Calibration, imaging and mm peculiarities

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http://www.alma.inaf.it/index.php/Courses

Radio telescopes ERA sections 3.4, 3.5

Receivers ERA sections 3.6.2, 3.6.4, 3.6.5

Calibration

Imaging

mm peculiarities



Both ALMA and VLA antennas have a Cassegrain optical configuration. All (or most of the) receivers are in the Secondary focus

VLA subreflector





VLA secondary focus

ALMA antennas



VLA feed horns 1.4 GHz - 40GHz





ALMA cryostat front view <1 m in diameter 90 GHz – 900 GHz



ALMA 90 GHz cartridge



~50 cm

To measure all four Stokes parameter of an arbitrary polarized source it is necessary to combine the outputs of two ortogonally polarized feeds. Circular feeds (VLA) or linear feeds (ALMA). Usually after the feed horn there is a device (OMT or wire grid) separating the two polarizations.





Radiometers

The simplest total-power radiometer measures the time-averaged power of the input noise in a well defined radio frequency range

$$\left[\mathbf{v}_{RF} - \Delta \mathbf{v} - \mathbf{v}_{RF} + \Delta \mathbf{v}\right]$$





Superheterodyne Receiers

Nearly all practical receivers are superheterodyne. The RF amplifier is followed by a mixer that multiplies the RF signal by a sine wave of frequency v_{LO} generated by a local oscillator (LO)





Superheterodyne Receiers

The product of two sine waves

 $\frac{2\mathrm{sin}\left(2\pi\nu_{\mathrm{LO}}t\right)\mathrm{sin}\left(2\pi\nu_{\mathrm{RF}}t\right)}{-}$

$$\cos\left[2\pi(\nu_{\rm LO}-\nu_{\rm RF})t\right] - \cos\left[2\pi(\nu_{\rm LO}+\nu_{\rm RF})t\right]$$

Contains the sum and difference frequency components. **The mixer acts as a frequency shifter.**

- Shifts the signal to a lower frequency (called **Intermediate Frequency IF**) where it is easier to amplify, transmit, filter, digitize
- Improves tunability over a wide range of frequencies, by adjusting only the LO frequency
- The IF amplifier and back-end devices can all operate over a fixed frequency range



Superheterodyne Receiers



• Signals from within the bands centered at are converted to the IF band and admitted by the filter.

 $v_{LO} \pm v_0$

- These bands are known as lower and upper sidebands.
- If only a single sideband is wanted, the other can be removed by suitable filters. In some cases both sidebands are accepted, resulting in a double-sideband receiver (many of ALMA's receivers are DSB)

Spectrometers

A spectrometer divides the passband into N adiacent narrow frequency ranges, and simultaneously measures the power in all N channels.



Modern interferometers use large band receivers. Data are taken in multichannel mode regardless if they are meant for continuum or line observations.

The maximum number of channels in dual polarization mode is 8192 for the VLA 3840 for ALMA **Continuum images**

Multi-Frequency synthesis (MFS)

Wide bandwidths allow higher sensitivity to continuum emission

$$\sigma = \frac{2k}{\eta} \frac{T_{\text{sys}}}{\sqrt{\Delta t \Delta \nu} \sqrt{N_{\text{ant}}(N_{\text{ant}} - 1)}A}$$



MFS combines all channels

the result is a single image

Continuum images

***** Multi-Frequency synthesis (MFS)

Wide bandwidths allow higher sensitivity to continuum emission but also uv coverage is improved

$$\sigma = \frac{2k}{\eta} \frac{T_{\text{sys}}}{\sqrt{\Delta t \Delta \nu} \sqrt{N_{\text{ant}}(N_{\text{ant}} - 1)}A}$$

* Distance in the uv-plane is proportional to b/λ so observing a large range in wavelengths changes points in the uv-plane into lines.



Spectral line observations

- The imaging process

 is the same as for a continuum map
 but making an image for
 each channel (a cube with
 axes RA, DEC and velocity/frequency)
- * The rms is larger than for continuum
- While imaging it is possible to average channels if the full spectral resolution is not needed



Interferometric data



Spectral lines

1-D slice along velocity axis



From each pixel one spectrum

Interferometer correlators





Output?

Interferometer correlators





1 visibility

∀ baseline
 ∀ time unit
 ∀ Frequency channel
 ∀ Polarization product

Calibration

In the interferometer the signals from two antennas are cross-correlated each baseline measures one *visibility* (per int, per chan, per pol)



Fourier space/domain $V(u,v) = \int \int T(x,y)e^{2\pi i(ux+vy)}dxdy$ $T(x,y) = \int \int V(u,v)e^{-2\pi i(ux+vy)}dudv$ Image space/domain

(van Cittert-Zernike theorem)

T(x,y) source brightness = I

V(u,v) = FT T(x,y)

If no calibration is applied....



This would be the image of 1037-295 the calibrator of your dataset

deconvolving V^{ij}_{obs}

The actual source visibilities are corrupted while reaching the receiver by many factors

 $V^{ij}_{obs} = G^{ij} V^{ij}_{real}$

G = K B J D E P T F

F=ionosphere T=troposphere P=parallactic angle (alt-az mounting) E=antenna voltage pattern D=polarization leakages J= electronic gains B=bandpass response K=geometric compensation

$$V_{obs}^{ij}(v,t) = G^{ij}(v,t) V_{real}^{ij}(v,t)$$

The calibration is the process to determine the complex gains G^{ij}, with some assumptions

Most of the effects are antenna-based (pointing, focus, atmosphere, receiver noise, receiver bandpass)

$$V^{ij}_{obs} = G^i G^j V^{ij}_{real}$$

Temporal dependence and frequency dependence are only lightly coupled so their variations can be determined independently or at least iteratively

 $G^{i}(v,t) = B^{i}(v) J^{i}(t)$

We need to determine amplitude **a** and phase θ of the gains G, or **real** and **Imag** parts

$$A = \sqrt{(\Re^2 + \Im^2)} \qquad \theta = \arctan\left(\frac{\Im}{\Re}\right)$$

$$A_{obs}^{ij} e^{i\theta_{obs}^{ij}} = A_{real}^{ij} a^i a^j e^{i(\theta_{real}^{ij} + \theta^i + \theta^j)}$$

Phases for interferometers are **not absolute**. **Need to define a reference antenna, whose phase is arbitrarly fixed to 0.**

Typically choose an antenna at the center of the array.

To solve the equations we observe sources for which we know the real visibilities: calibrators

$$V^{ij}_{obs} = G^{ij} V^{ij}_{mode}$$

$$A_{obs}^{ij} e^{i\theta_{obs}^{ij}} = A_{model}^{ij} a^i a^j e^{i(\theta_{model}^{ij} + \theta^i + \theta^j)}$$

We choose bright sources when possible, we know ${{\bf A}^{{\rm ij}}}_{\rm model}$

We observe them at the phase center we know $\theta^{ij}_{_{model}}$

Bandpass calibration

$$G^{i}(v,t) = B^{i}(v)J^{i}(t)$$

- Calibrate for the response in frequency of each antenna ...basically, electronics
- Observations of a bright QSO (typically at the beginning of the observation)
- Amplitude constant within the band
- Observing time long enough to reach high S/N on each channel

Bandpass calibration

Observing at the phase center a source with known model

$$A_{mod}(v) = 1$$
 and $\theta_{mod} = \dots$



$$A_{obs}^{ij} = B^{i} B^{j} A_{mod}^{ij}$$







amplitude

Bandpass calibration

Observing at the phase center a source with known model





$$\theta^{ij}_{obs} = \theta^i + \theta^j + \theta^{ij}_{mod}$$







phase

Gain calibration

$$G^{i}(v,t) = B^{i}(v)J^{i}(t)$$

- Calibrate for the long time scale dependent response of each antenna
 - ...basically, atmosphere
- Observations of a point like source (QSO)
- As close as possible to the target (< 4 deg)</p>

Gain calibration



Observed regularly before and after target scans



Gain calibration

$$G^{i}(v,t) = B^{i}(v) J^{i}(t)$$

- Observed regularly before and after target scans
- Coherence time
- Solutions applied to the target using a linear interpolation



Amplitude calibration

- Define the Jy/K scale basically antenna efficiency
- Observations of a non variable object
 (typically at the beginning of the observation) *
- No matter where in the sky



The scale is calculated for the flux calibrator and transferred to bandpass and phase calibrator

After calibration

deconvolving V^{ij}_{cal}



Imaging
In the next two weeks we are going to deal with

visibilities and uv plane

To get familiar with them you can play with

🖈 a java applet online:

http://www.narrabri.atnf.csiro.au/astronomy/vri.html

or a python script written by Ivan Marti-Vidal (nordic ARC node) APSYNSIM

https://launchpad.net/apsynsim

1 D



Dirac function

FT?

Fourier Transform



1 D

2 D



1 D

2 D



Snapshot observation with two antennas 1 baseline





← uv-coverage





8 hrs observation with two antennas 1 baseline (~2 km)





← uv-coverage





8 hrs observation with two antennas 1 baseline (~800 m)





← uv-coverage

Resulting image

8 hrs observation with two antennas 1 baseline (~800 m)





← uv-coverage





Snapshot observation with 36 antennas 1260 baselines





← uv-coverage

Resulting image



Aperture synthesis

Long observations make the Dirty beam better approximate a gaussian

Slides from IRAM school



J. Pety lecture at 8th IRAM Millimeter Interferometry School











Dirty Beam Shape and Super Synthesis





J. Pety lecture at 8th IRAM Millimeter Interferometry School



Dirty Beam Shape and Super Synthesis









We need to get $T(x,y) = \int \int V(u,v)e^{-2\pi i(ux+vy)}dudv$

Consider a two point-like sources as target to observe

I (x, y)





V(u, v)

We need to get $T(x,y) = \int \int V(u,v)e^{-2\pi i(ux+vy)}dudv$

But

we actually sample the Fourier domain at discrete points





where S(u,v) is the sampling function S= 1 at points where visibilities are measured and S = 0 elsewhere

 \boldsymbol{V}_{true} is the 2 point-like sources ideal Fourier transform (example from APSYNSIM)

We need to get $T(x,y) = \int \int V(u,v) e^{-2\pi i (ux+vy)} du dv$

Applying the convolution theorem:



The Fourier transform FT of the sampled visibilities gives the true sky brightness convolved with the Fourier transform of the sampling function (called **dirty beam**).

$$I^{D}(x, y) = B_{dirty}(x, y) \otimes I(x, y)$$

To get a useful image from interferometric data we need to Fourier transform sampled visibilities, and **deconvolve for the dirty beam** \rightarrow **clean**

Imperfect reconstruction of the sky

Incomplete sampling of uv plane → sidelobes

 $B_{dirty}(x, y)$



- Central maximum has width 1/(u_{max}) in x and 1/(v_{max}) in y
- Has ripples (sidelobes) due to gaps in uv coverage



deconvolution \rightarrow sidelobes removal

We need to get $T(x,y) = \int \int V(u,v)e^{-2\pi i(ux+vy)}dudv$

Need to choose:

Image pixel size (cellsize)

Make the cell size small enough for Nyquist sample of the longest baseline $(\Delta x < 1 / 2 \ u_{max}; \Delta y < 1 / 2 \ v_{max})$ Usually 1/4 or 1/5 of the synthesized beam to easy deconvolution

Image size (imsize)

The natural resolution in the uv plane samples the primary beam **At least twice the field of view for the Nyquist sampling** Larger if there are bright sources in the sidelobes of the primary beam (they would be aliased in the image)

Basic assumption: each source is a collection of point sources

1) Initializes the residual map to the dirty map and the Clean component list to an empty value



Basic assumption: each source is a collection of point sources

2) Identifies the pixel with the peak of intensity (I_{max}) in the residual map and adds to the clean component list a fraction of $I_{max} = \gamma I_{max}$



Basic assumption: each source is a collection of point sources

3) Subtracts over the whole map a dirty beam pattern, including the full sidelobes, centered on the position of the peaks saved in the clean component list, and normalized to the γI_{max} at the beam center.



Basic assumption: each source is a collection of point sources

4) Iterates until stopping creteria are reached



Stopping criteria

|I_{max}| < multiple of the rms
(when rms limited)</pre>

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Stopping criteria

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Deconvolution - Classic CLEAN Hogborn 1974, Clark 1980, Cotton-Schwab 1984

Basic assumption: each source is a collection of point sources

 5) Multiples the clean components by the clean beam an elliptical gaussian fitting the central region of the dirty beam
→ restoring



Deconvolution - Classic CLEAN Hogbom 1974, Clark 1980, Cotton-Schwab 1984

Basic assumption: each source is a collection of point sources

5) Multiplies the clean components by the clean beam (**restore**) and add it back to the residual



Resulting image pixel have units of Jy per clean beam

But

Interferometer elements are sensible to direction of arrival of the radiation Primary beam effect $\rightarrow T(x,y) = A(x,y) T'(x,y)$



The response of the antennas in the array must be corrected for during imaging to get accurate intensities for source outside the core of the beam.

But

Primary beam effect $\rightarrow T(x,y) = A(x,y) T'(x,y)$

T(x,y)



T'(x,y)

rms 8e-4

rms 3e-3

But measured visibilities actually contain noise and some uv ranges are sampled more than others $\sigma(u, v) \propto \frac{1}{\sqrt{T_{sys1}T_{sys2}}}$

• Gridded visibilities are $\rightarrow V(u,v) = W(u,v) V'(u,v)$



* Natural weighting $W(u,v) = 1/\sigma^2(u,v)$

 σ is the noise variance of the visibilities

* Uniform weighting $W(u,v) = 1/\delta_s(u,v)$

 $\delta_{\underline{v}}$ is the density of (u,v) points in a symmetric region of the uv plane

Unfortunately, in reality, the weighting which produces the best resolution **(uniform)** will often utilize the data very irregularly resulting in poor sensitivity \rightarrow compromises

***Briggs weighting**

combines inverse density and noise weighting. An adjustable parameter "robust " allows for continuous variation between natural (robust=+2) to uniform (robust=-2)

***** Weighting effects on the Dirty beam

Natural 0.29" x 0.23" Best sensitivity **Uniform** 0.24"x0.17" Best angular resolution





***** Weighting effects on the image

Natural res = 0.29" x 0.23" rms = 0.8 mJy/beam Uniform res = 0.24"x0.17" rms = 3 mJy/beam



If the region of interest is larger than the primary beam



If the region of interest is larger than the primary beam

need to mosaic many interferometric pointings



Clean is basically the same → need to specify the central pointing (phasecenter) the image size = full mosaic area and the mode 'mosaic' (imagermode and ftmachine)

With increasing frequency:

★ No external human interferences in the data

★ No ionospheric effect



- ★ Tropospheric effects: absorption and delay of signal
 - stronger weather dependency
 - T_{sys} dominated by atmospheric noise
- ☆ Time variability of quasars increases



which flux calibrators?





The role of the troposphere

- H₂O (mostly vapor)
- "Hydrosols" (water droplets in clouds and fog)
- "Dry" constituents: O₂, O₃, CO₂, Ne, He, Ar, Kr, CH₄, N₂, H₂

clouds & convection = time variation

Column density as function of altitude







Tropospheric opacity depends on altitude





Tropospheric opacity depends on altitude



Difference due to the scale height of water vapor

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 $T_{sys} \sim T_{atm} (1 - e^{\tau}) + T_{rx}$

e.g. to observe a 1 Jy source with a 10 m radiotelescope we have to measure $T_{A} \sim 0.04$ K against $T_{SVS} \sim 100$ K

At lower frequencies T_{rx} is dominant



At higher frequencies (mm/submm) the noise associated with the atmosphere T_{atm} is dominant, and acts like a blackbody emitter, attenuating the astronomical signal



System noise temperature

ALMA front end are equipped with an Amplitude Calibration Device (ACD)



To measure T_{sys} and T_{rx} stored in tables

Every scan could have a Tsys measurement, but <400 GHz relatively constant ~10min. Tsys spectra are applied off-line to the correlated data.

Assuming correlated data in units of % correlation multiplication by Tsys will change the unit to Kelvin



Before



Tsys calibration

Spectral Tsys band 3 (~100 GHz)



Before



Tsys calibration



Spectral Tsys band 3 (~100 GHz)

After





Mean effect of atmosphere on Phase

Variations in precipitable water vapor (PWV) cause phase fluctuations, worse at higher frequencies, resulting in:

- Phase shift due to refractive index $n \neq 1$
- Low coherence (loss of sensitivity)

Patches of air with different pwv (and hence index of refraction) affect the incoming wave front differently.

Antenna 1, 2, 3 see slightly different disturbances

Sky above antenna 4 varies independently

The phase change experienced by an e.m. wave can be related to pwv

$$\varphi_e \approx \frac{12.6\,\pi}{\lambda} \cdot pwv$$



Hogg, Guiraud, & Decker, 1981



Atmospheric phase fluctuations



Phase noise theory $\varphi_{rms} = \frac{K b^{\alpha}}{\lambda}$

b=baseline length (km) $\alpha = 1/3$ to 5/6 (thin or thick atmosphere) $\lambda =$ wavelength (mm) K constant (~100 for ALMA)

Kolmogorov turbulence

The break is typically @ baseline lengths few hundred meters to few km (scale of the turbulent layers)

Break and maximum are weather and wavelength dependent



Atmospheric phase fluctuations \rightarrow decorrelation

We lose integrated flux because visibility vectors partly cancel out

$$\langle V \rangle = V_o \langle e^{i\varphi} \rangle = V_o e^{-(\varphi_{rms}^2)/2}$$

$$\phi_{rms}$$
= 1 radian \rightarrow = 0.60 V_c

In summary

Fluctuations in the line-of-sight pwv of an antenna cause phase variations of the order of ~30 deg / sec at 90 GHz, and scales linearly with frequency....

$$\varphi_e \approx \frac{12.6\,\pi}{\lambda} \cdot pwv$$

and the phase noise is worse at longer baselines...

$$\varphi_{rms} = \frac{K b^{\alpha}}{\lambda}$$

WVR correction

Each ALMA 12 m antenna has a water **vapour radiometer**





WVR correction

Each ALMA 12 m antenna has a water **vapour radiometer**

Four "channels" flanking the peak of the 183 GHz water line

Data taken every second





WVR correction

Each ALMA 12 m antenna has a water vapour radiometer

Four "channels" flanking the peak of the 183 GHz water line

Data taken every second

Convert 183 GHZ brightness to PWV (wvrgcal): model PWV, temperature and pressure compare to the observed "spectrum" compute the correction:





WVR correction

Band 6 (230 GHz)



Raw phases & WVR corrected phases



WVR correction



Band 6 (230 GHz)

Raw phases & WVR corrected phases

Calibration in ALMA:

Tsys and wvr calibration are done "a priori" without observations of dedicated calibrators bservations.





- all are resolved on long baselines
- brightness varies with distance from Sun and Earth
- line emission present \rightarrow need models

Other possibilities: asteroids, red giant stars...

NOW: Monitoring of point-like quasars!!!

