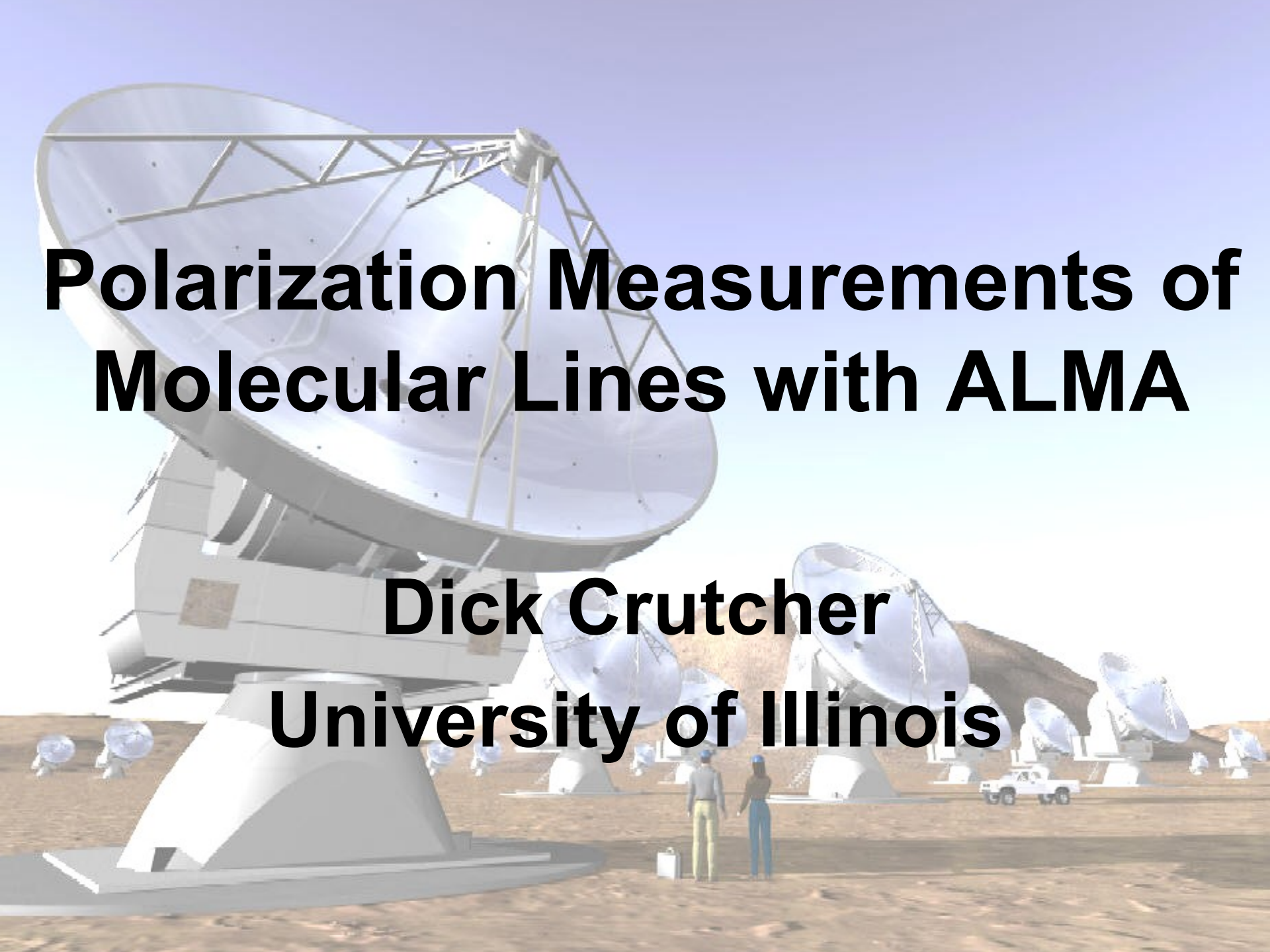


A 3D rendering of the Atacama Large Millimeter/submillimeter Array (ALMA) in a desert landscape. The foreground features a large, white, parabolic radio telescope dish mounted on a complex metal structure. In the background, several other similar dishes are visible, along with a small white utility vehicle and two human figures for scale. The sky is a clear, light blue.

Polarization Measurements of Molecular Lines with ALMA

Dick Crutcher
University of Illinois

Why bother with polarization?

Magnetic fields!

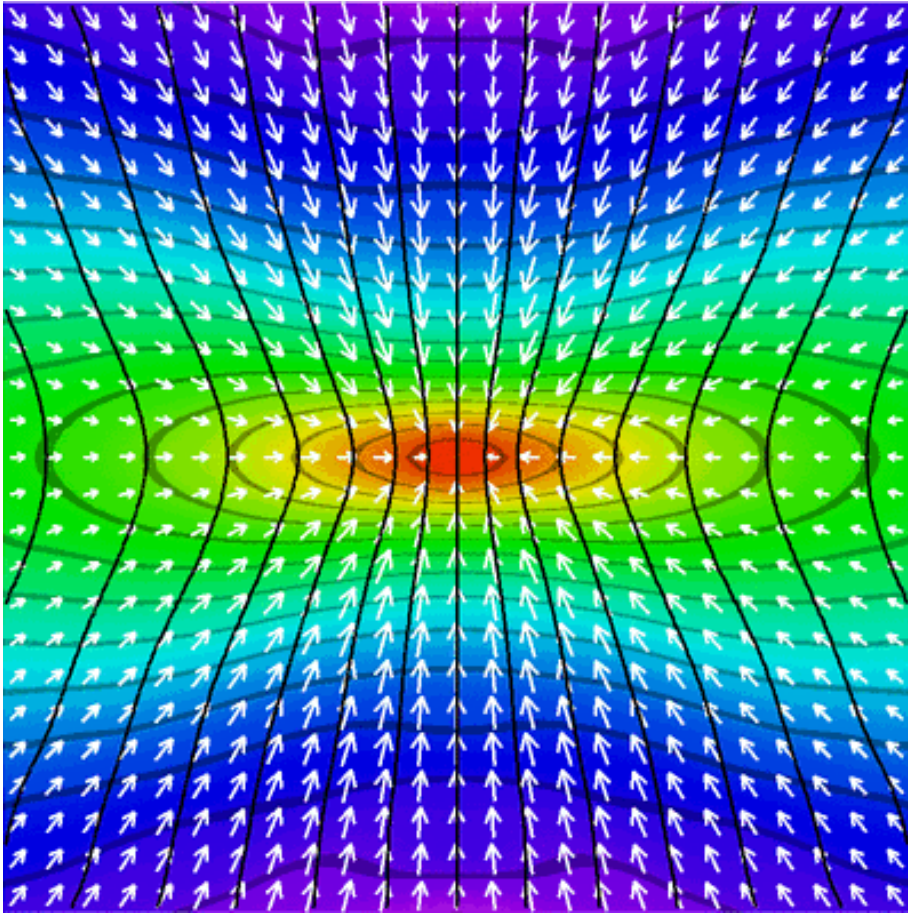
Why magnetic fields?

“Magnetic fields are to astrophysicists what sex is to psychoanalysts.”

- H. C. van de Hulst

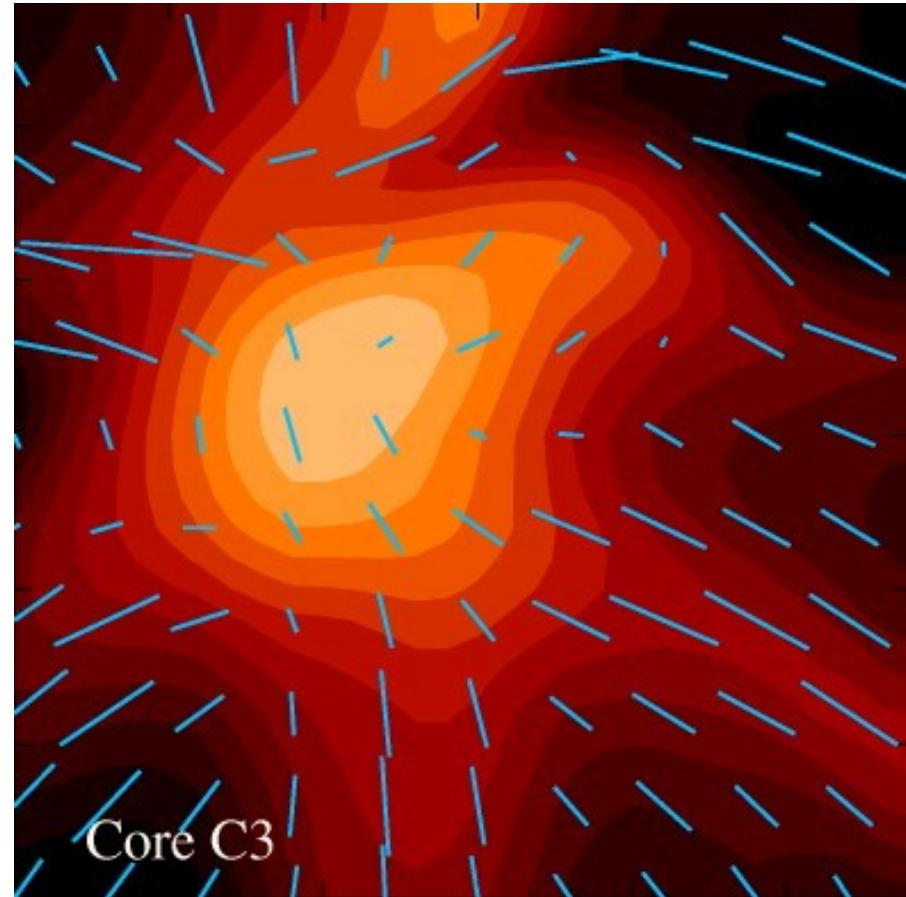
Magnetic Field Morphology

strong field case



Fiedler and Mouschovias (1993)

weak field case



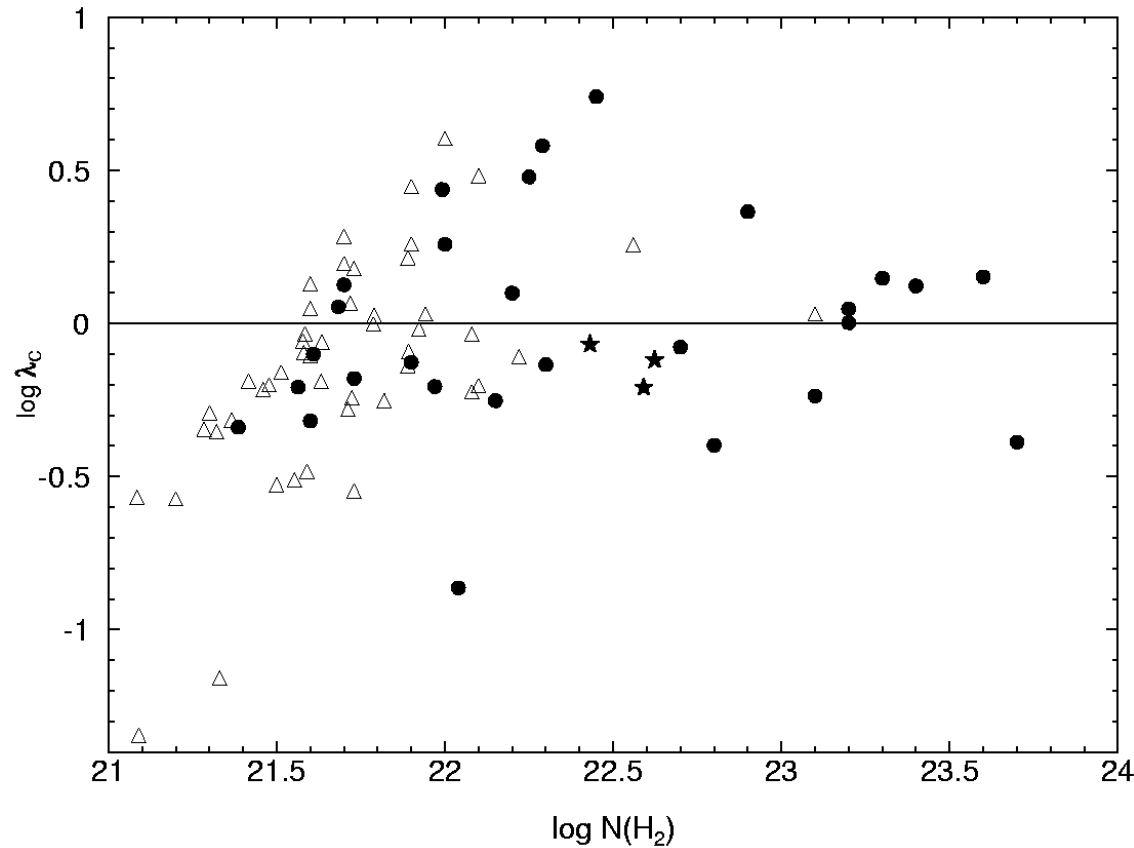
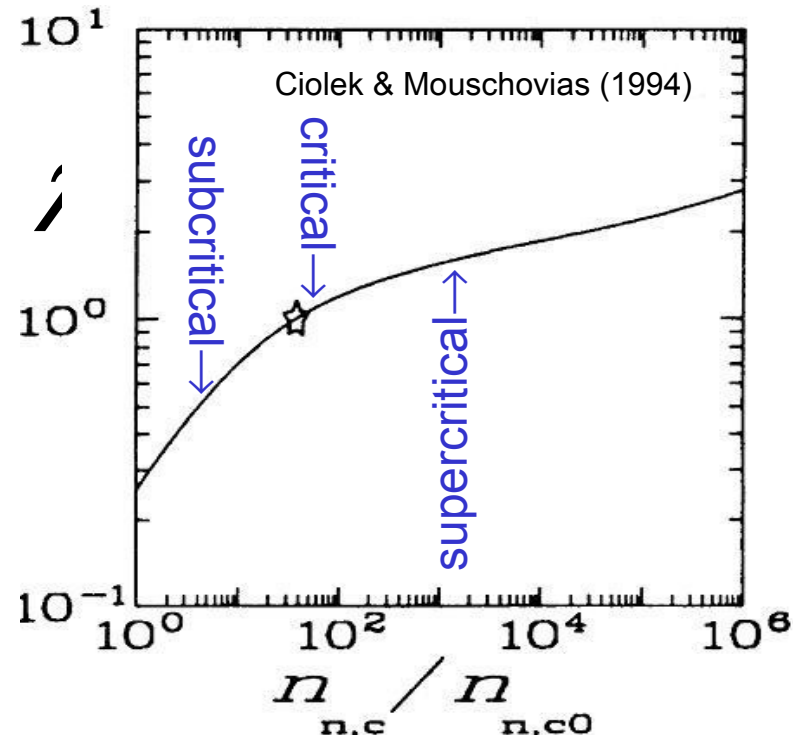
Padoan et al (2001)

Mass-to-Flux Ratio: M/Φ

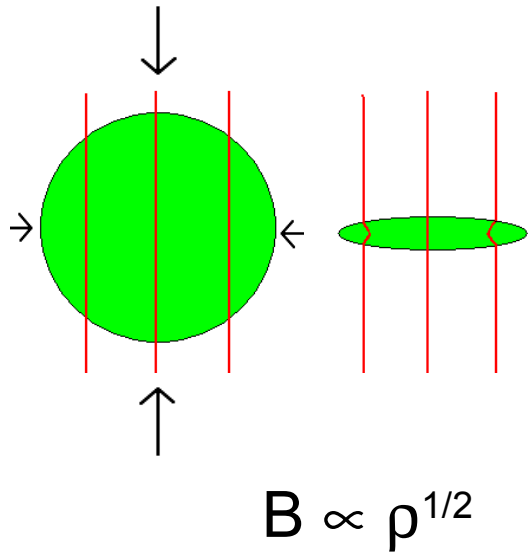
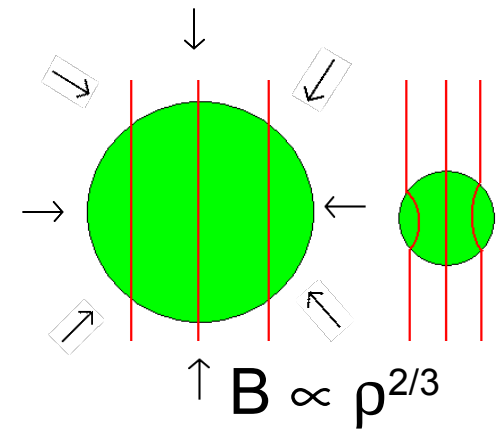
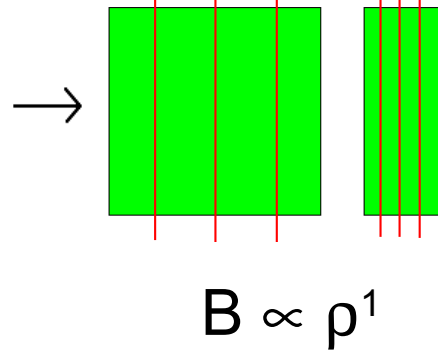
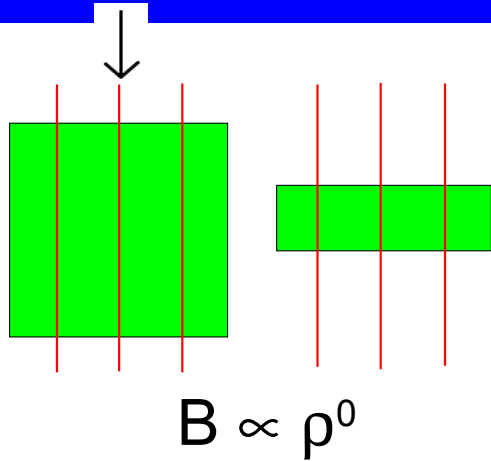
mass/flux ratio $\equiv$ gravitational collapse / magnetic support

$$\frac{M_{\text{observed}}}{\Phi_{\text{observed}}} \propto \frac{N(\text{H}_2)}{B}$$

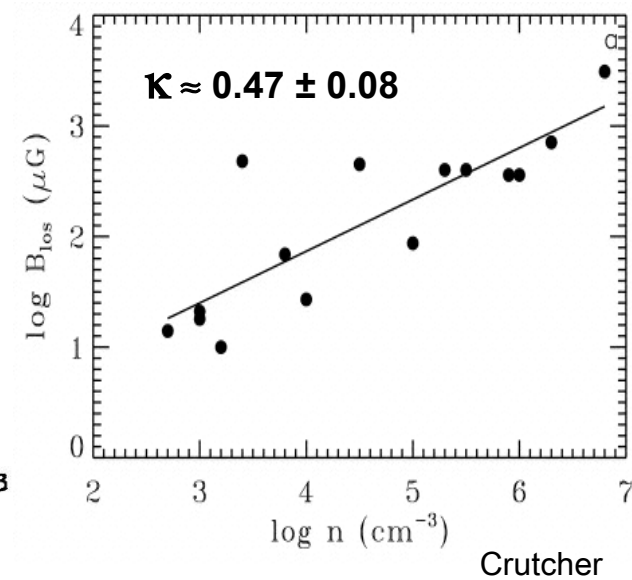
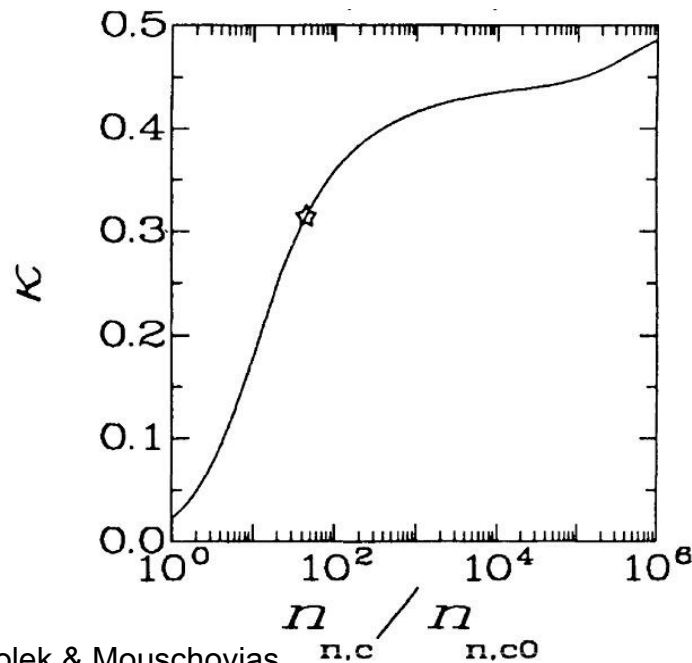
$$\lambda \equiv \frac{(M/\Phi)_{\text{observed}}}{(M/\Phi)_{\text{critical}}}$$



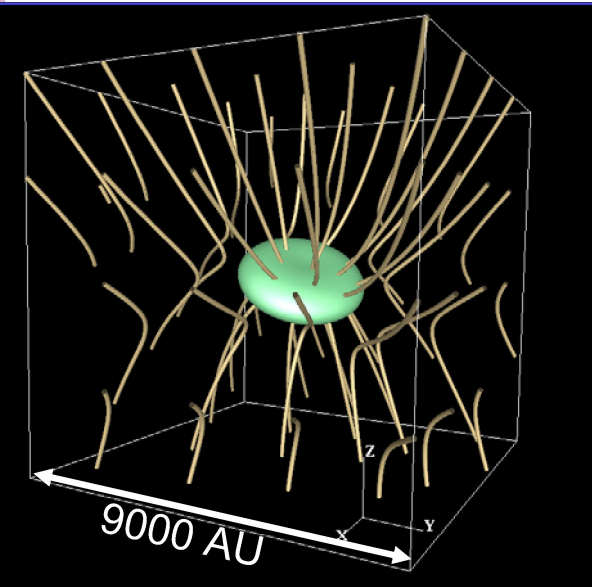
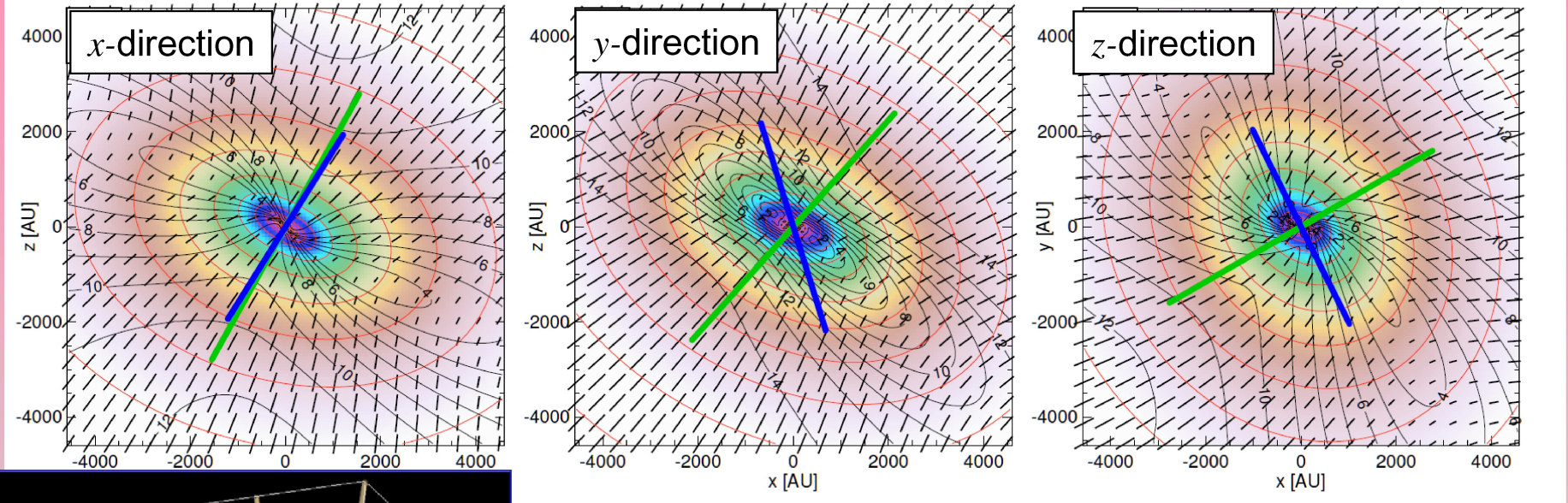
Scaling of B with ρ : $B \propto \rho^\kappa$



Magnetic support,
ambipolar diffusion



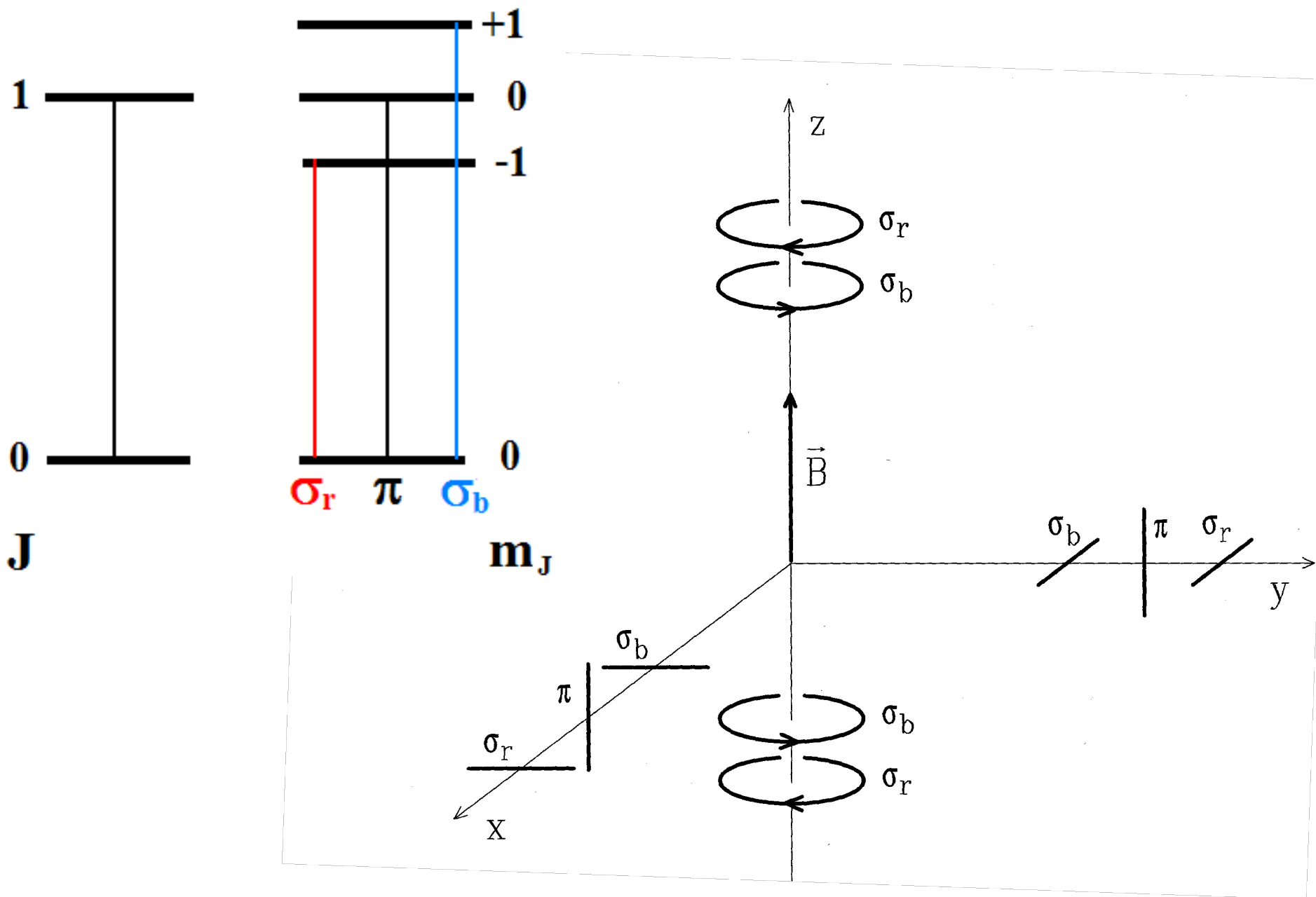
Polarization vectors at 5000 AU scale (Weak field model: $\langle B \rangle = 50.1 \mu\text{G}$)



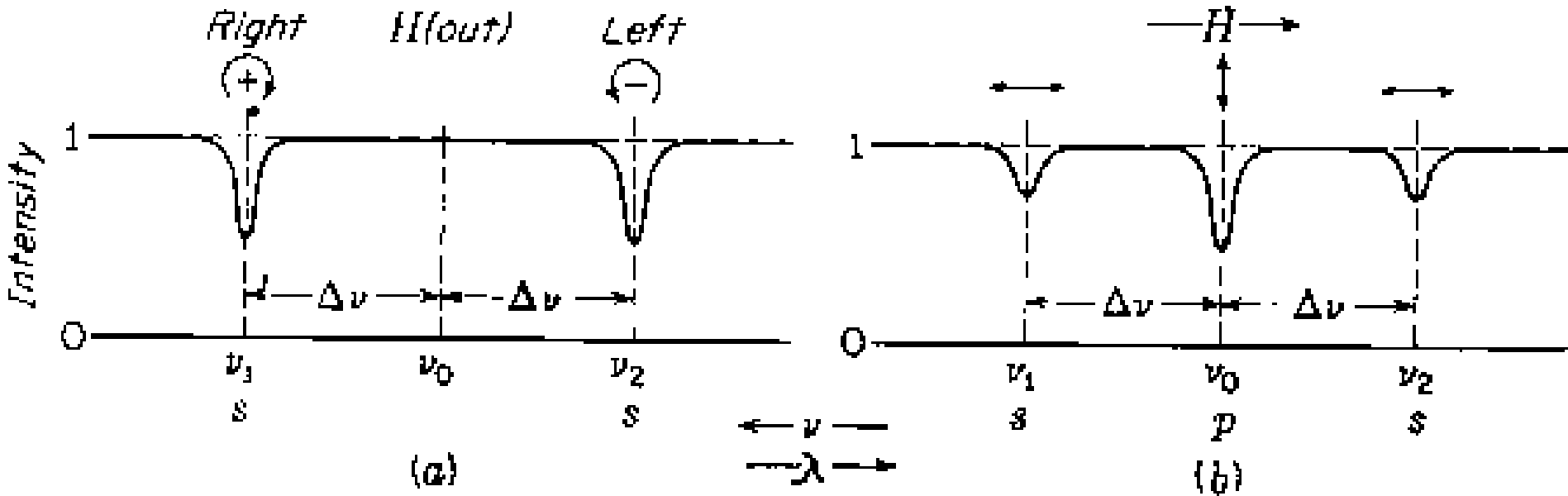
Tree-dimensional angle between the magnetic field and the outflow is 53.5 deg.

- The alignment depends on the line of sight.
- The direction of the central B cannot be inferred from a polarization map of the cloud core scale directly.
- The direction of the central B can be probed by the outflow.

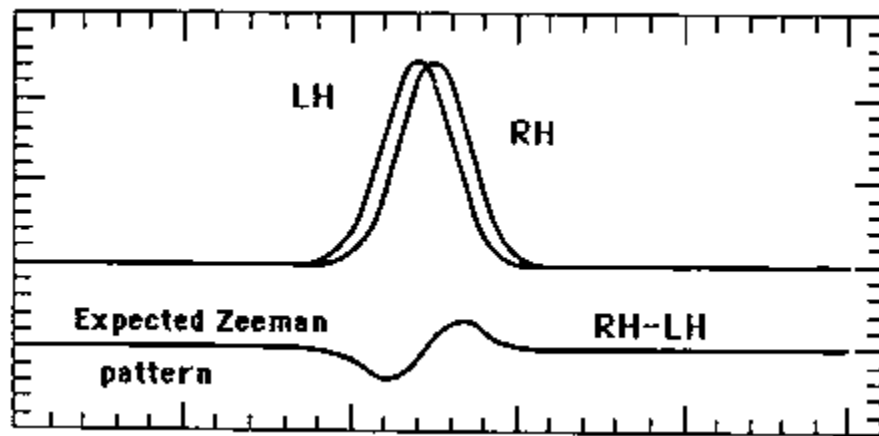
Zeeman Effect (1)



Zeeman Effect (2)



$$\Delta\nu_z = |\mathbf{B}| Z, \quad Z \approx 1 - 2 \text{ Hz}/\mu\text{G}, \quad (Z_{\text{HI}} = 1.4 \text{ Hz}/\mu\text{G})$$



$$V = L - R \propto (dI/d\nu)(\Delta\nu_z \cos\theta) \Rightarrow$$

line of sight $\mathbf{B}$

$$Q \text{ or } U \propto (d^2I/d\nu^2)(\Delta\nu_z \sin\theta)^2 \Rightarrow$$

plane of sky $\mathbf{B}$ (not really)

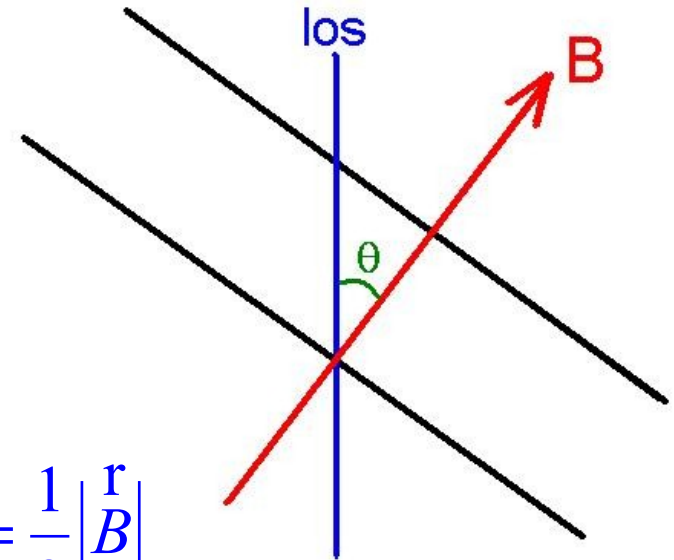
$$(dI/d\nu)\Delta\nu_z \propto |(\Delta\nu_z / \Delta\nu_{\text{FWHM}})|$$

Zeeman Effect (3)

$$V \propto \frac{dI}{dv} \Delta v_z \cos \theta, \quad \Delta v_z \propto \left| \frac{\mathbf{r}}{B} \right|$$

$$\Rightarrow B_{los} = \left| \frac{\mathbf{r}}{B} \right| \cos \theta$$

$$\langle B_{los} \rangle = \int_0^{\pi/2} \left| \frac{\mathbf{r}}{B} \right| \cos \theta \sin \theta d\theta / \int_0^{\pi/2} \sin \theta d\theta = \frac{1}{2} \left| \frac{\mathbf{r}}{B} \right|$$

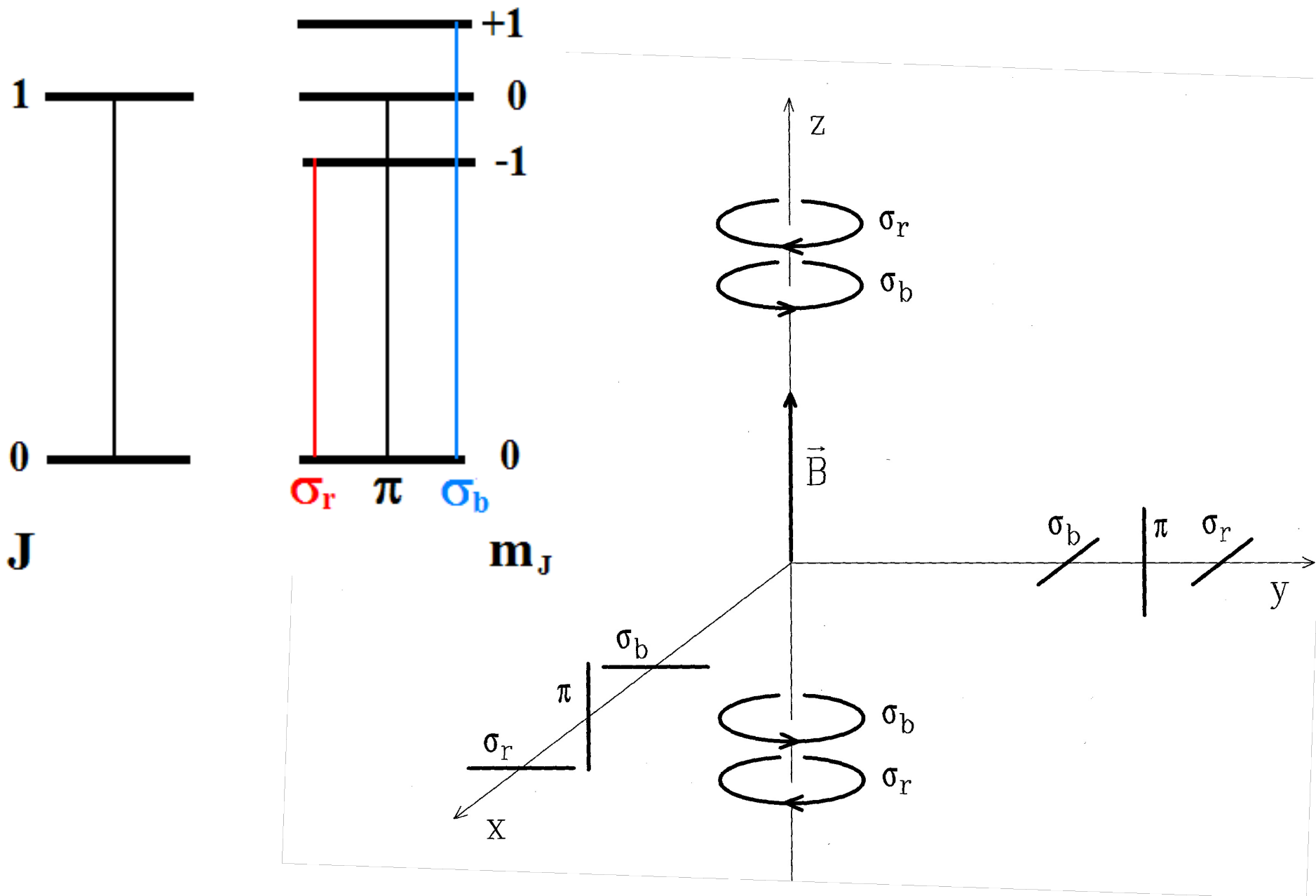


$$\frac{M}{\Phi} \propto \frac{N_B}{B} = \frac{N_{los} \cos \theta}{B_{los} / \cos \theta} = \frac{N_{los}}{B_{los}} \cos^2 \theta$$

$$\left\langle \frac{M}{\Phi} \right\rangle = \int_0^{\pi/2} \left(\frac{M_{obs}}{\Phi_{obs}} \right) \cos^2 \theta \sin \theta d\theta / \int_0^{\pi/2} \sin \theta d\theta = \frac{1}{3} \left(\frac{M_{obs}}{\Phi_{obs}} \right)$$

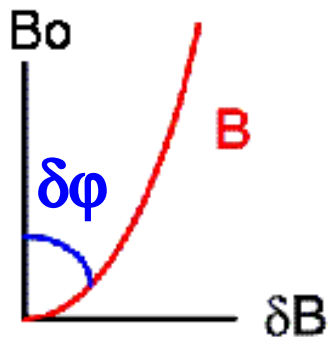
$$\lambda_c = \frac{1}{3} \lambda_{obs}$$

Goldreich-Kylafis Effect (1)



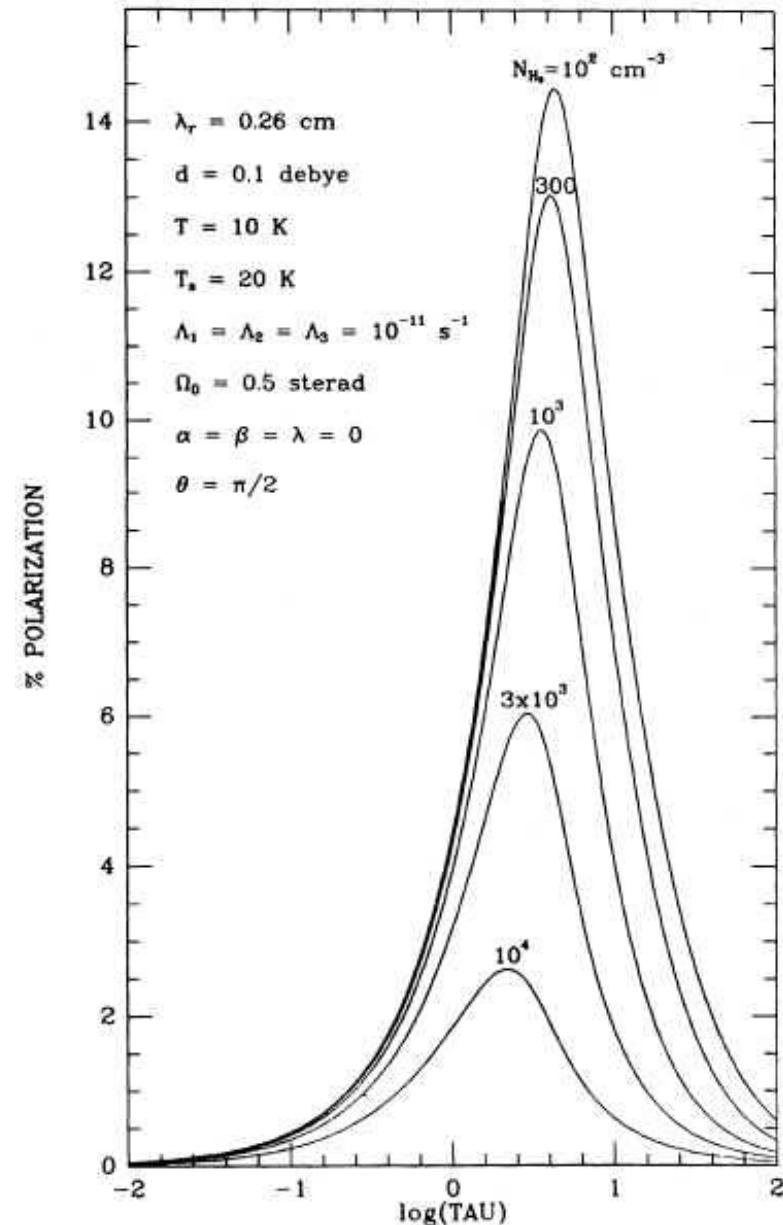
Goldreich-Kalafis Effect (2)

- Local anisotropy in line optical depth $\Rightarrow$
- anisotropy in radiation field $\Rightarrow$
- non-LTE population of magnetic sublevels $\Rightarrow$
- linear polarization $\perp$ or $\parallel$ **B**
- Chandrasekhar & Fermi:

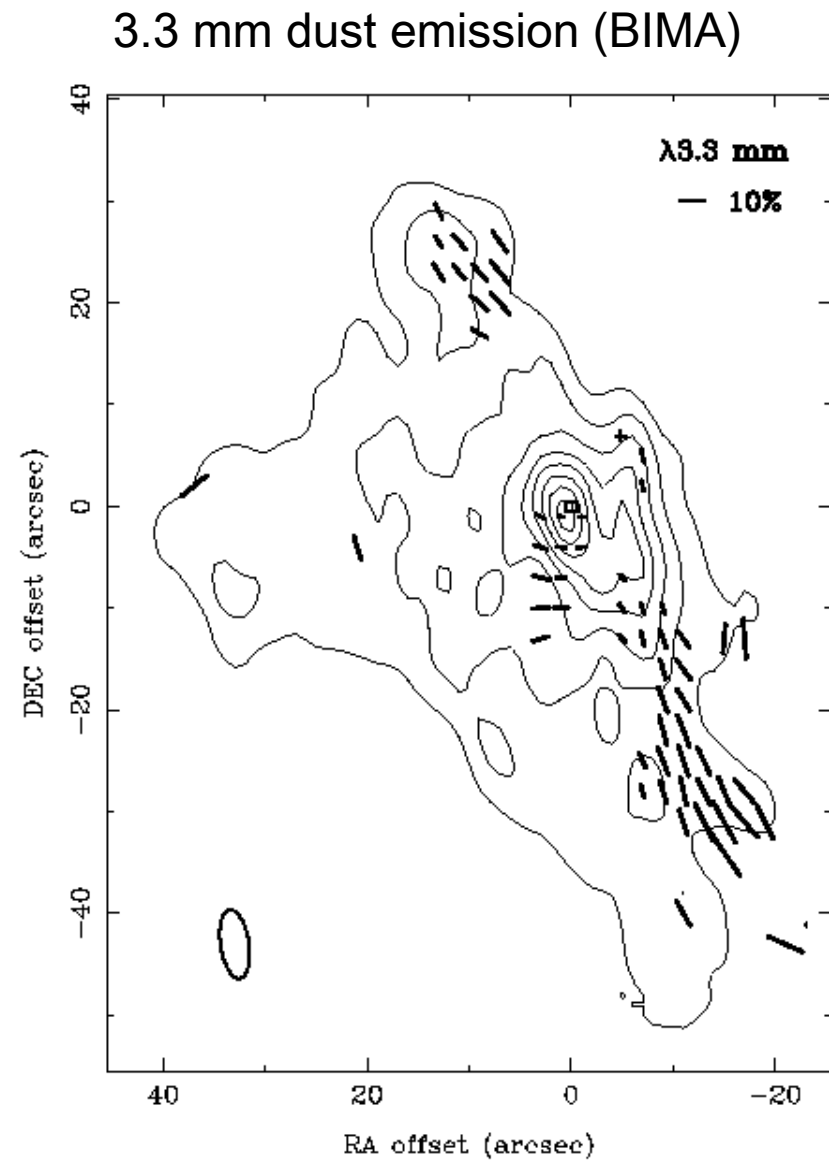
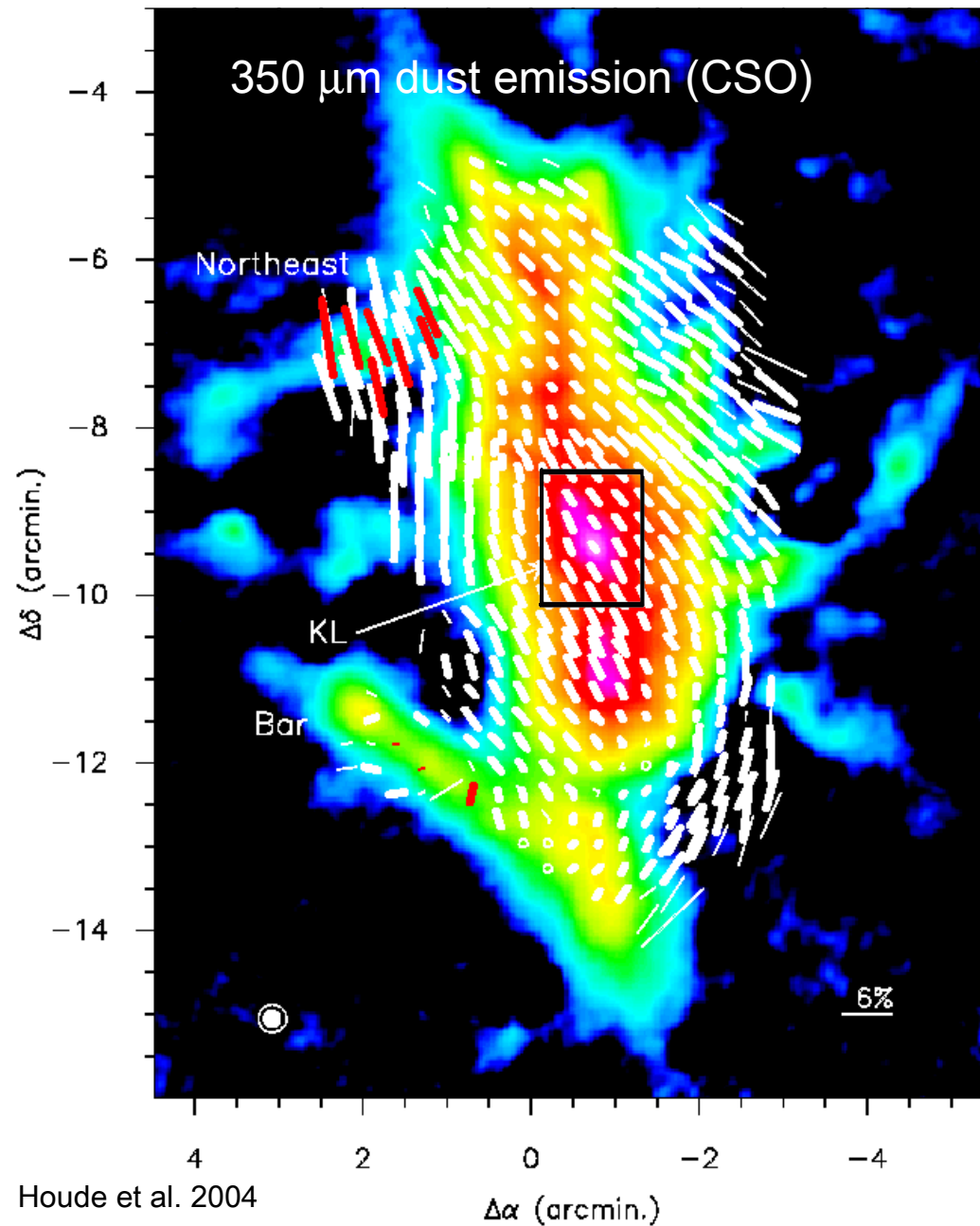


$$\delta V \approx \delta B / (4\pi\rho)^{1/2}, \quad \delta\phi \approx \delta B / B_{\text{pos}}$$

$$\therefore B_{\text{pos}} \approx 0.5(4\pi\rho)^{1/2} \delta V_{\text{los}} / \delta\phi$$

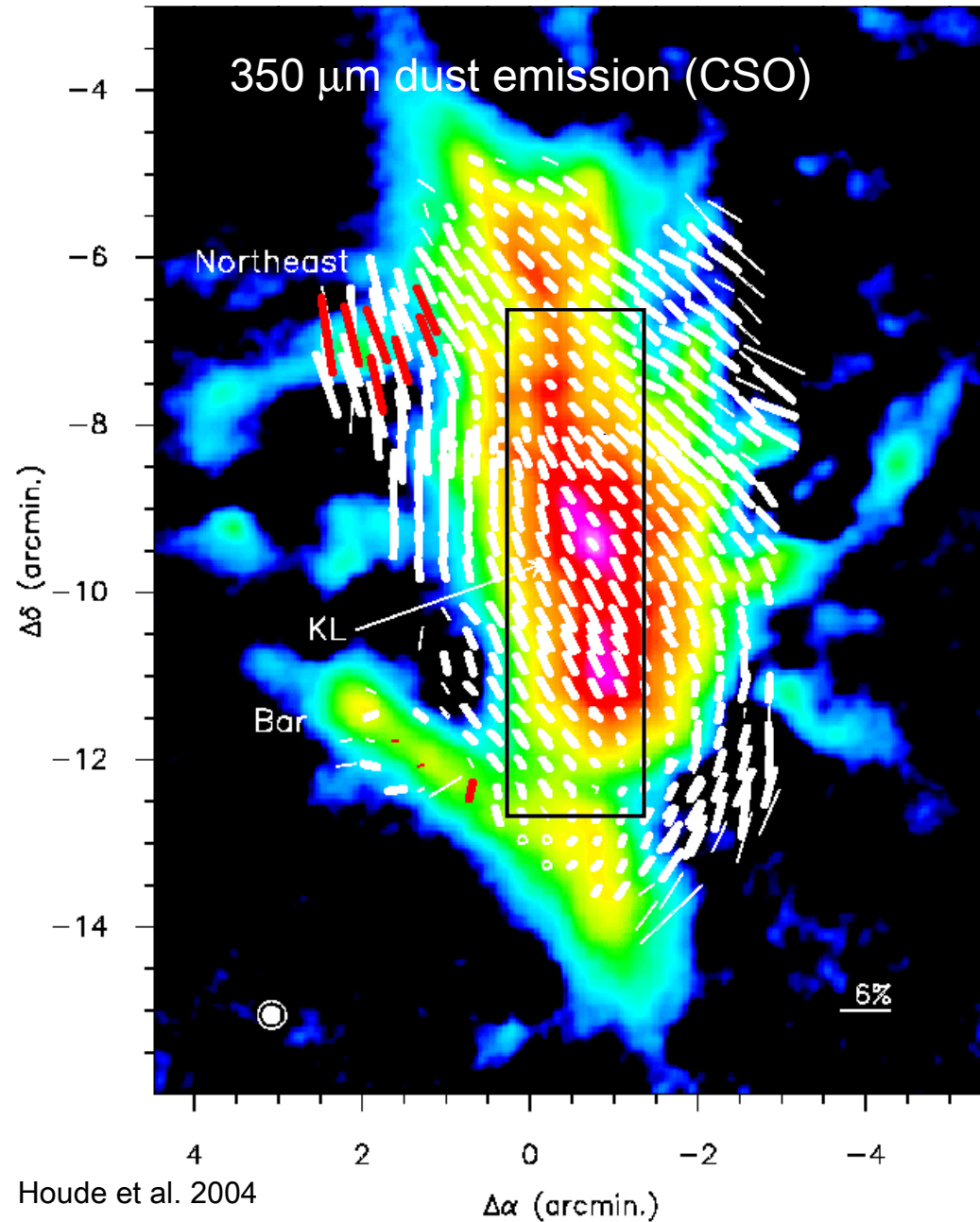


OMC1 (1)



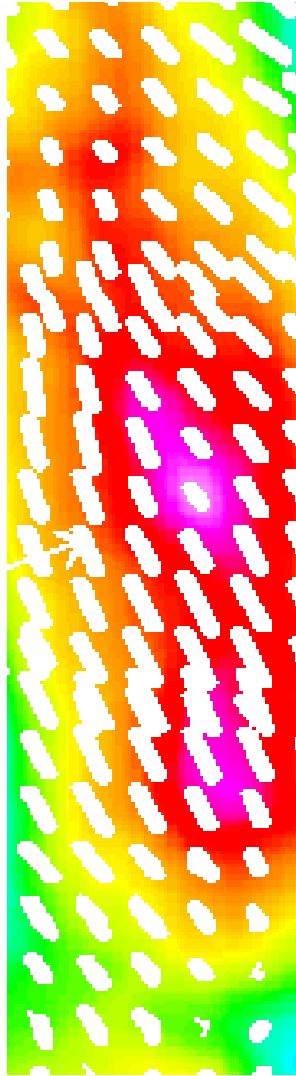
Rao et al. 1998

OMC1 (2)

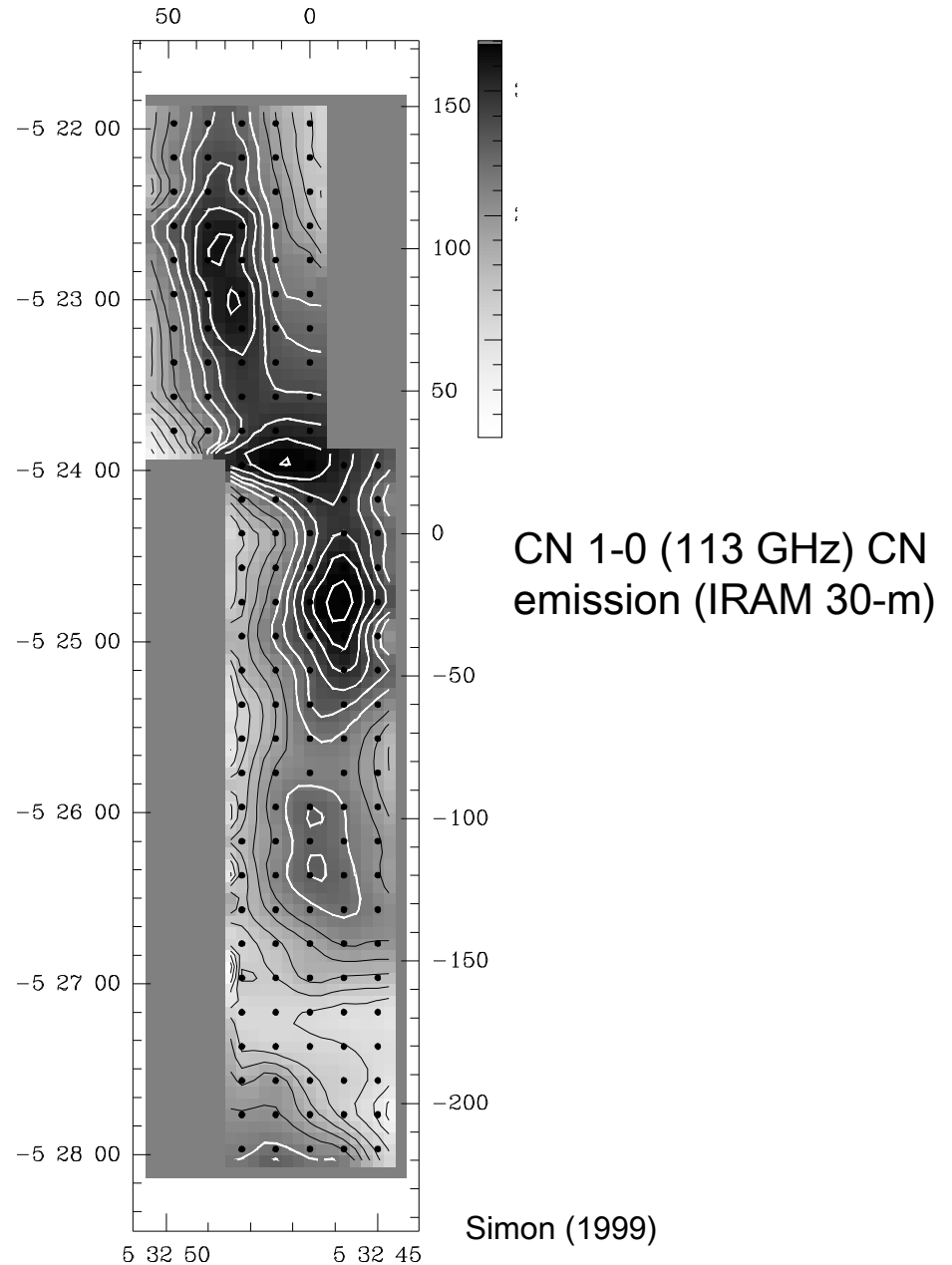


OMC1 (3)

350 μm dust
emission (CSO)



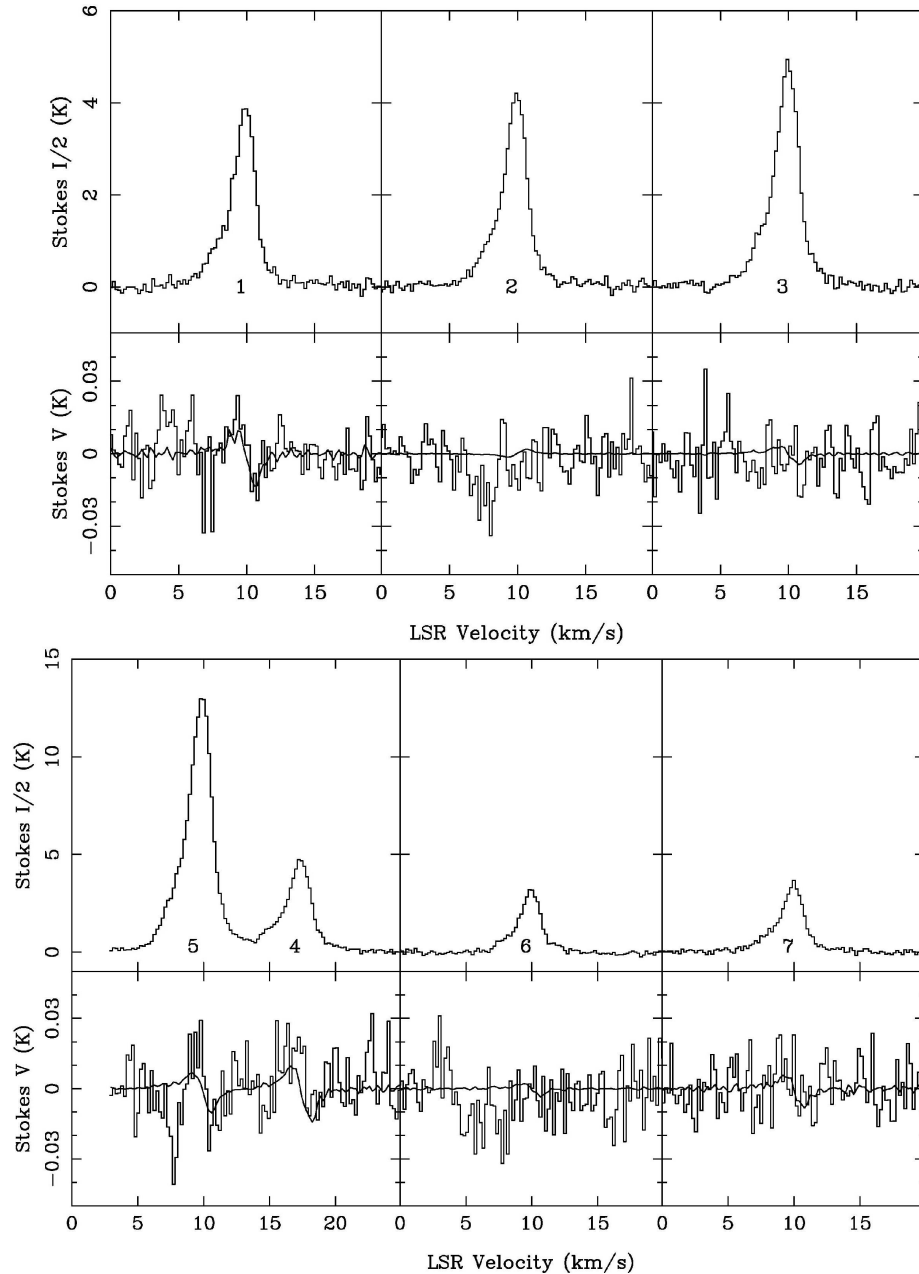
Houde et al. 2004



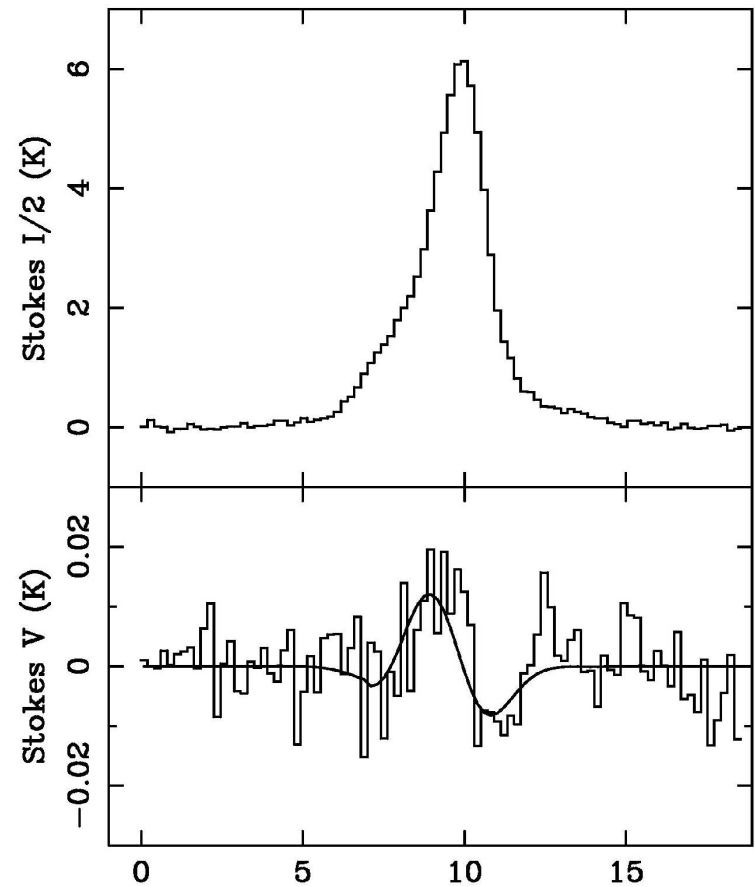
CN 1-0 (113 GHz) CN
emission (IRAM 30-m)

Simon (1999)

OMC1 (4)



CN 1-0 (113 GHz) CN
Zeeman (IRAM 30-m)

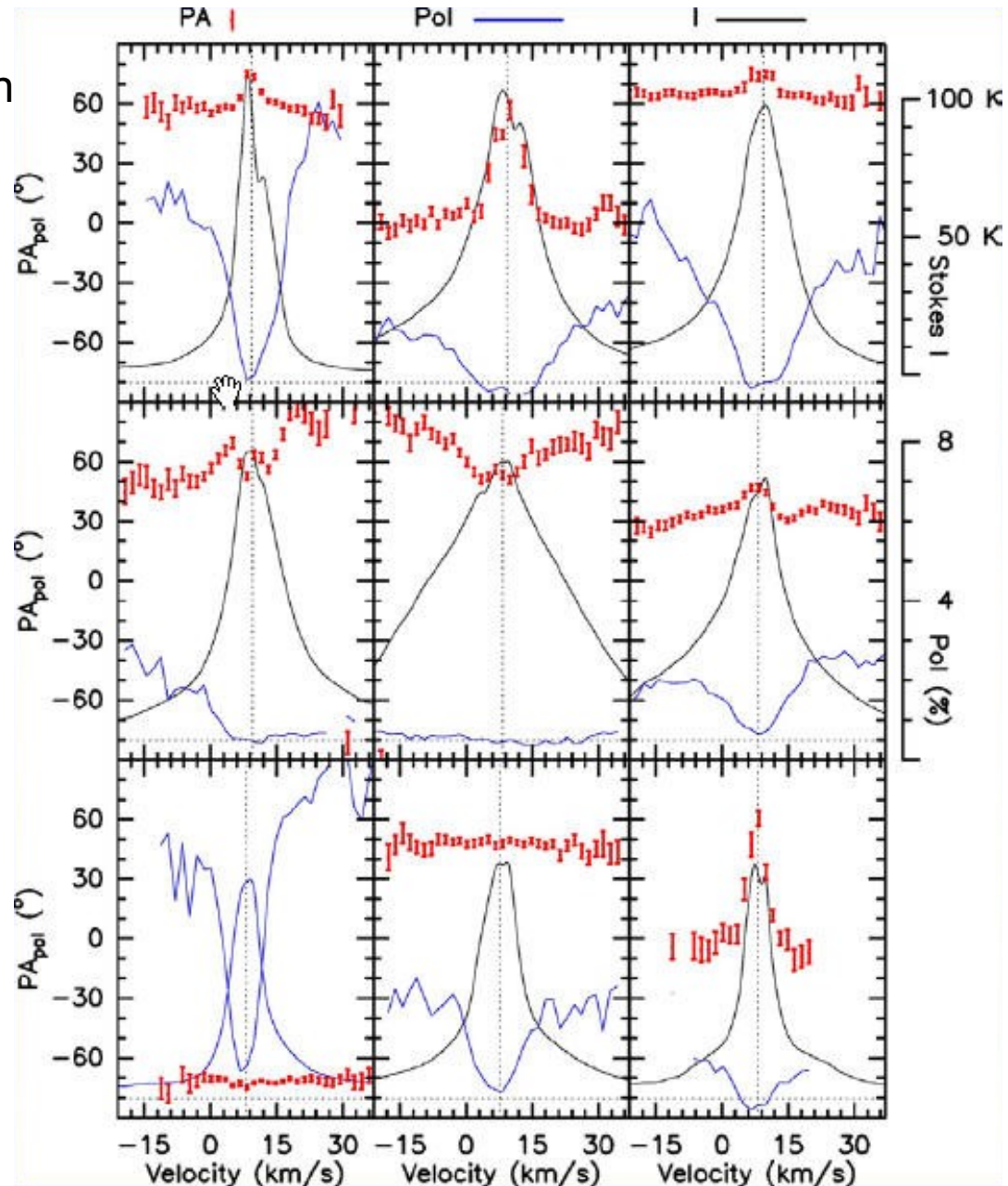


$$B_{\text{LOS}} = -0.36 \pm 0.08 \text{ mG}$$

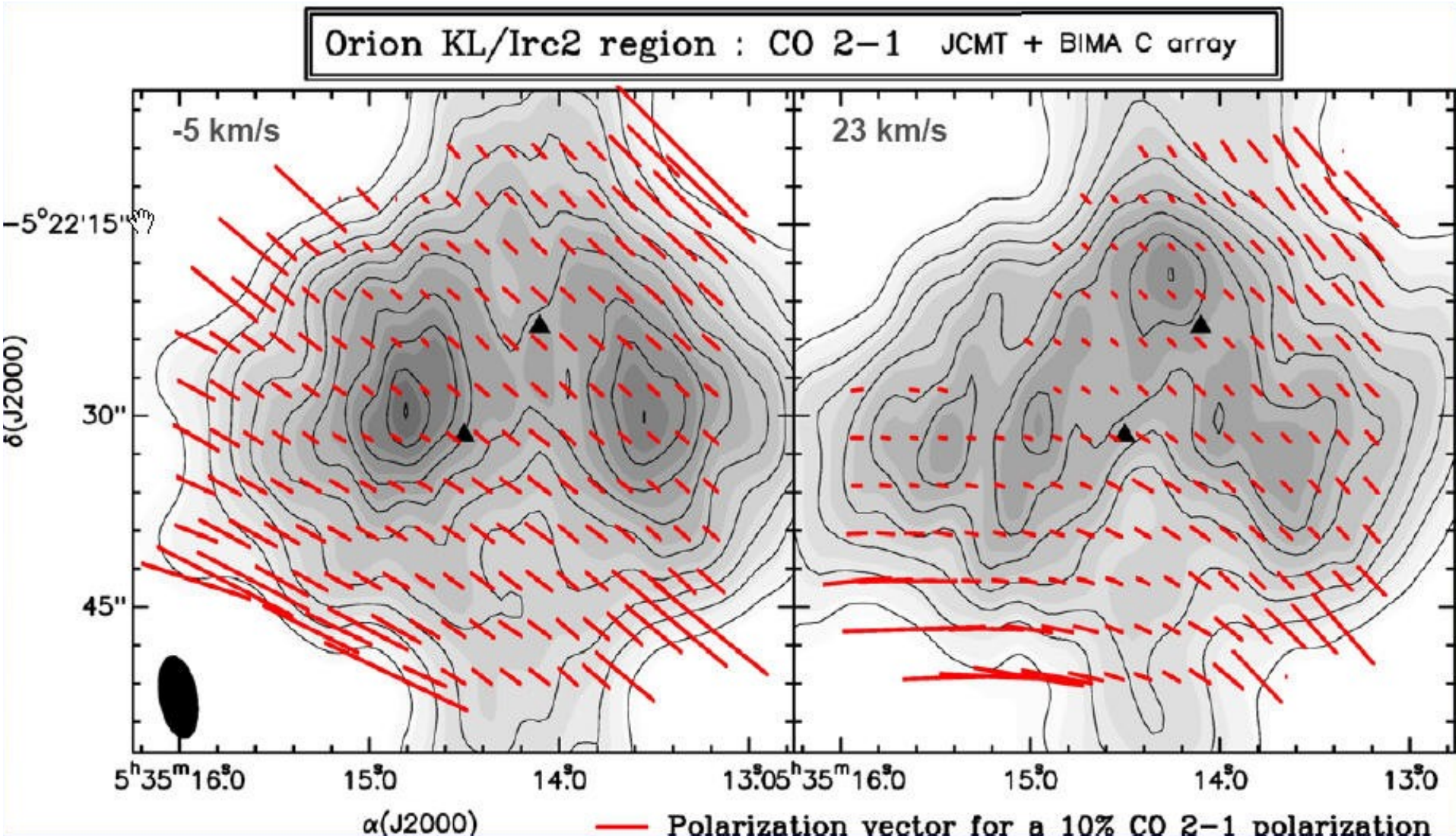
Crutcher et al. 1999

OMC1 (5)

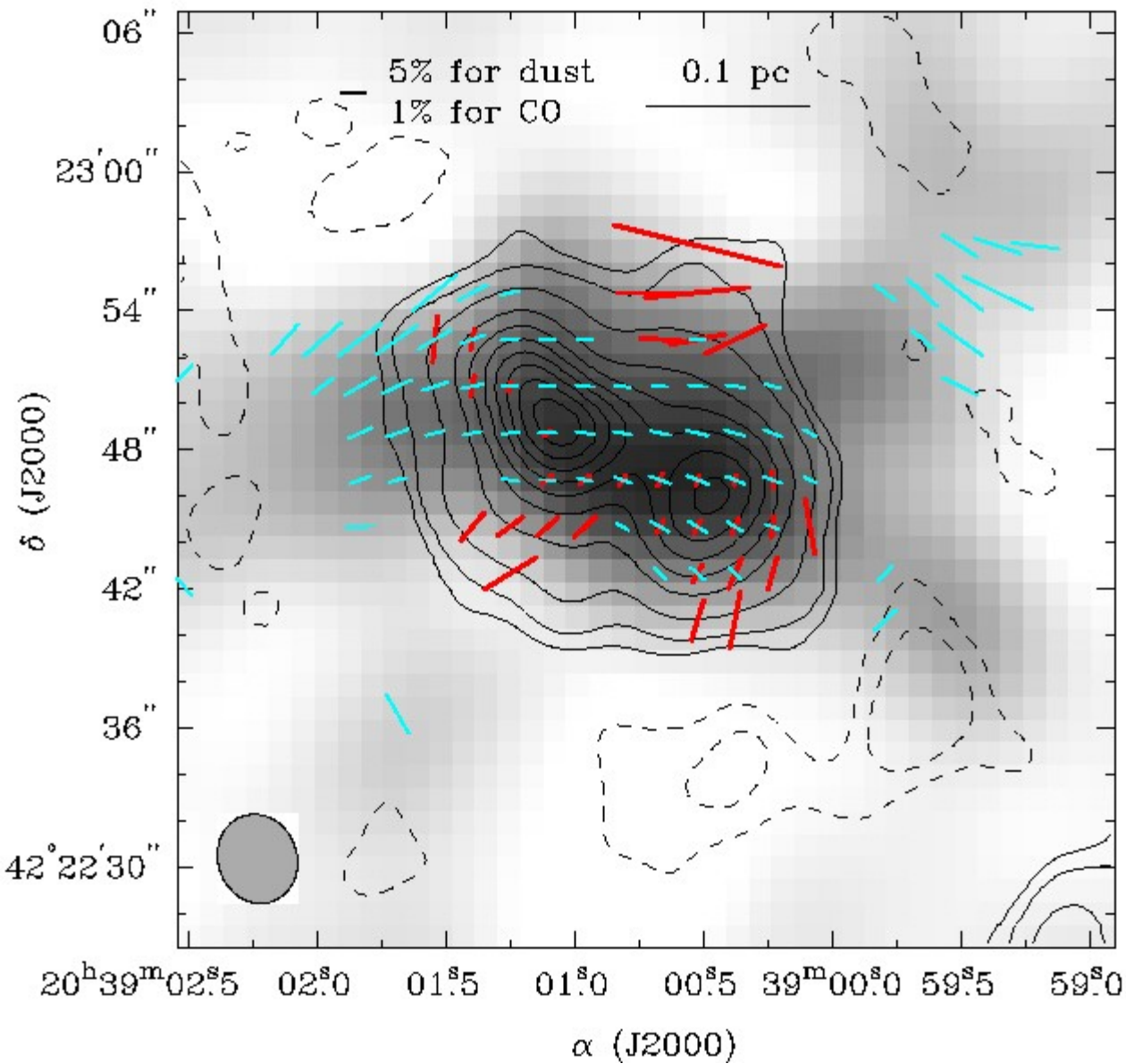
CO 2-1 linear polarization
(BIMA + JCMT)



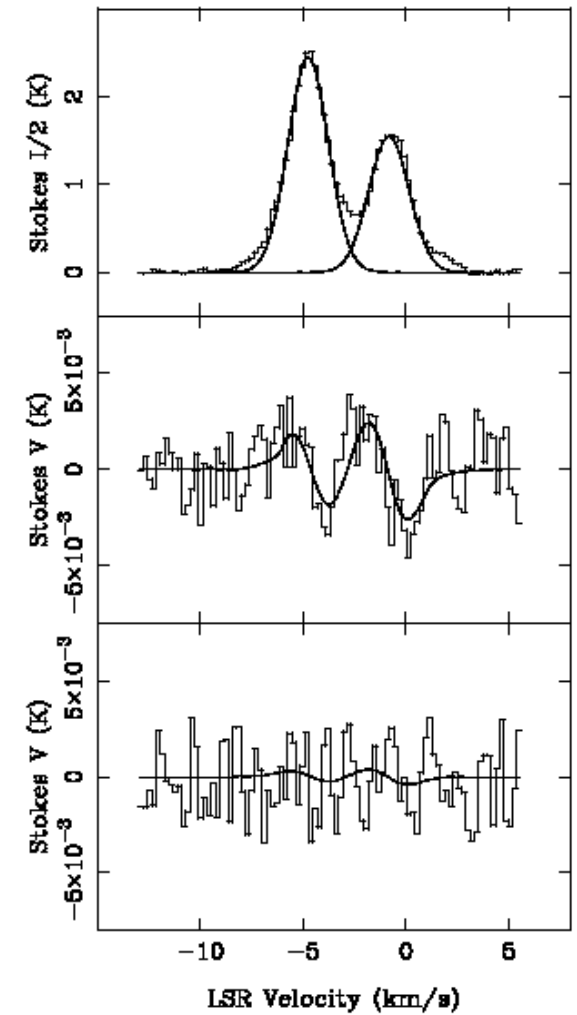
OMC1 (6)



DR21OH (1)



Lai et al. (2003)



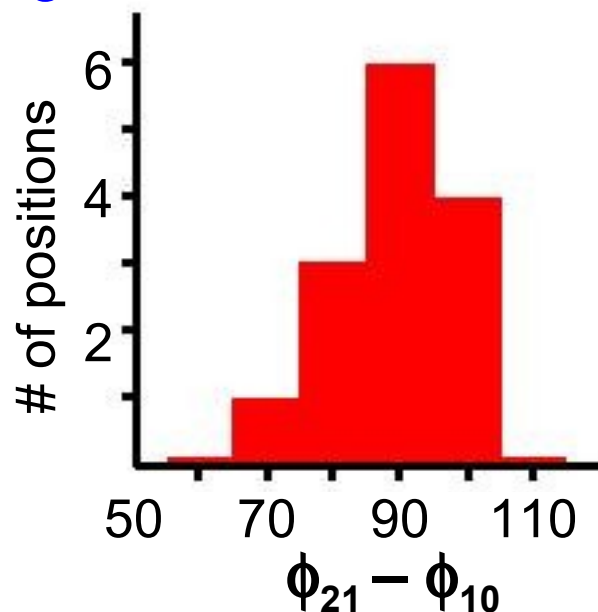
$B_{\text{los}} = 0.4, 0.7 \text{ mG}$

Crutcher et al. (1999)

DR21OH (2)

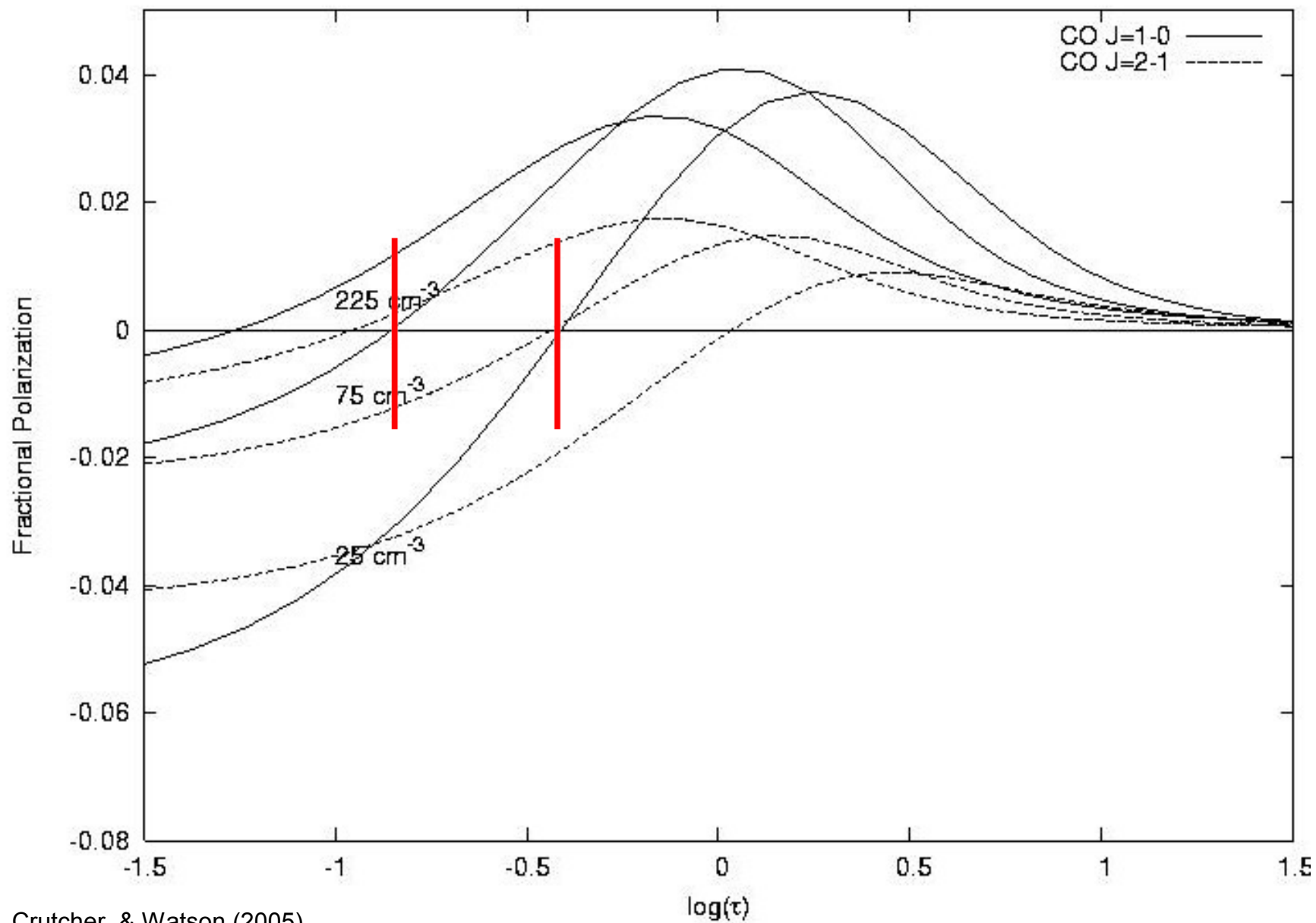
Linearly Polarized J=2-1 and J=1-0 Lines

- J=2-1 polarization is perpendicular to dust polarization and therefore parallel to the magnetic field
- J=1-0 polarization is orthogonal to J=2-1 polarization!



- requires two sources of anisotropic CO excitation
 - anisotropic velocity gradient (and τ), and photon trapping
 - IR from compact dust cores

DR21OH (3)



DR21OH (4)

1. CO polarization:

$$n(\text{H}_2) \sim 10^2, B_{\text{pos}} \approx 0.01 \text{ mG}$$

2. Dust polarization & CN Zeeman:

$$n(\text{H}_2) \sim 10^6, N(\text{H}_2) \approx 3 \times 10^{23}$$

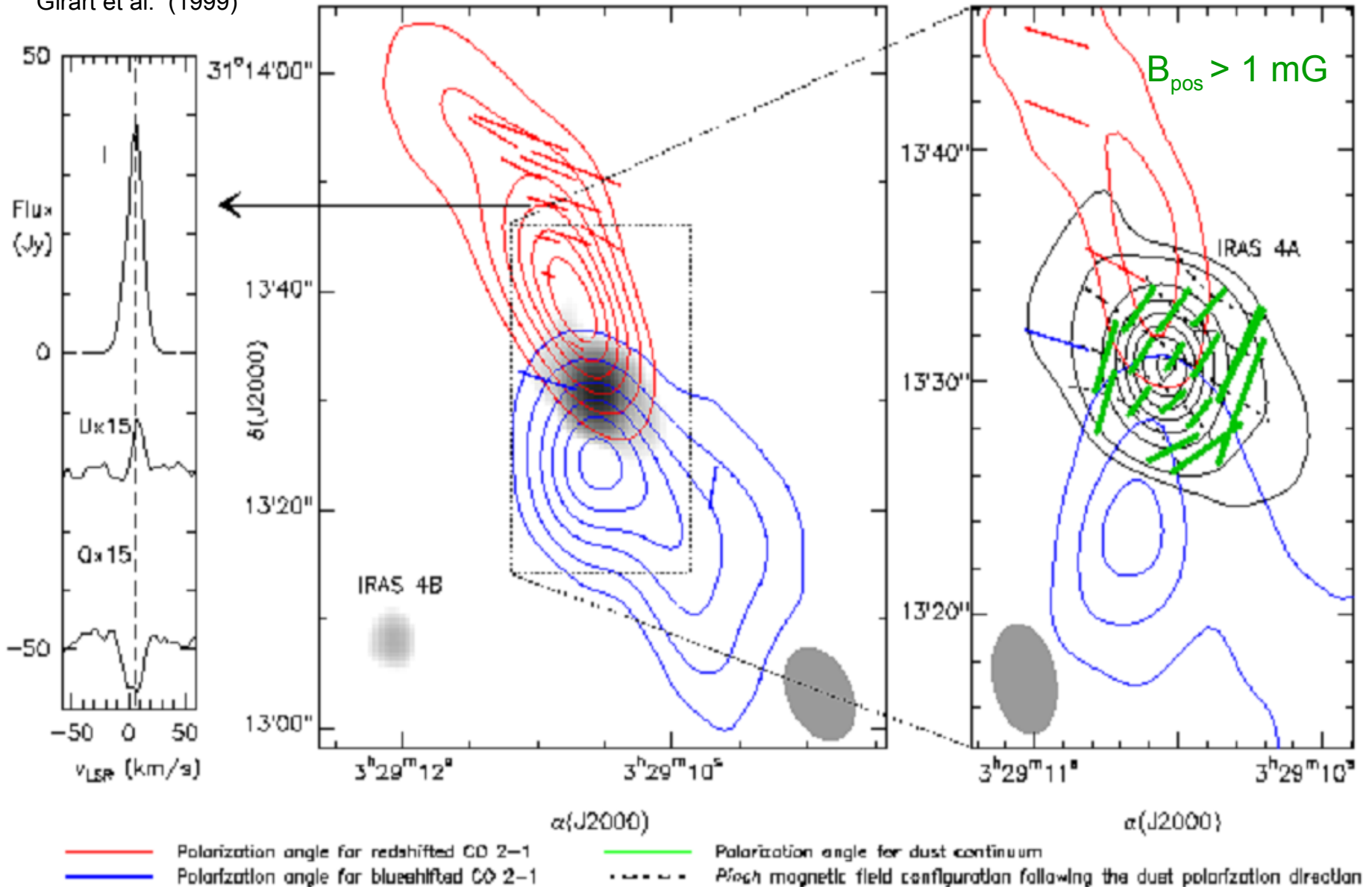
$$B_{\text{pos}} \approx B_{\text{los}} \approx 0.7 \text{ mG}, M/\Phi \approx 3.3$$

Combining 1 and 2, $B \propto \rho^{0.45}$

NGC1333 IRAS4 (1)

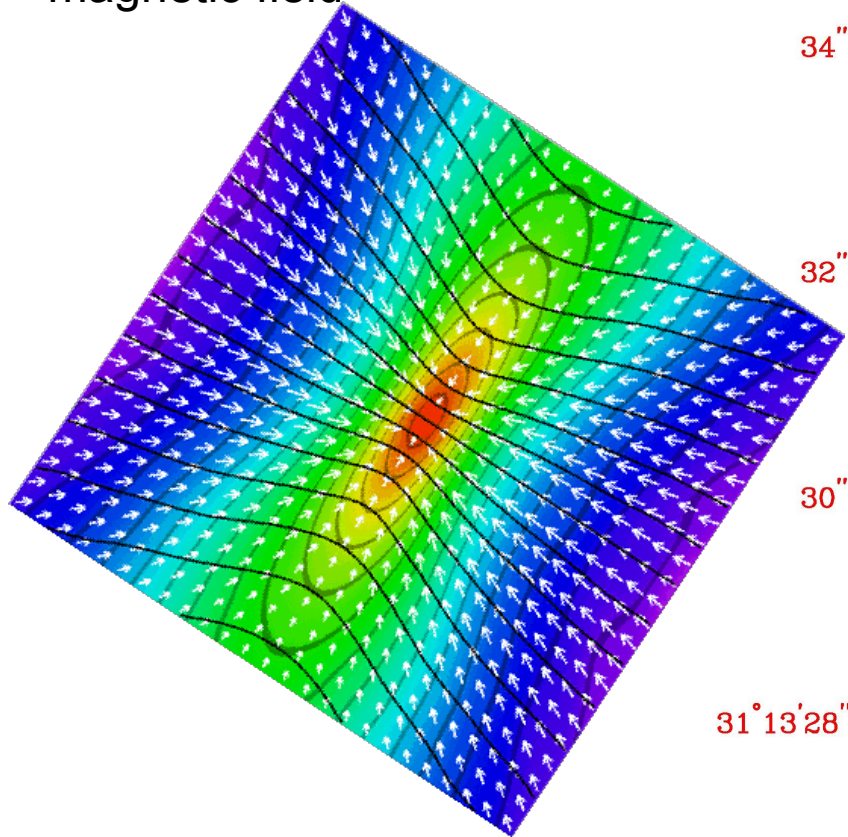
Dust emission (230 GHz) and CO 2-1 emission (BIMA)

Girart et al. (1999)



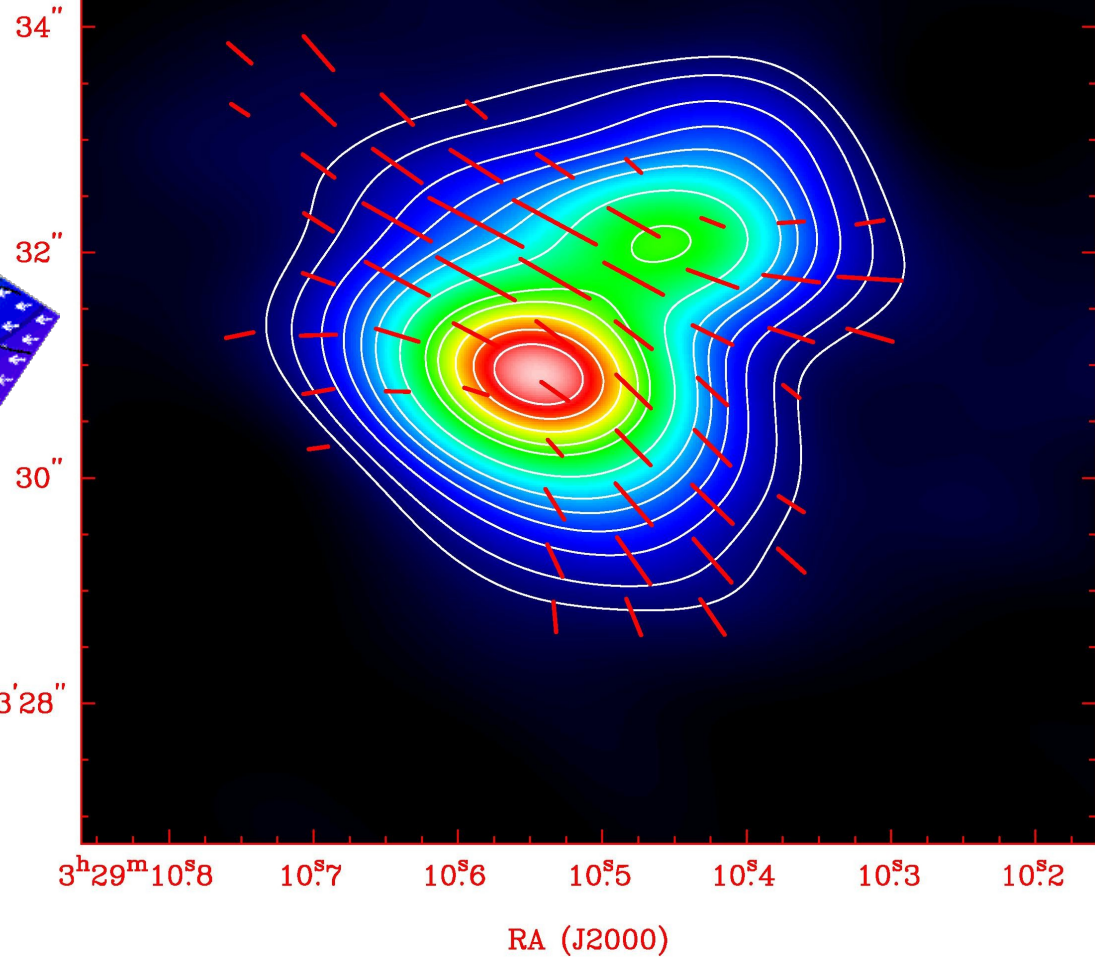
NGC1333 IRAS4 (2)

core formation simulation, strong
magnetic field



Fiedler and Mouschovias (1993)

850 μm dust emission (SMA)



Girart, Rao, and Marrone (2006)

ALMA Polarization Science

- Simultaneous CN (113 GHz) Zeeman, CO (115 GHz) linear polarization, & 3 mm dust emission polarization mapping
- Simultaneous CO (345 GHz) linear polarization and 0.85 mm dust polarization mapping
- Spectral-line linear polarization mapping of other lines (HCN, N_2H^+ , etc.) to probe field morphologies at higher densities than CO
- 3-D tomography of magnetic fields in star formation regions

