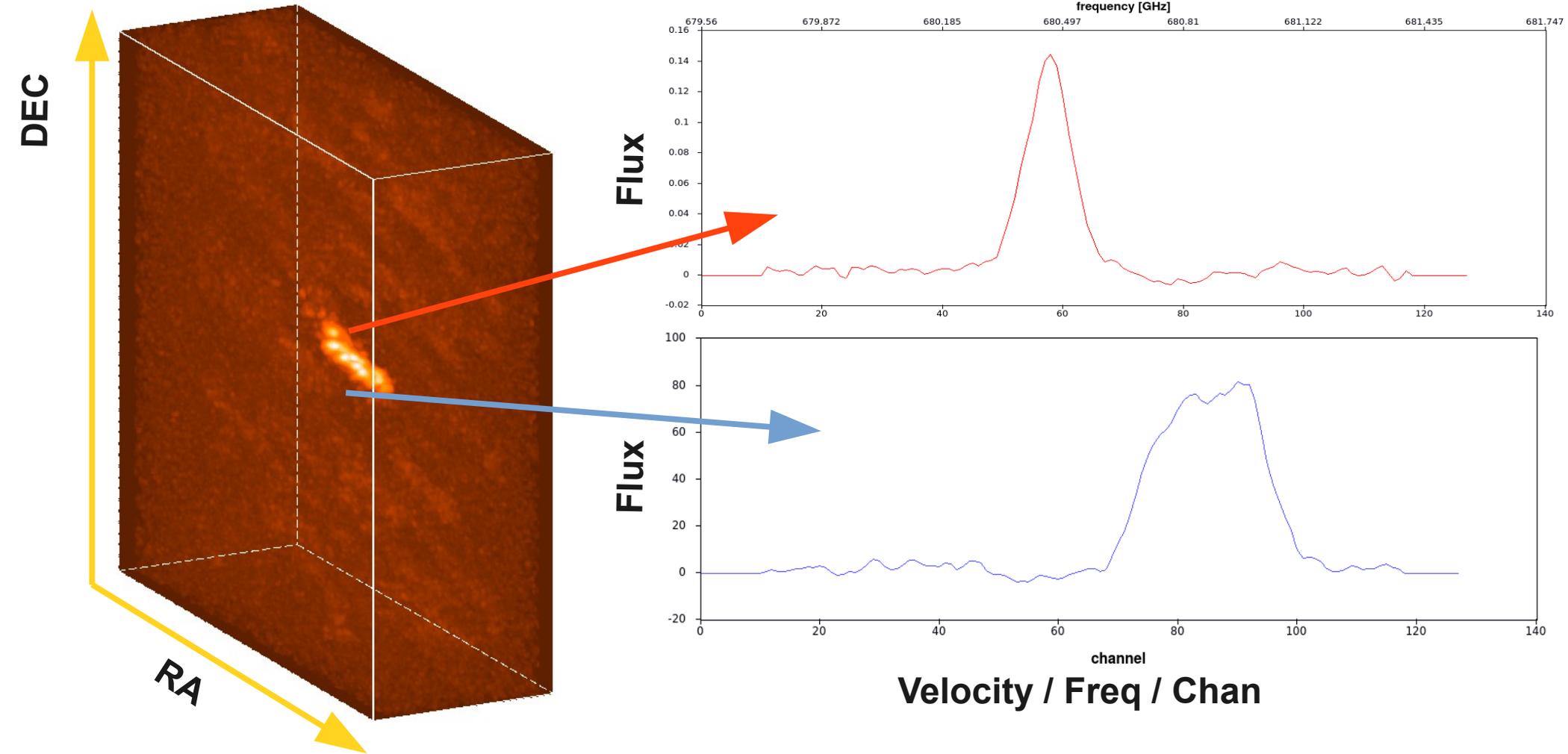
Spectral line images are 3-dimensional.

One image from each channel



Spectral lines

1-D slice along velocity axis



From each pixel one spectrum

Laboratorio ALMA

IRA – Quarto piano (stanza in fondo al corridoio)

Lun 17, mar 18 ore 09:00 – 13:00

Mer 19 seminario **UniBO**

Gio 20, Ven 21 ore 09:00 – 17:00

Lun 24, mar 25, mer 26 ore 09:00 – 13:00

Gio 27, Ven 28 ore 09:00 – 17:00