

Molecular clouds and star formation

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Overview of this lecture:

The galactic interstellar medium (ISM):

constituents and their co-existence; large-scale distribution

Molecular clouds

properties; chemistry; mass and temperature

Kinematics

rotation curve, kinematic distances

Star formation

young stellar objects (YSOs); IMF

manifestations (interaction with surroundings)

Star formation: high-mass

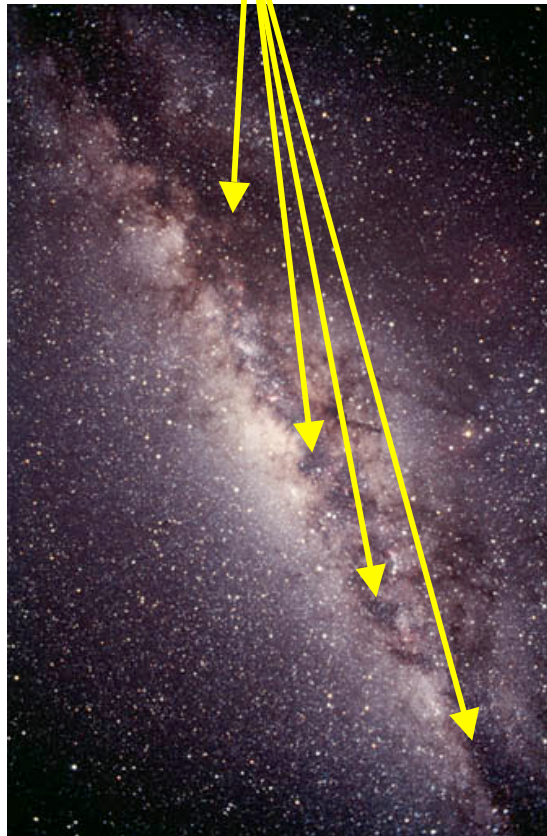
intro only. Is main topic of next lecture, by Cesaroni

THE PHASES OF THE INTERSTELLAR MEDIUM

Not just stars...

ISM: 90% H, 9% He, 1% “rest”

Dust mixed with gas



Abundances: for every 10^6 H atoms, there are 250 C, 500 O, 80 N atoms \sim solar (\equiv cosmic). Other elements: IS abundance \ll cosmic: **depletion** (material locked up in dust grains)

Characterize ISM acc. to condition of H:

HI: $M \sim 2 \times 10^9 M_{\odot}$

H₂: $M \sim M(\text{HI})$

HII: $M \sim 1 \times 10^8 M_{\odot}$

$M(\text{ISM}) \sim 4\% M(\text{visible matter in Galaxy})$

$M(\text{dust}) \sim 1\text{-}2\% M(\text{ISM})$

Energy in the ISM:

Radiation field, magnetic fields, cosmic rays

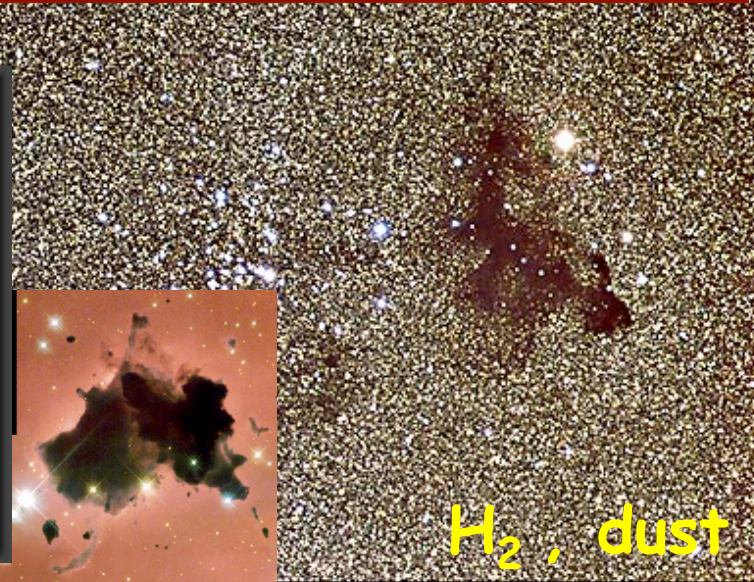
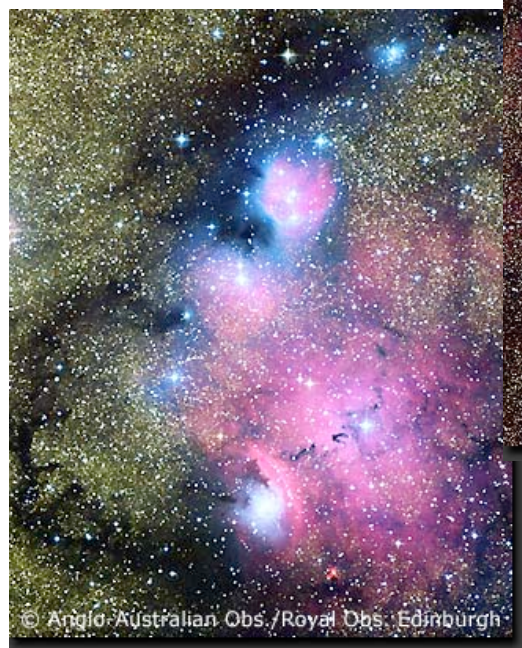
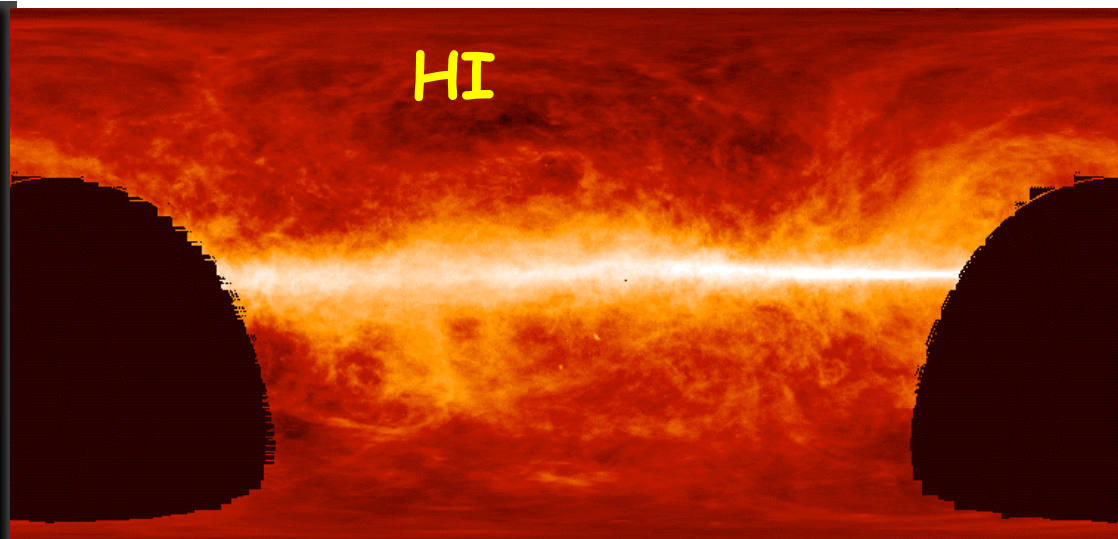
High density? Not really... (only in some locations):

High-density molecular cloud core: $\geq 10^6$ particles cm^{-3}

Earth's atmosphere at sea level: $\sim 3 \times 10^{19}$ particles cm^{-3}

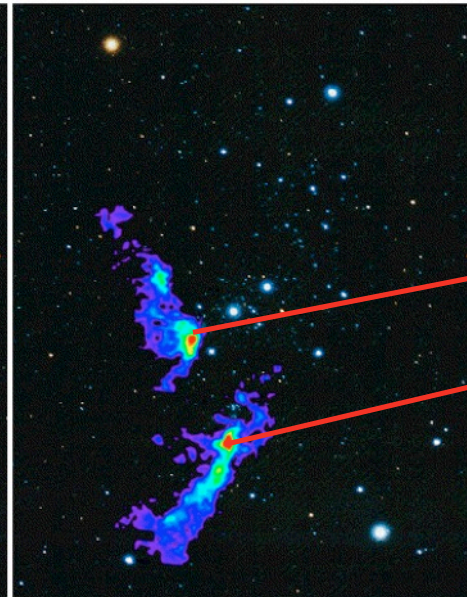
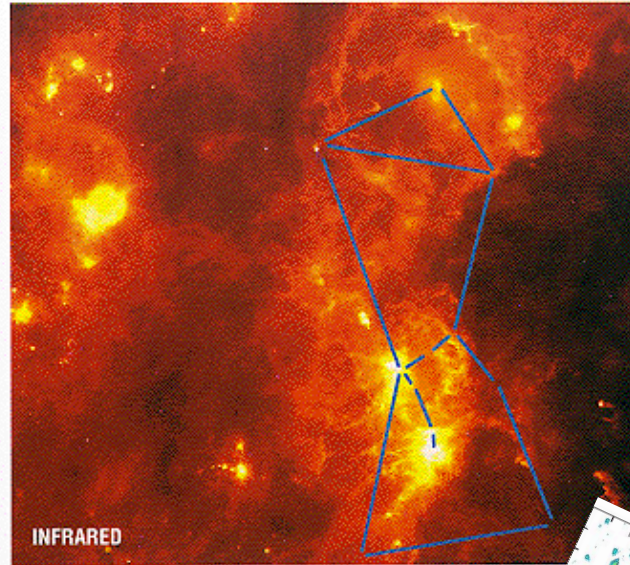
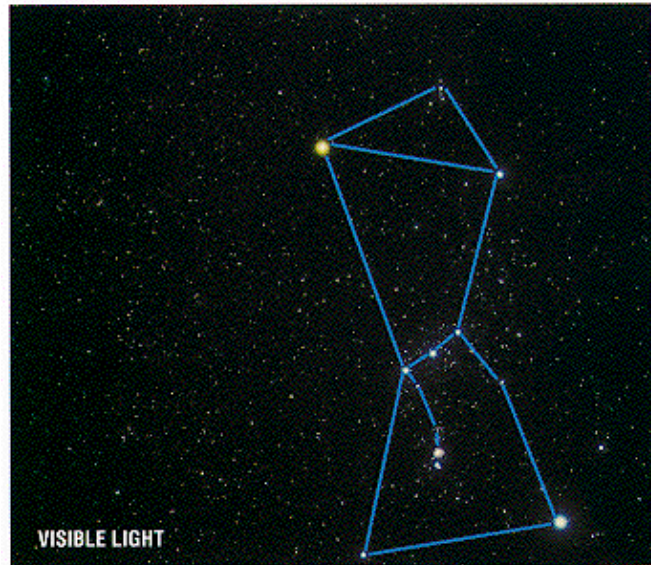
Best terrestrial vacuum: $3 \times 10^{12-13}$ particles cm^{-3} !!

Average density ISM: ~ 1 particle cm^{-3}

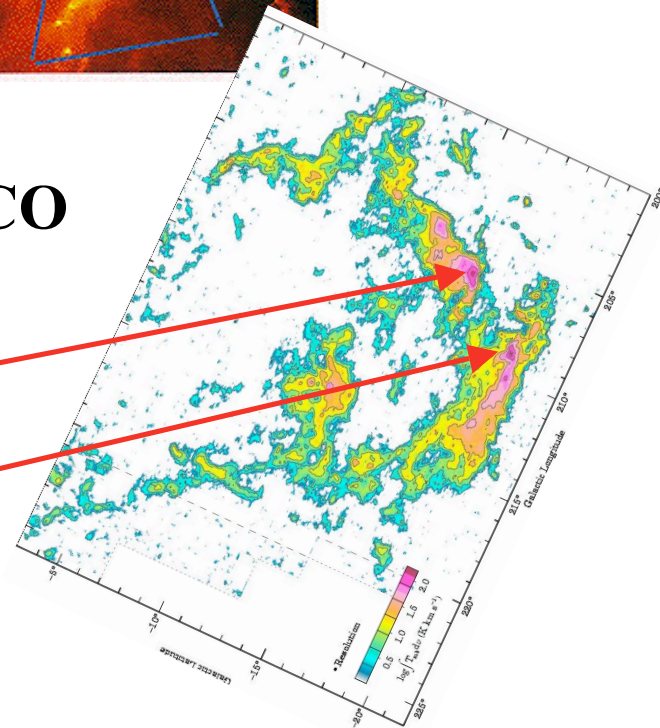


What you see depends on frequency

Orion: optical, IR, and mm



CO

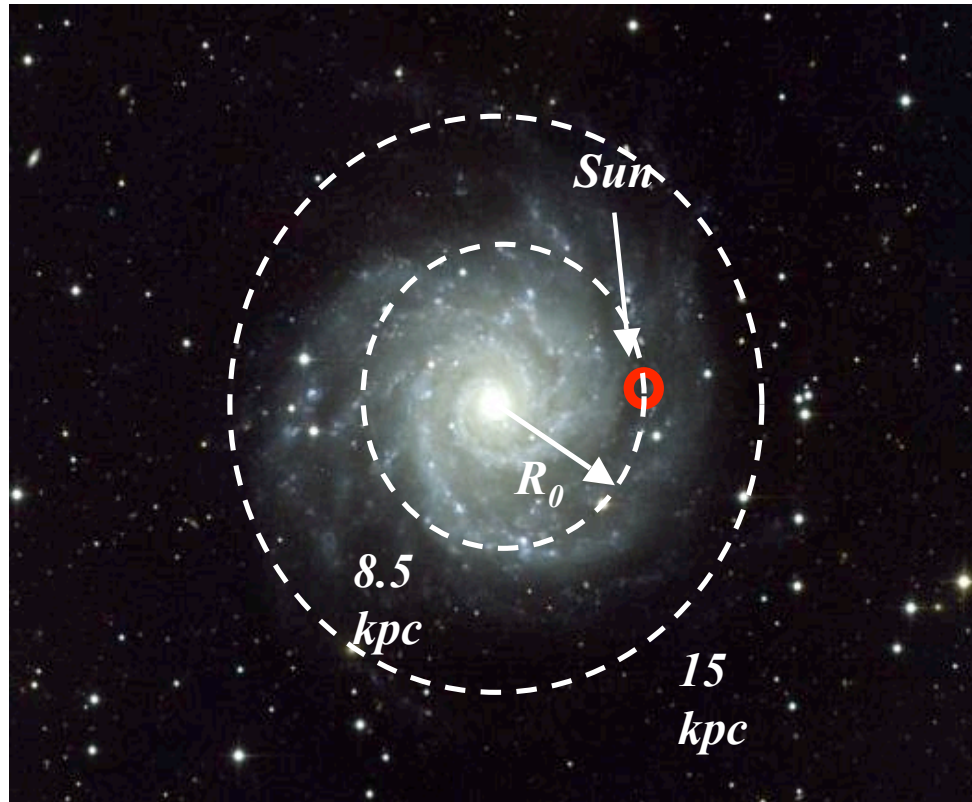


HH46 – Visual → NIR → MIR

The Spitzer-view



Inner, outer, & (far-) outer Galaxy



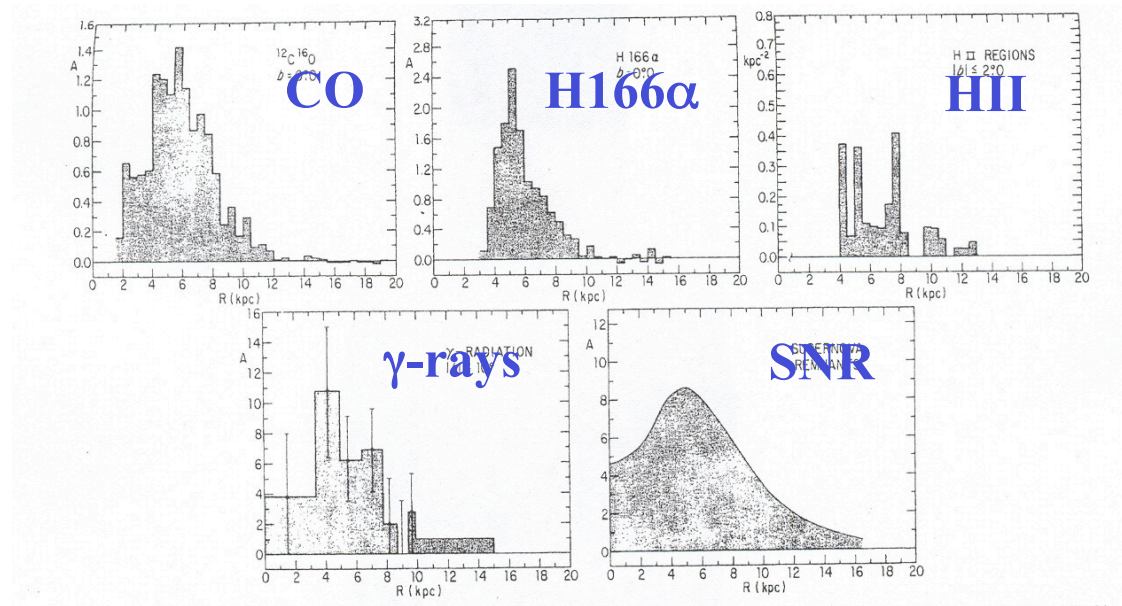
Solar circle: $R = R_0 = 8.5$ kpc

Inner Galaxy: $R < R_0$

Outer Galaxy: $R > R_0$

Far-Outer Galaxy: $R > 15$ kpc

Distribution ISM



$R(\text{kpc}): 0 \quad 10 \quad 20$

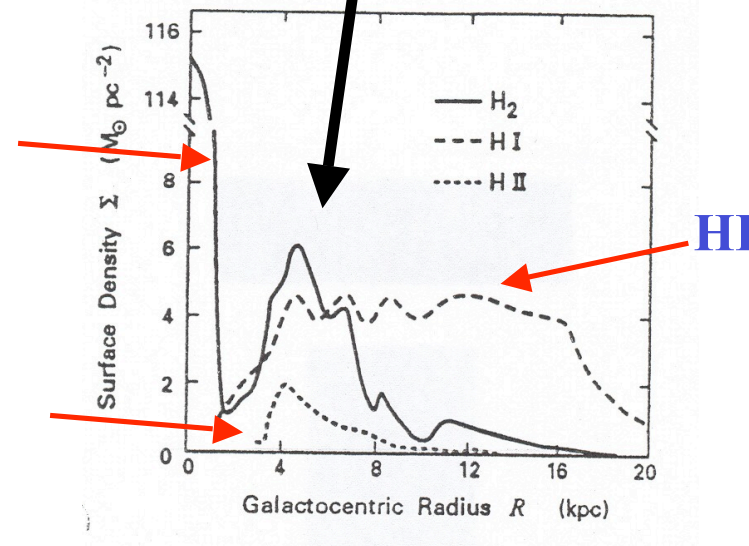
Galactic ring
 $4 < R < 6 \text{ kpc}$

Distributions peak at $R < R_0 = 8.5 \text{ kpc}$
 Max. extent $\sim 2 R_0$

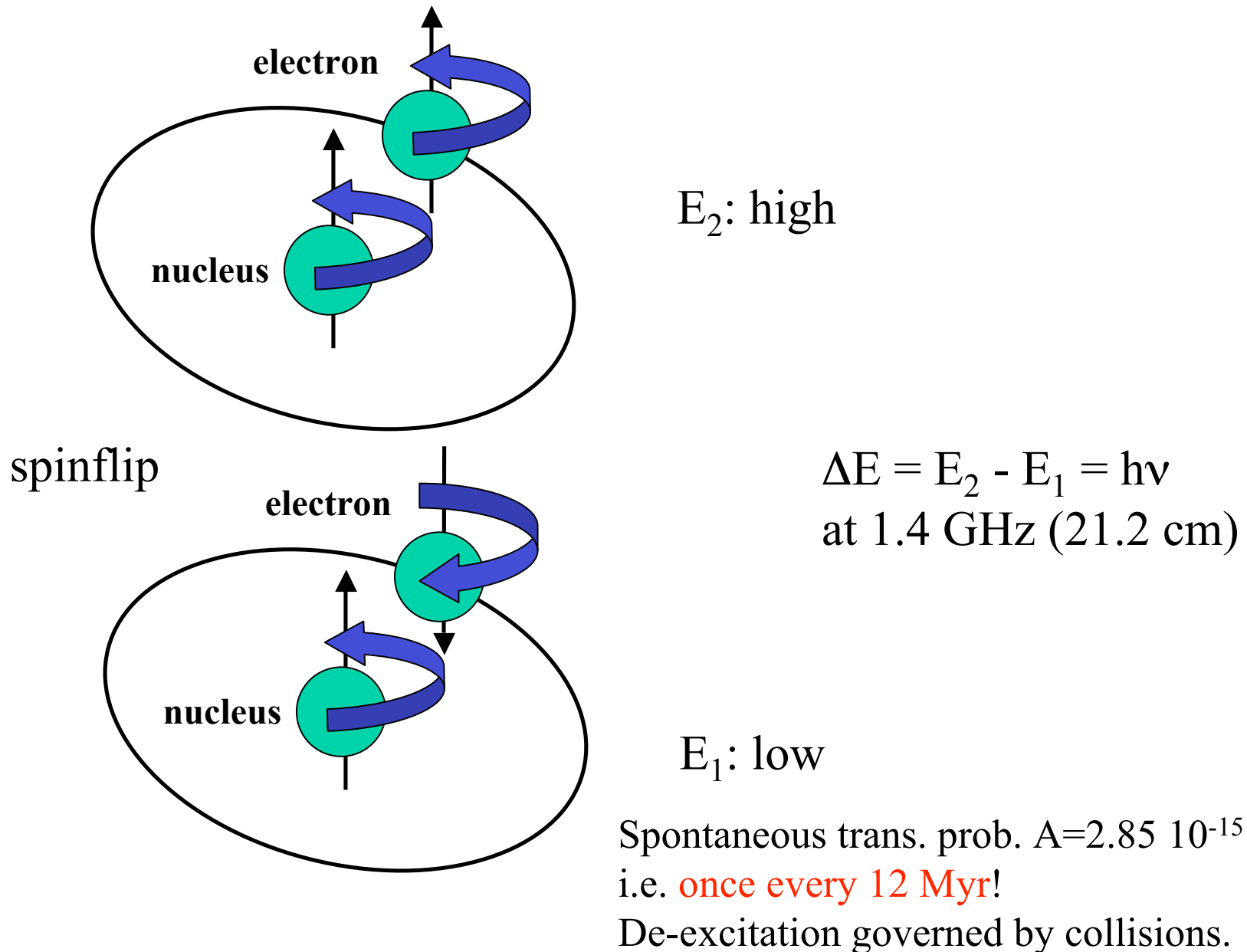
H_2

H II

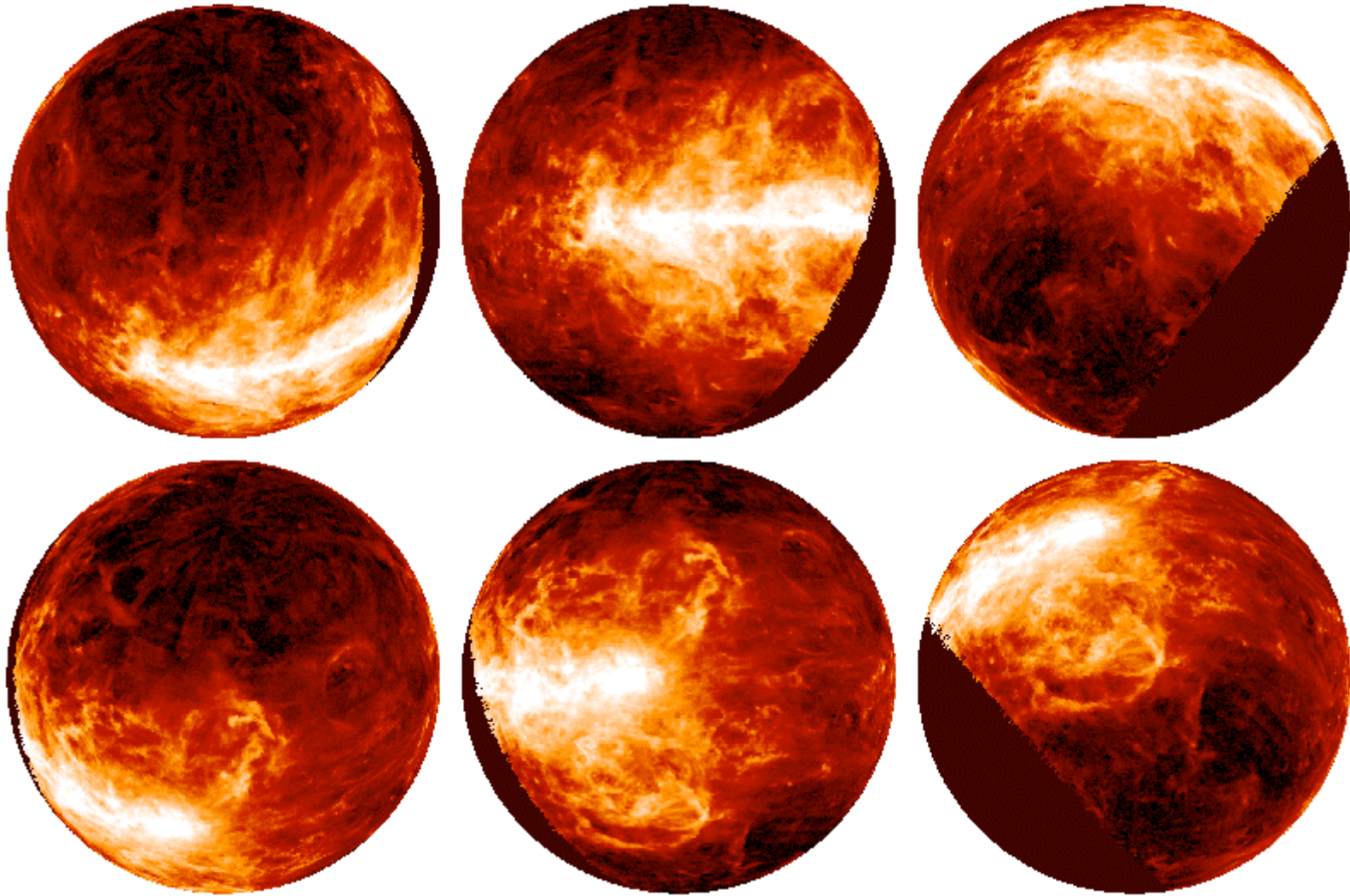
H I



Radiation mechanism of HI



Galactic distribution HI



Hartmann & Burton 1994

CO, not H₂

ISM composed essentially of hydrogen:

HI: 21-cm line

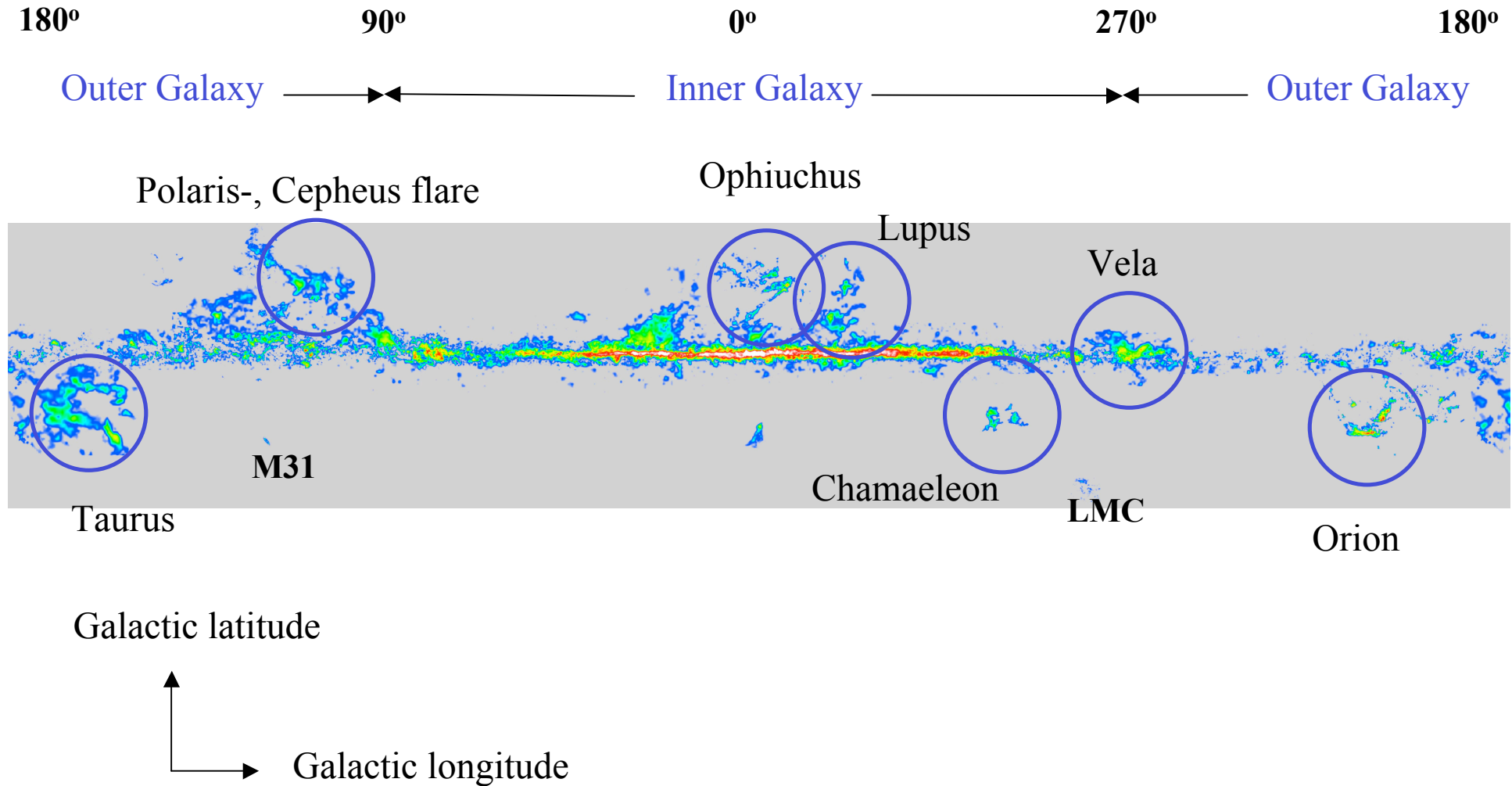
H₂: symmetric molecule \Rightarrow no radio emission

- UV absorption lines
- IR emission lines

CO: most abundant after H₂ : $[\text{H}_2]/[\text{CO}] \sim 1 \times 10^{-4}$.

- excited by collisions with H₂
- easily observed rotational transitions at (sub-)mm wavelengths
- $n(\text{H}_2) \geq \text{a few} \times 10^3 \text{ cm}^{-3}$

Galactic distribution CO



Dame, Hartmann & Thaddeus 2001

HI: tilted disk

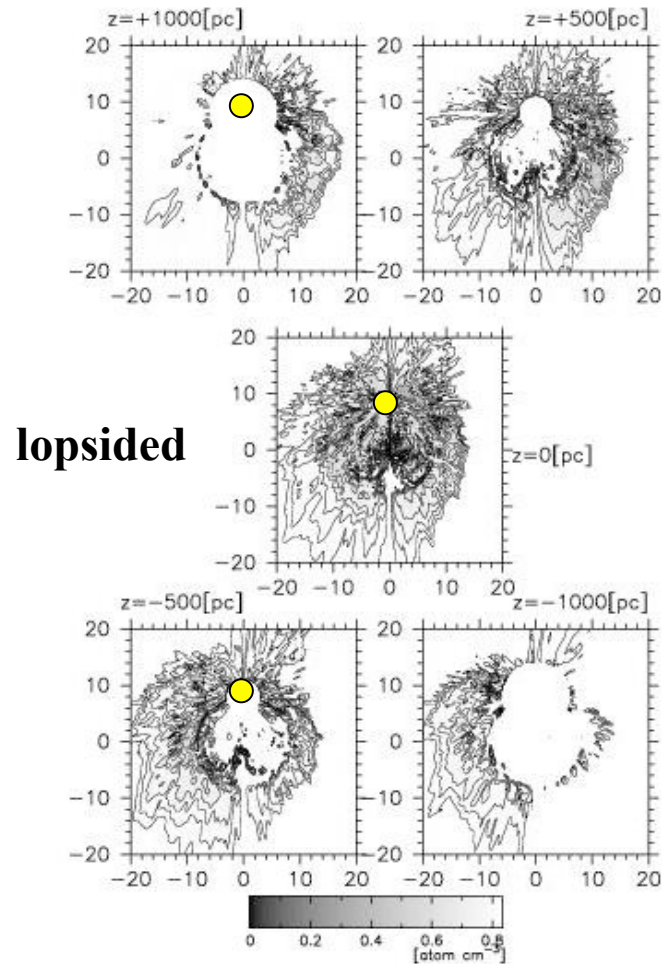


Fig 6

Nakanishi & Sofue 2003 PASJ

HI: warped & flared disk

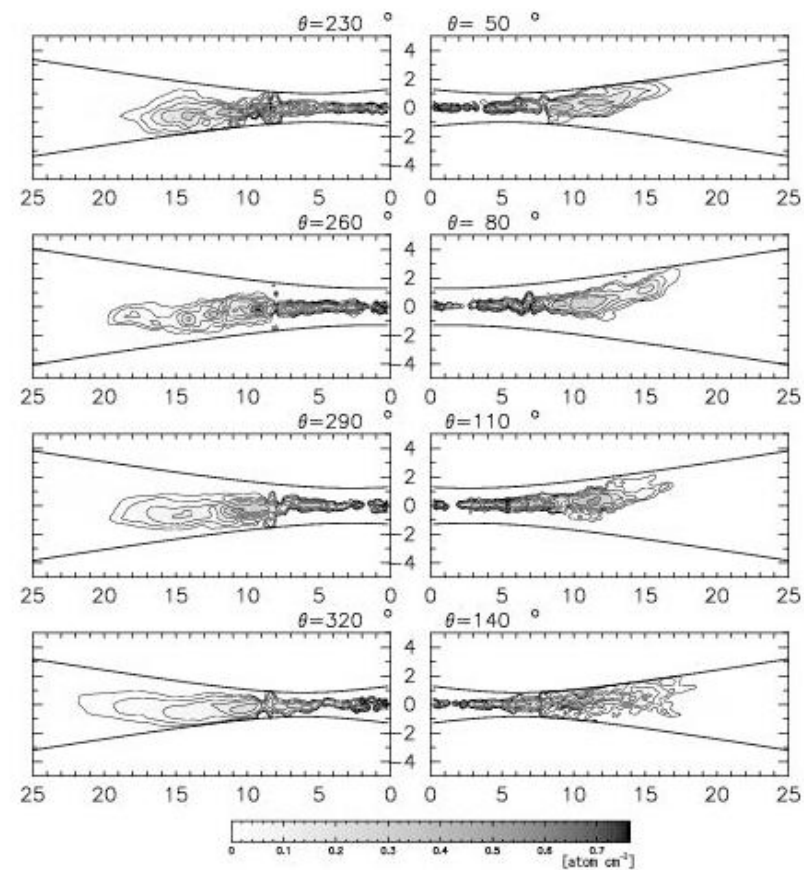


Fig 7

Same seen in H₂/CO

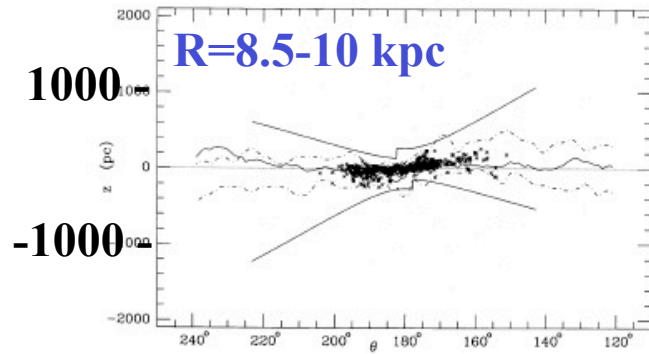


Fig. 8a. Distribution with galactocentric azimuth of the z heights of molecular clouds with kinematic distances in the range $R = 8.5$ to 10.0 kpc

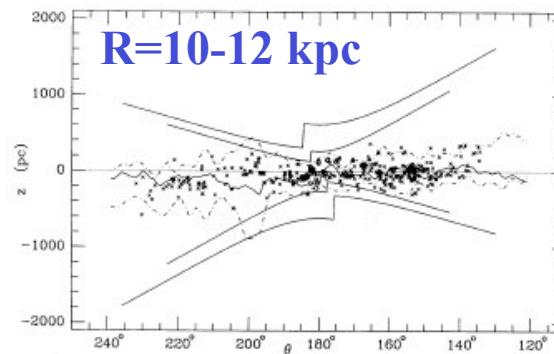


Fig. 8b. Shape of the molecular cloud layer at $10 < R < 12$ kpc

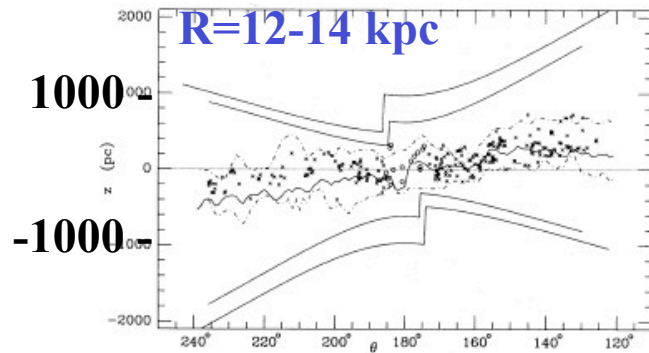


Fig. 8c. Shape of the molecular cloud layer at $12 < R < 14$ kpc

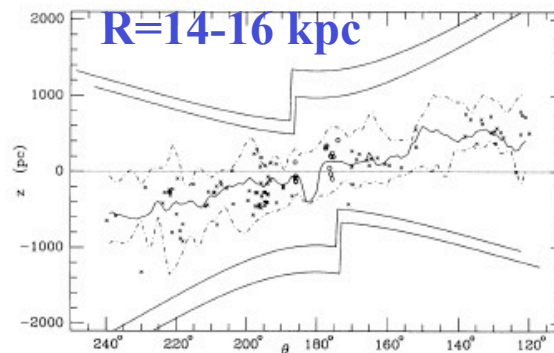


Fig. 8d. Shape of the molecular cloud layer at $14 < R < 16$ kpc

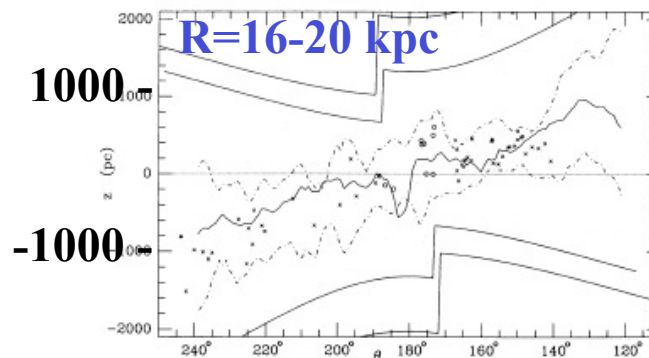
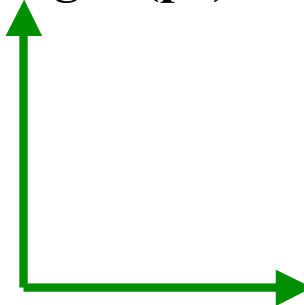


Fig. 8e. Shape of the molecular cloud layer at $16 < R < 20$ kpc

z-height (pc)

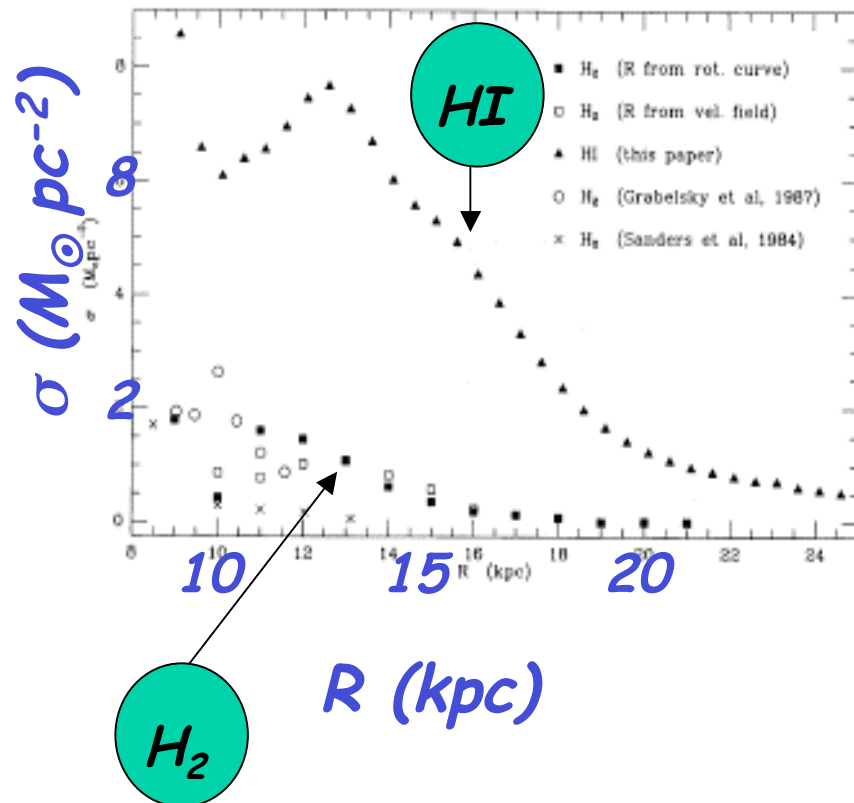


**Galactocentric
azimuth (deg)**

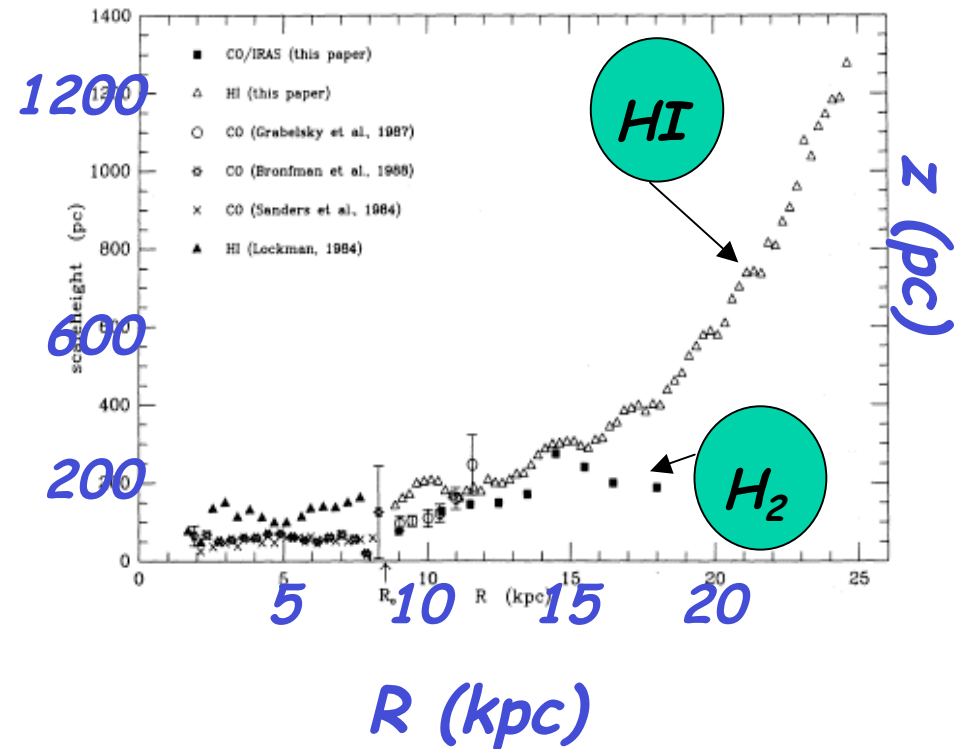
Warping & flaring in CO

*Wouterloot, Brand, Burton, & Kwee
1990, A&A 120, 21*

Surface density



Scale height



"flared disk" ('a svasato')

In OG: Surface density down, scale height up \Rightarrow volume density even lower

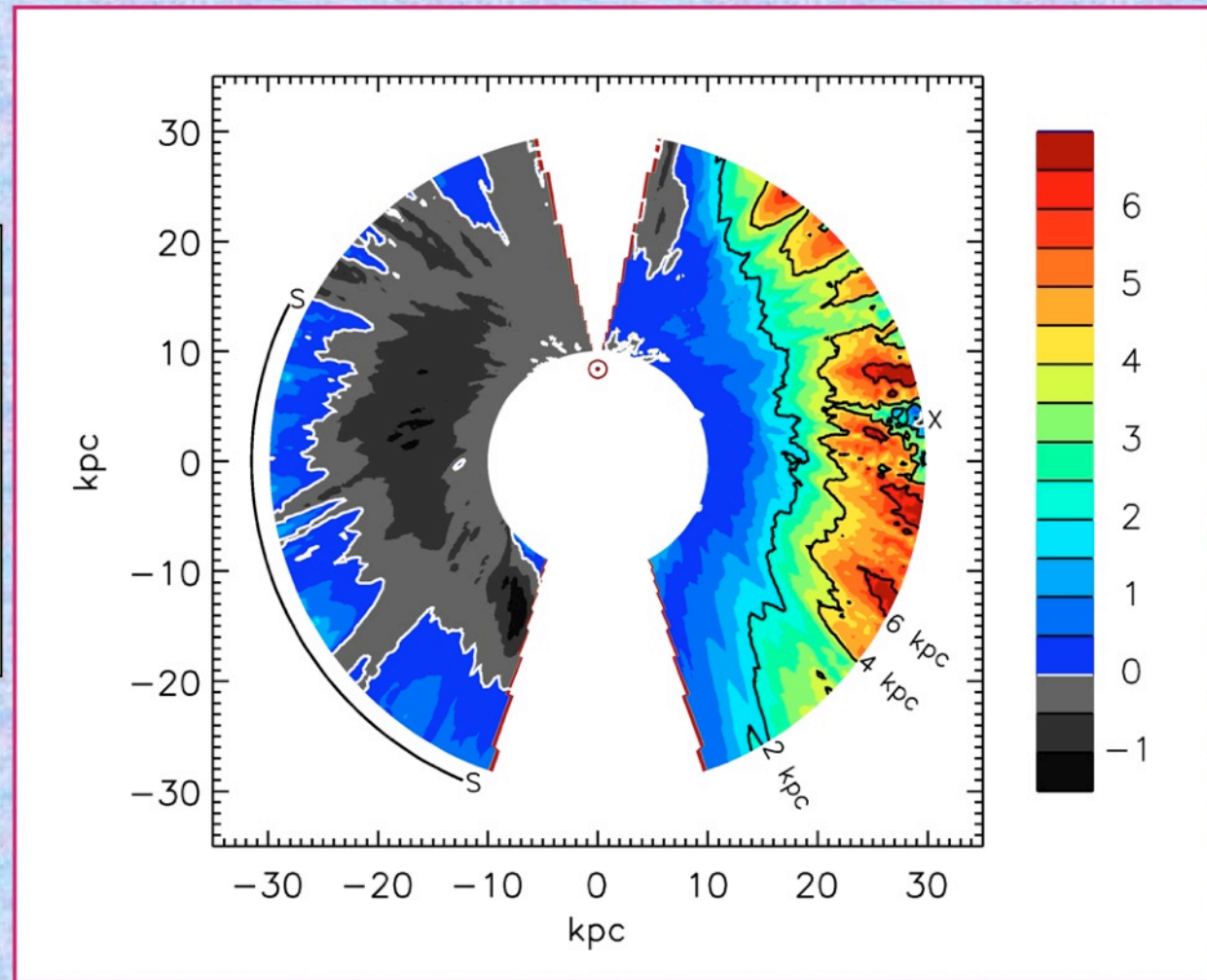
Wouterloot, Brand, Burton, & Kwee 1990

Displacement of mean plane from $b = 0^\circ$

Blue, Red = pos

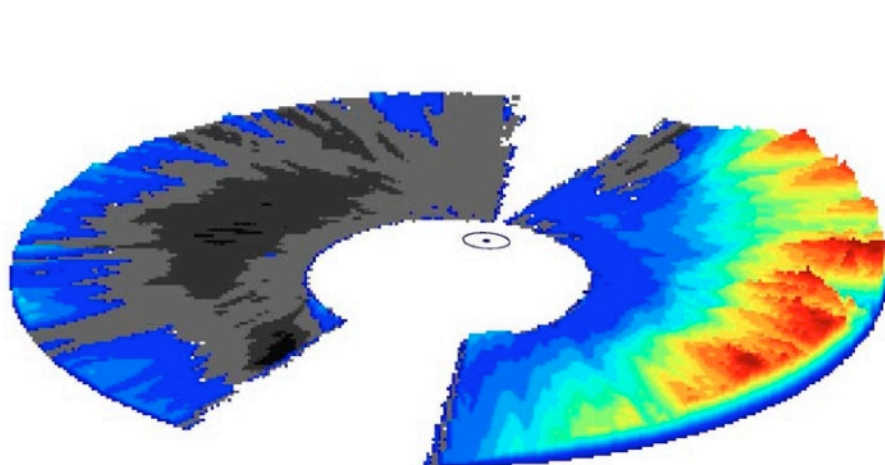
Grey = neg

Darker hues
mean higher
amplitude

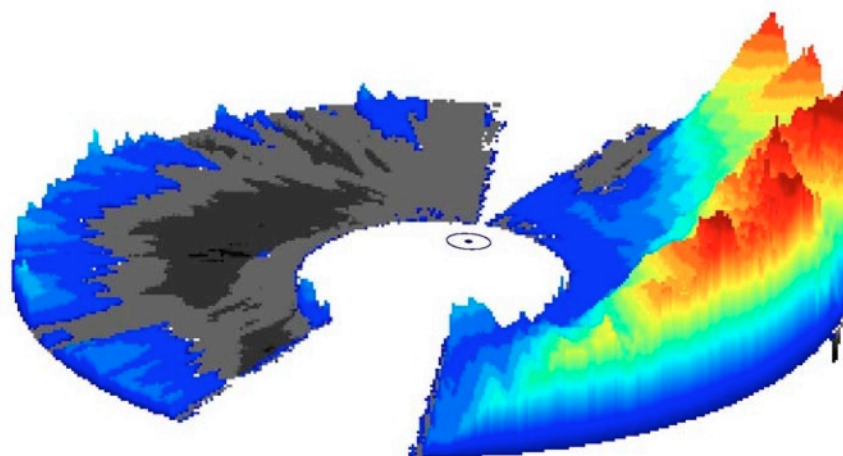


Levine, Blitz, Heiles, Weinberg 2008, 2006

View of warp from $l = 30^\circ$



To Scale

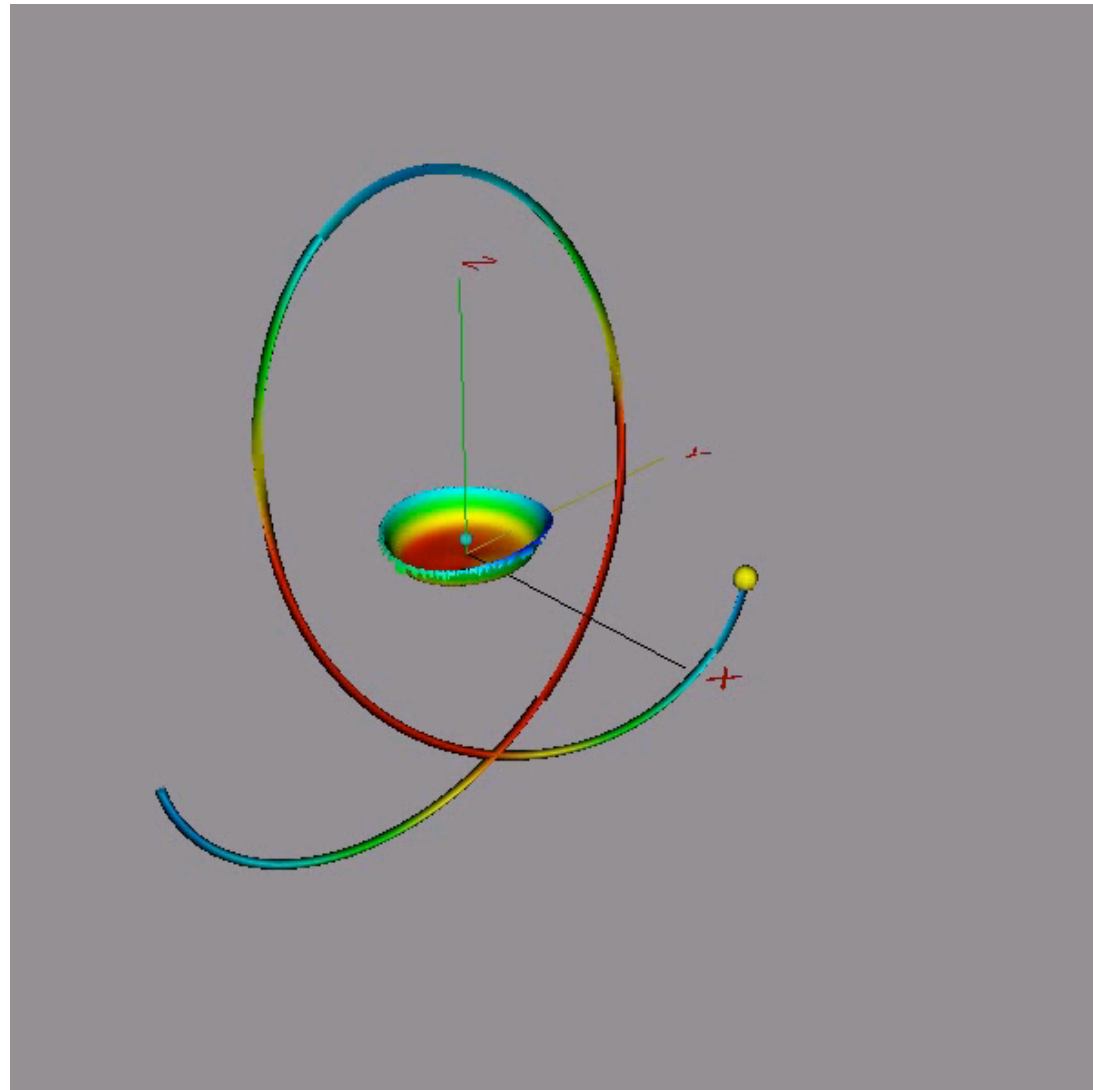


5x exaggeration

Levine, Blitz, Heiles, Weinberg 2008, 2006

Milky Way Galaxy: “warped and vibrating like a drum”

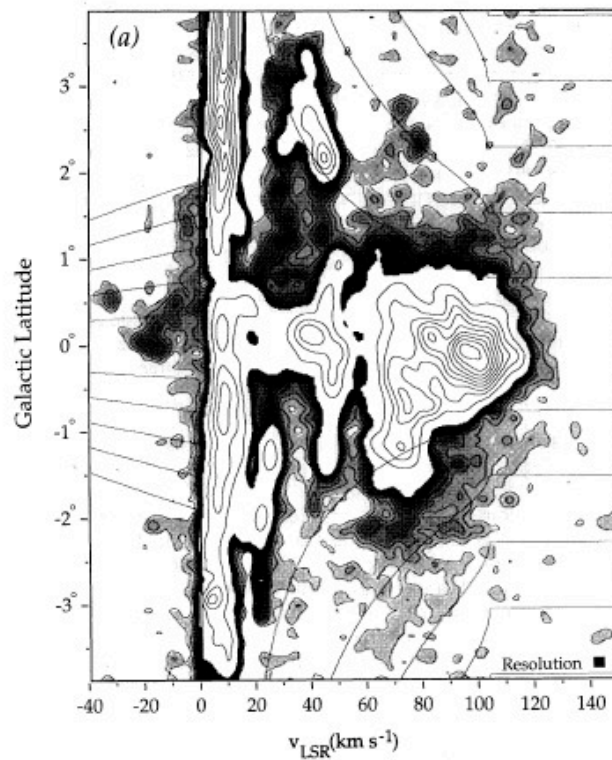
Levine, Blitz, Heiles,
Weinberg 2008, 2006



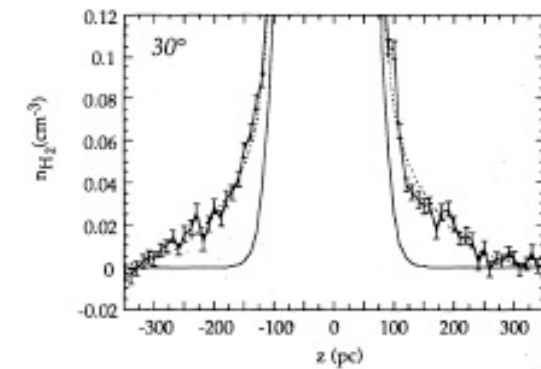
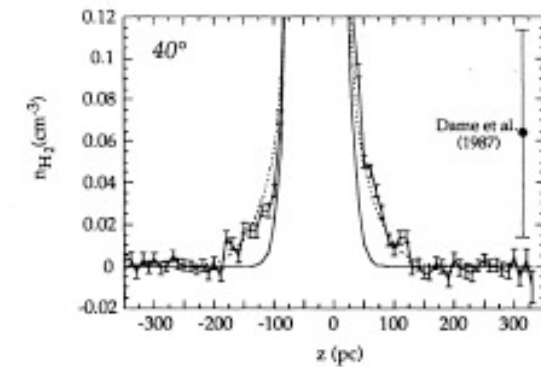
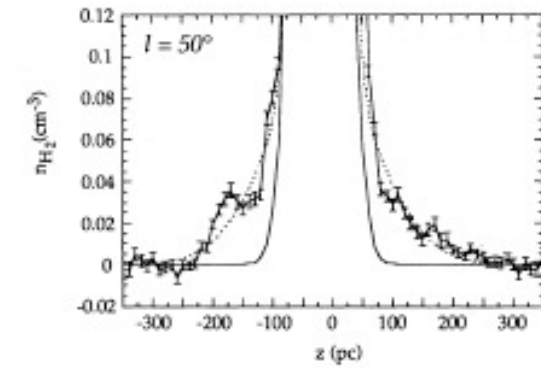
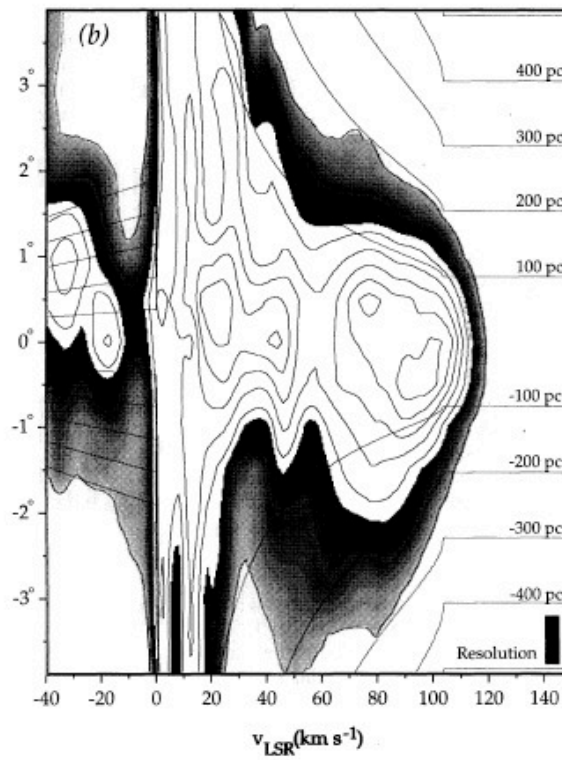
A thick disk in CO

(Dame & Thaddeus 1994)

CO (29.5-30.5 degs)



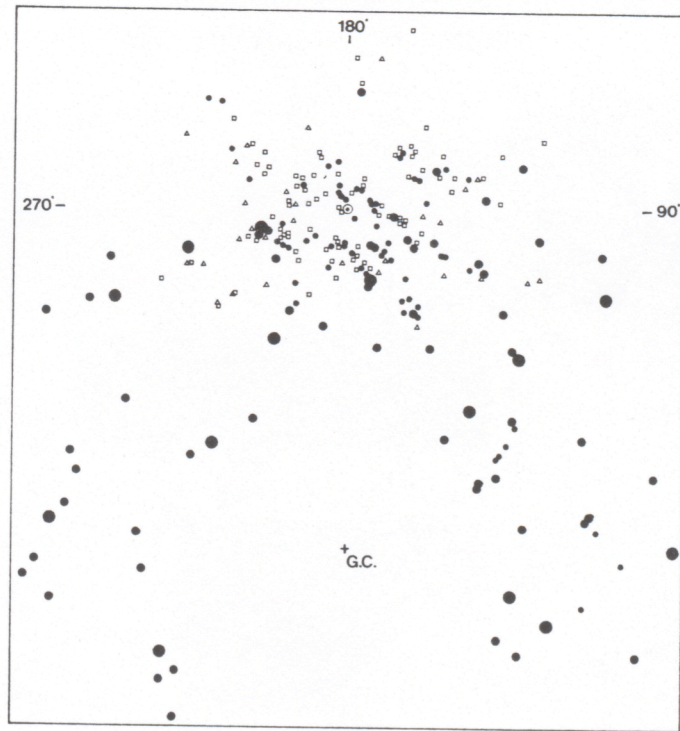
HI



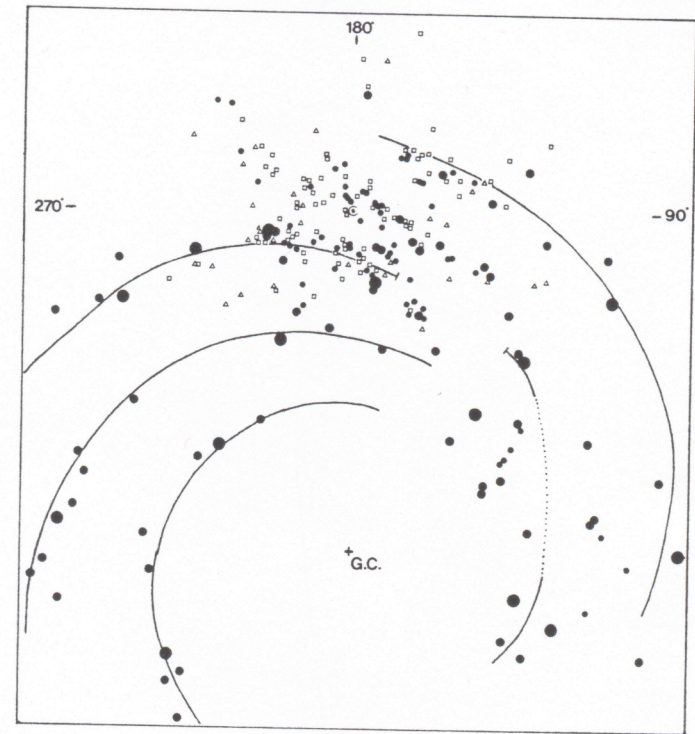
$n(\text{H}_2)$ vs. z-height

Is there a spiral arm pattern?

Distribution of
HII regions
(young stars)



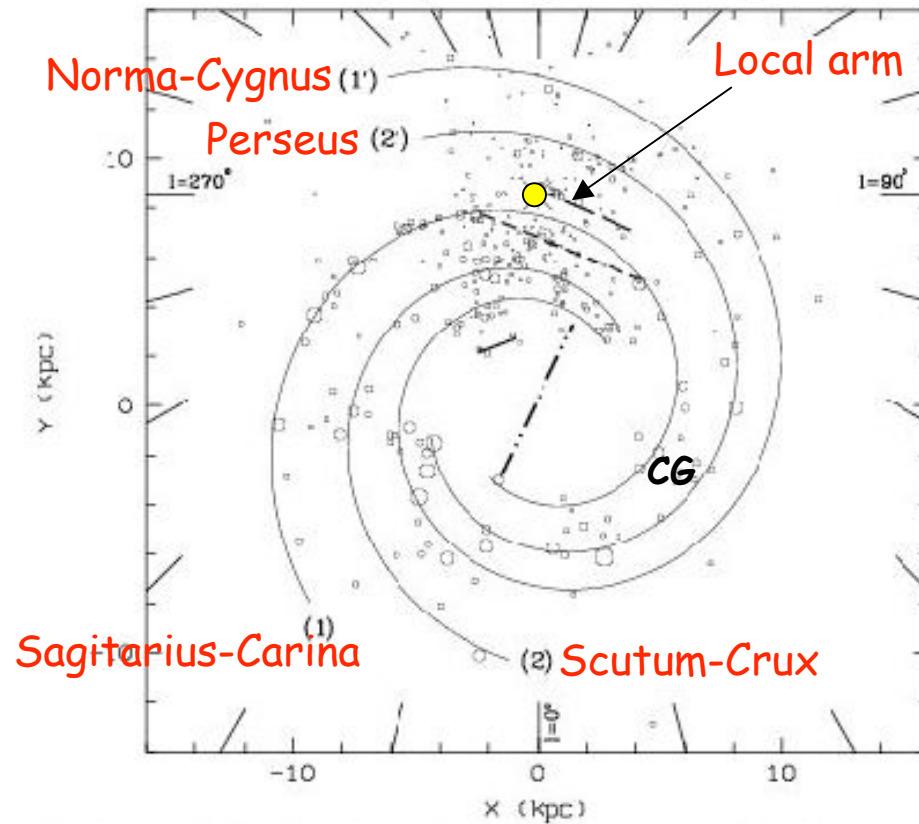
Same, but with
spiral pattern
drawn in



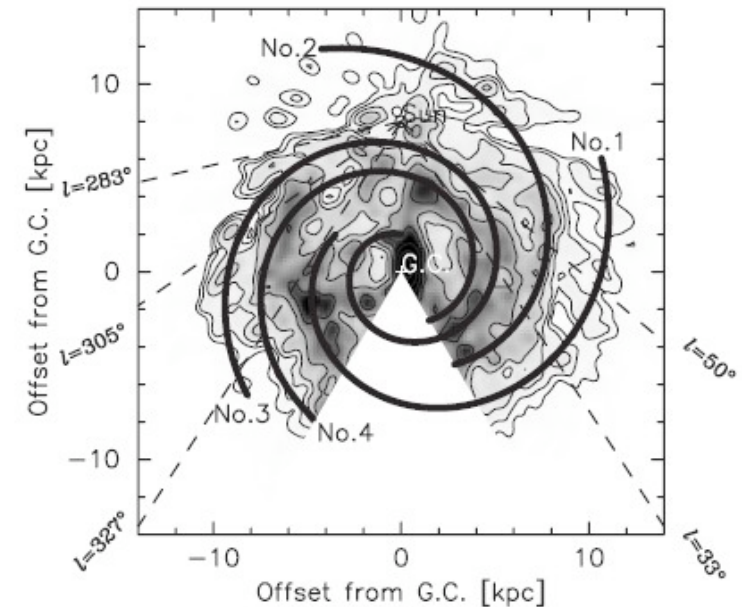
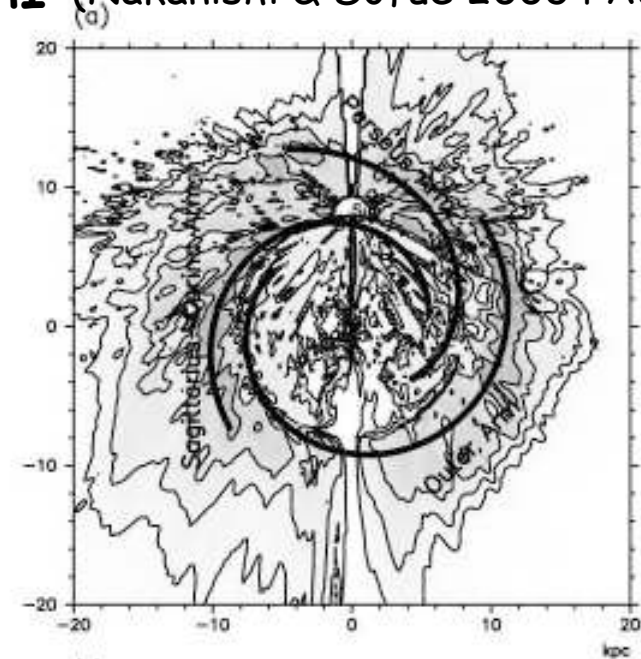
Georgelin 1975

Spiral structure

From H α (Russeil, A&A 2003)



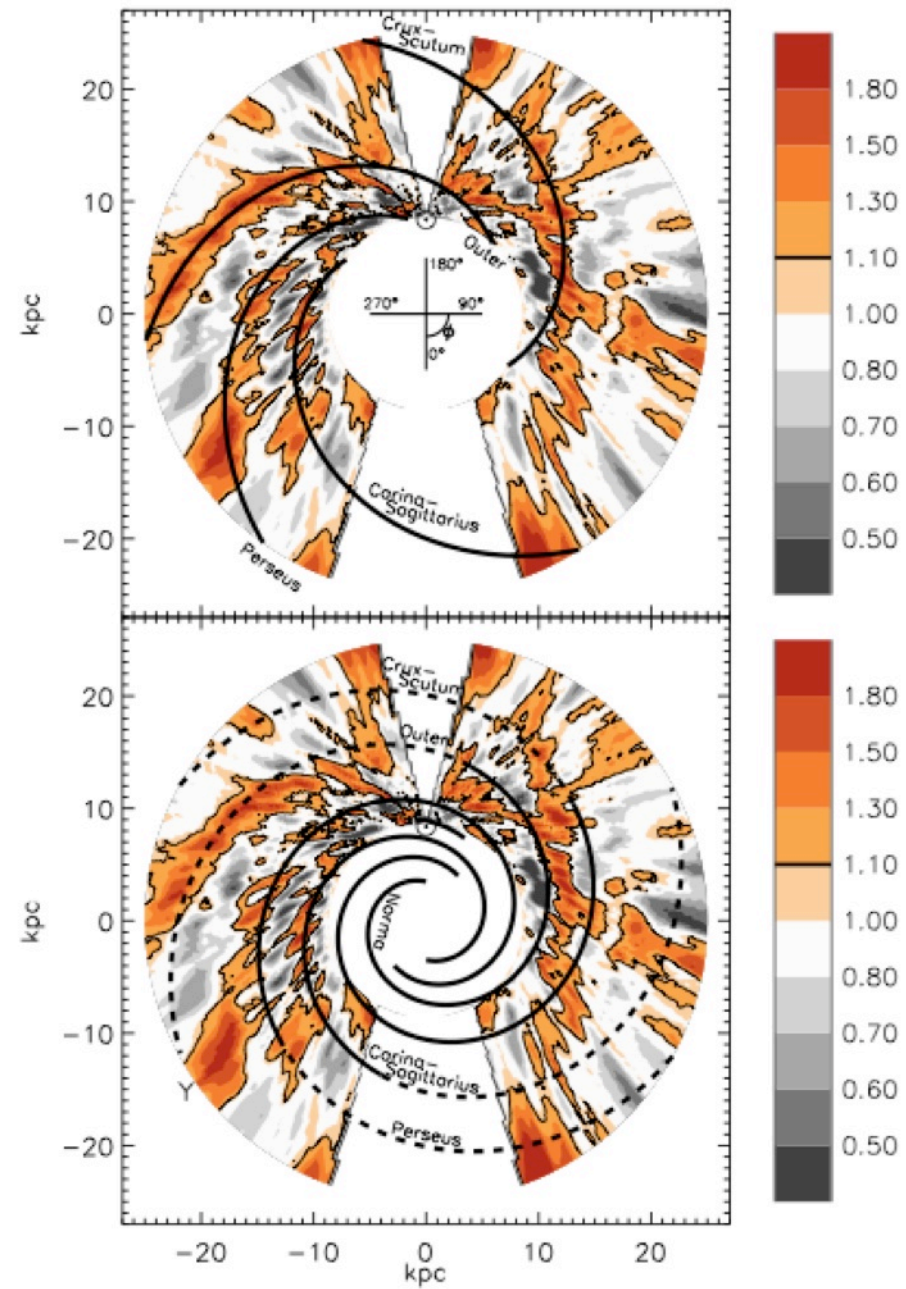
From HI (Nakanishi & Sofue 2003 PASJ)



From CO(1-0)

(Nakanishi & Sofue 2006 PASJ)

From HI



Levine, Blitz, Heiles, Weinberg 2008, 2006

***NEW* Outer arm in HI**

McClure-Griffiths et al. 2004

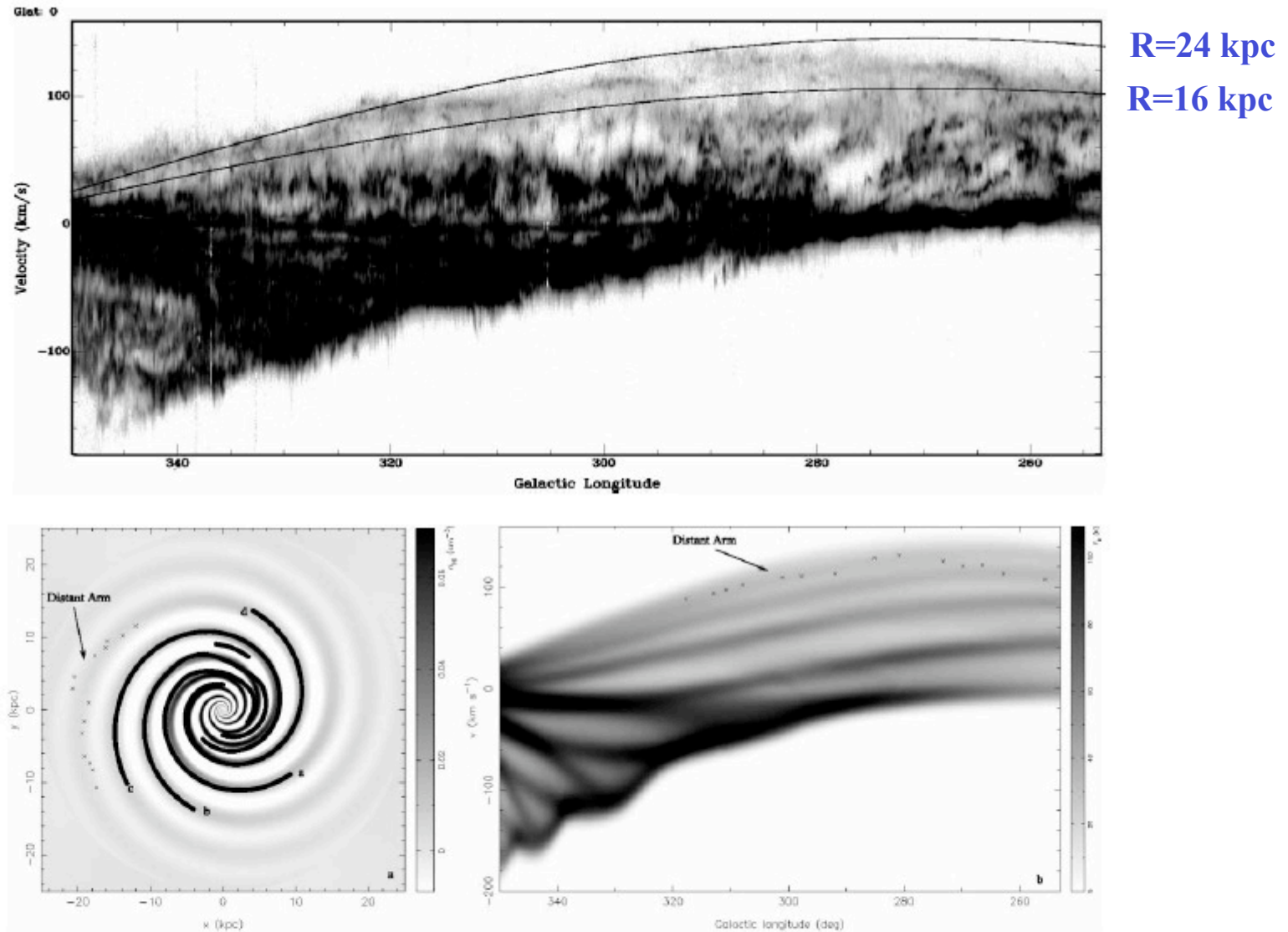


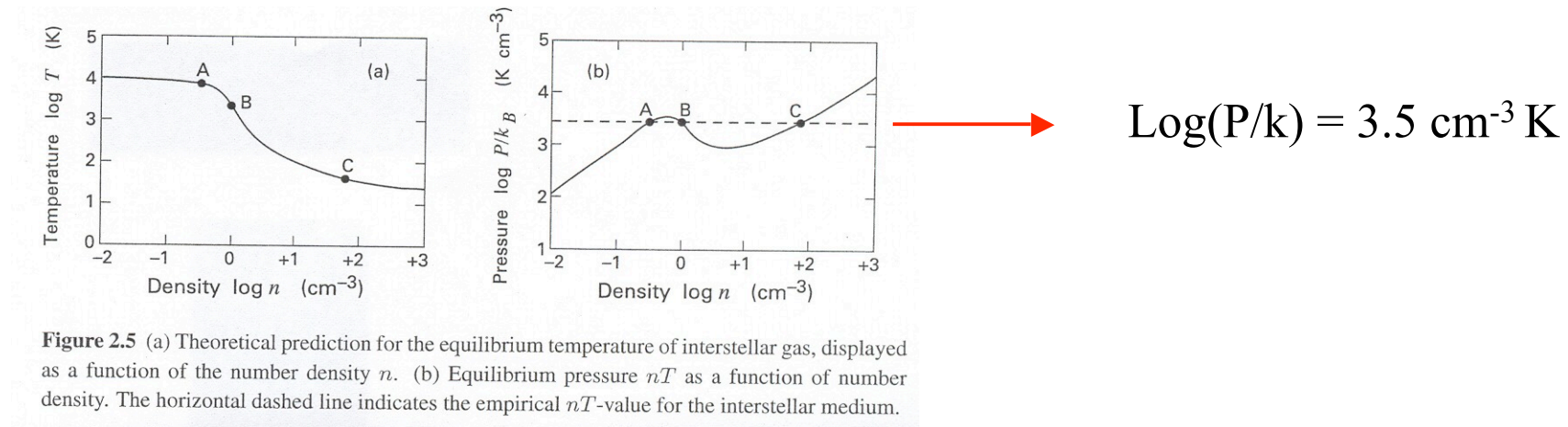
FIG. 1.—(a) Differential H I density (spiral perturbation minus the underlying Toomre disk) for the simple four-arm Milky Way spiral model described in § 4.

The multi-phase ISM

		T(K)	$n_H(\text{cm}^{-3})$	f_v	f_M	Probes
HII						
traditional		10^4	$0.1-10^4$	0.001	0.02	H α , recomb. lines
coronal	HIM	$\geq 3 \times 10^5$	0.003	0.6?	0.001	[OVI], X-rays
warm	WIM	8000	0.25	0.2	0.1?	HI, H α , H166 α
HI						
clouds	CNM	80	40	0.025	0.4	HI
warm	WNM	8000	0.4	0.1-0.5?		HI
H₂						
diffuse	Transl	30-80	10^2-10^3	≤ 0.01		HI, CO, 100 μm
dense	Dark	10-100	10^3-10^6	0.005	0.5	mm molec. lines FIR dust

Models of the ISM (2-phase)

Early model: Field, Goldsmith & Habing 1969



Assume pressure equilibrium ($P/k \propto nT = \text{constant}$)

Stable points: A and C, corresponding to:

WNM ($n=0.4$, $T=7000$) and CNM ($n=60$, $T=50$)

Explained most of the then-known observations.

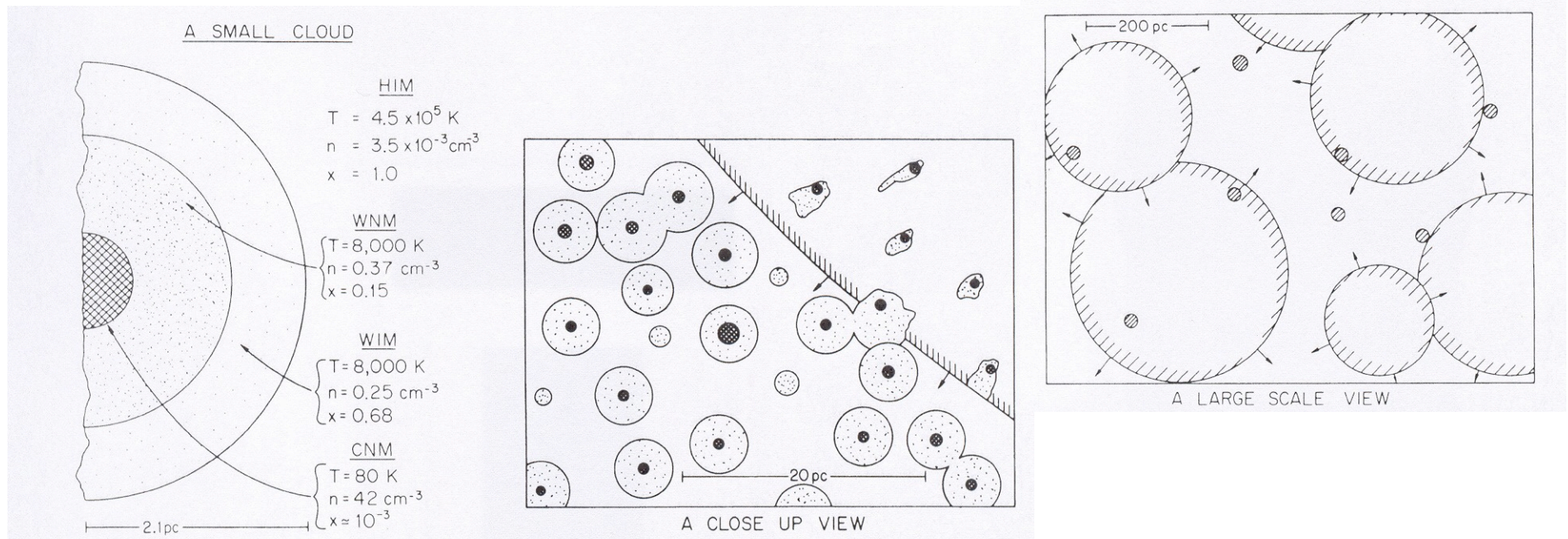
Models of the ISM (3-phase)

Ostriker & McKee 1977: 3-phase model

Gas distributed among 4(!) forms: HIM, WIM, WNM, CNM that are in P-equil. at $P/k \approx 3000 \text{ Kcm}^{-3}$.

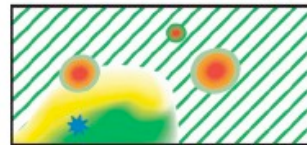
SNe, OB-winds create system of hot tunnels in ISM

Recent assesment: Cox, 2005 Ann. Rev. A&A 43

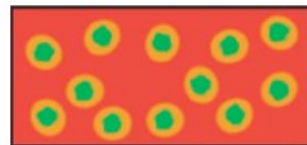


Models of the ISM (Cox upgrade)

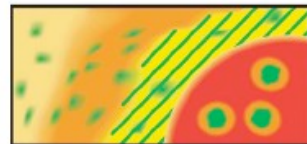
CONCEPTIONS: Within the disk



- Warm intercloud gas**
- Local SNRs
 - Ionized regions



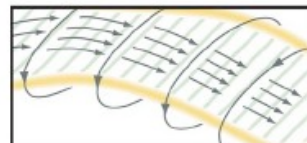
- Hot intercloud gas**
- Dilute SNRs
 - Evaporating clouds
 - Ionized surfaces



- Tepid intercloud gas**
- Local hotter regions
 - Evaporating clouds

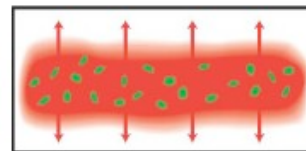


- Adding superbubbles**
- But to which picture?

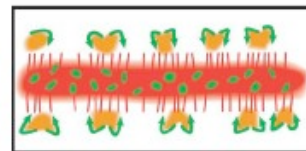


- Flux ropes**
- Filamentation
 - Emptiness

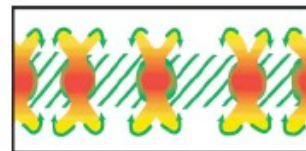
CONCEPTIONS: Vertical



- Thermal wind**
- From escaping hot intercloud gas
 - Or, a hot halo



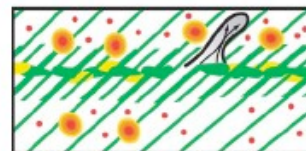
- Galactic fountain 1**
- From escaping hot intercloud gas which cools



- Galactic fountain 2**
- From superbubbles breaking out above the disk



- Thick quiescent disk**
- Superbubbles confined
 - Spiral density waves
 - Ionization mechanism?

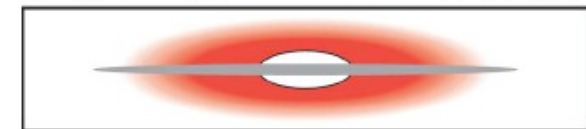


- Active halo**
- Cosmic ray wind
 - Microflares
 - High z super novae

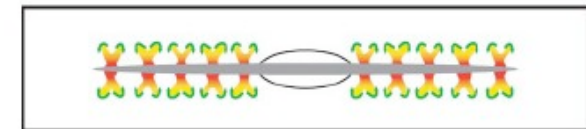
CONCEPTIONS: Global

Global thermal wind...

...or a hot halo?

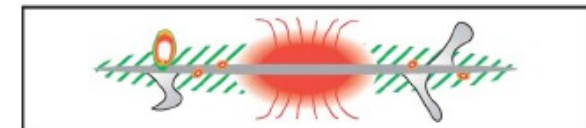


Galactic fountain



Thick Quiescent Disk...

...with nuclear wind?



Active halo

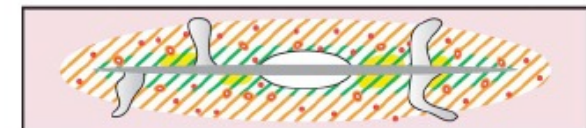


Figure 10 Various conceptions of the larger scale structure of the Galactic atmosphere. In this figure, *hatched green* indicates warm HI; *hatched green on yellow background*—diffuse warm HI; *orange*—hotter gas bearing OVI; *red*—material hot enough to emit X rays; *gray*—plumes of escaping cosmic rays; and *red dots*—microflares. Problems with the top two panels are discussed in the text. The lower two panels contain some elements of potentially greater realism.

Molecular clouds – transition interface

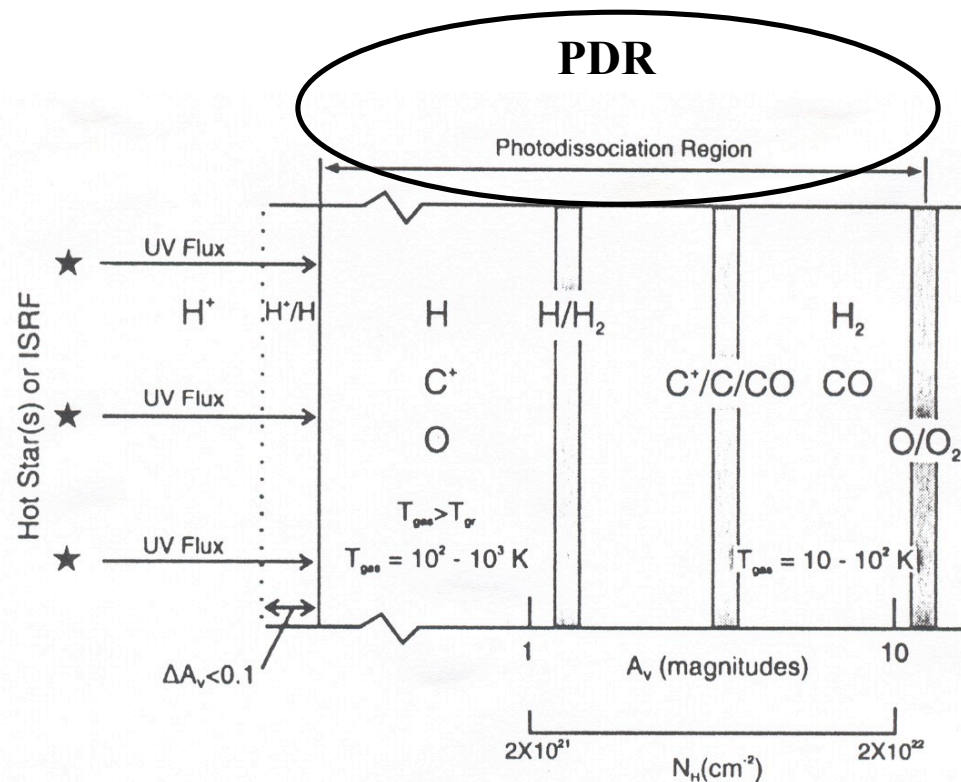


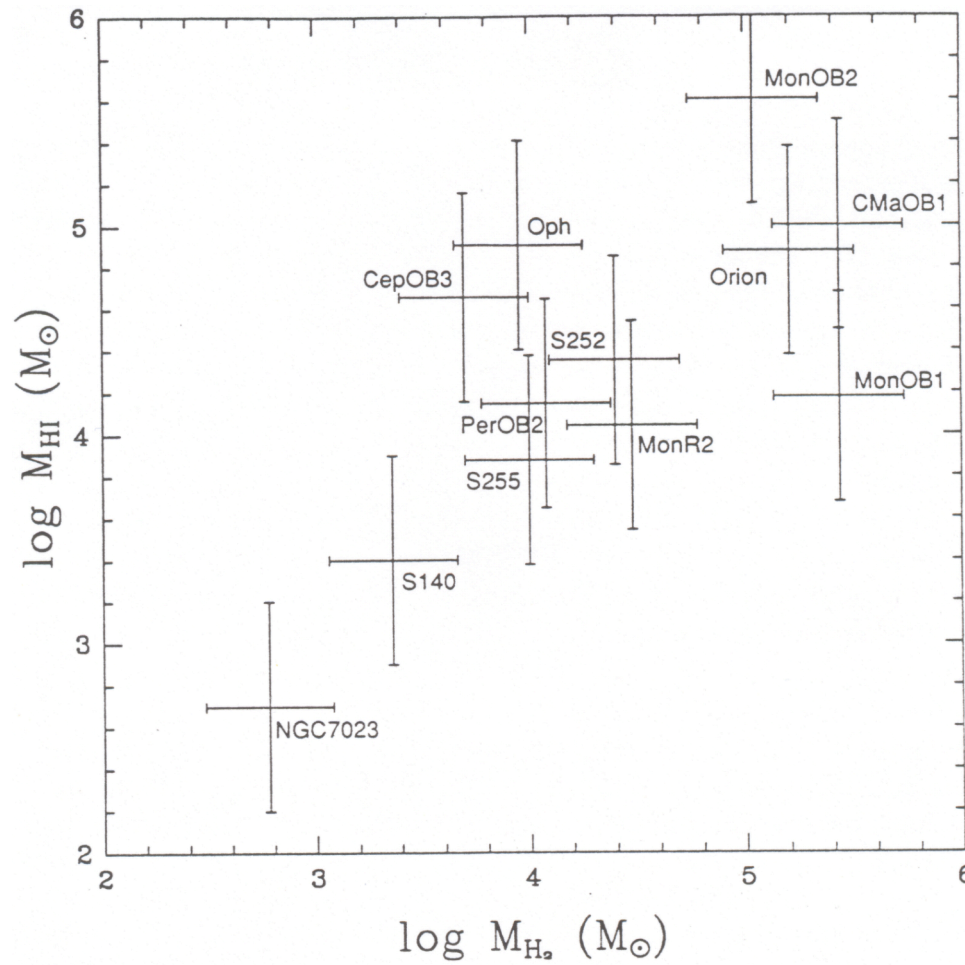
Figure 3 A schematic diagram of a photodissociation region. The PDR is illuminated from the left and extends from the predominantly atomic surface region to the point where O_2 is not appreciably photodissociated ($\simeq 10$ visual magnitude). Hence, the PDR includes gas whose hydrogen is mainly H_2 and whose carbon is mostly CO. Large columns of warm O, C, C^+ , and CO and vibrationally excited H_2 are produced in the PDR. The gas temperature T_{gas} generally exceeds the dust temperature T_{dust} in the surface layer.

Molecular clouds are self-shielding against UV radiation.

Clouds are surrounded by envelope of HI.

Inside: molecules. Most abundant after H_2 is CO (10^{-4}).

Molecular clouds: atomic envelope



Blitz, 1993 PPIII

Sh 2 - 217

H α

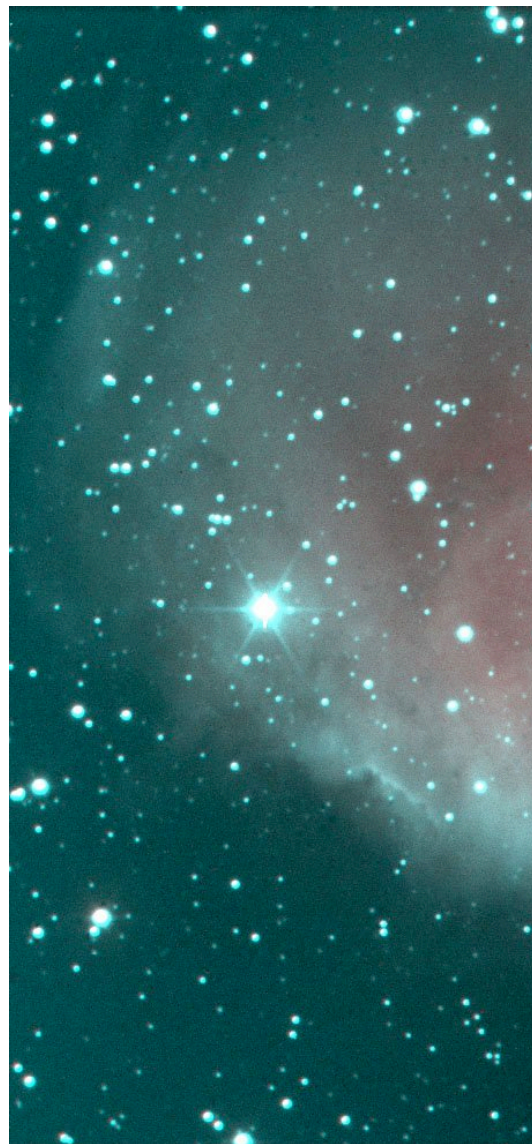


Deharveng et al. 2003

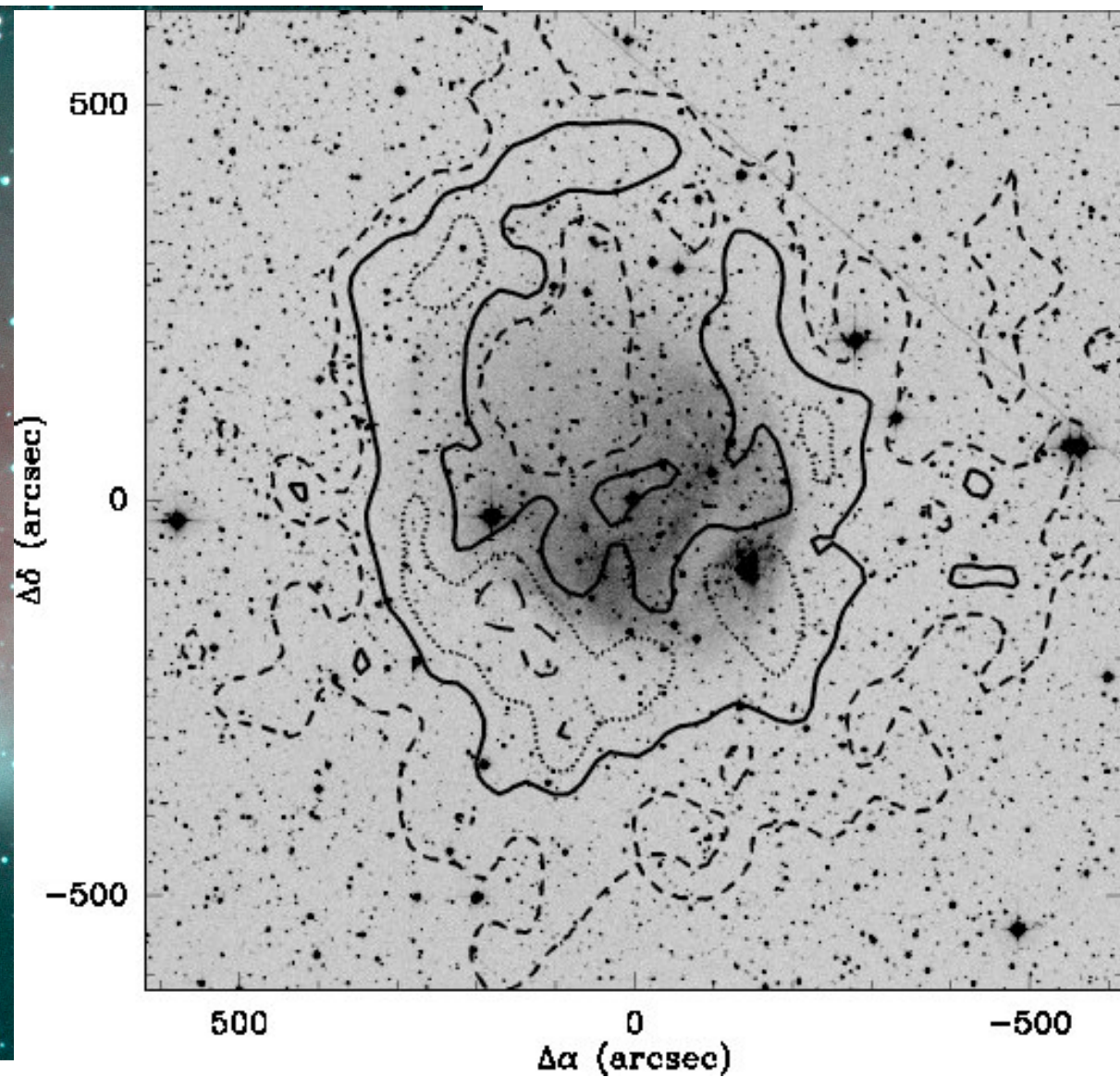
Sh 2 - 217

H α

Opt. + HI

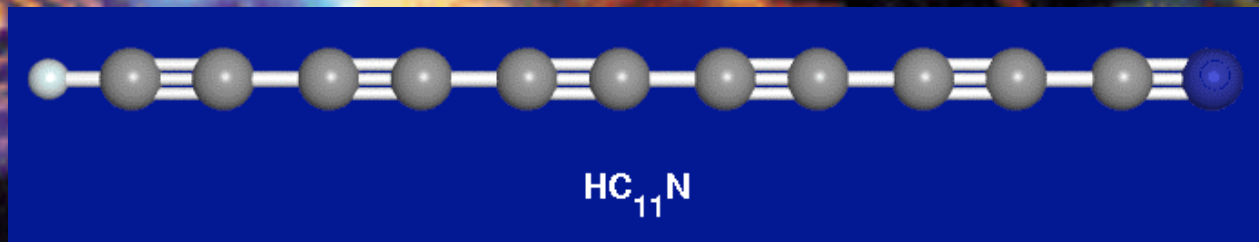


Deharveng et al. 2003



Brand et al. 2009 in prep.

Interstellar Molecules

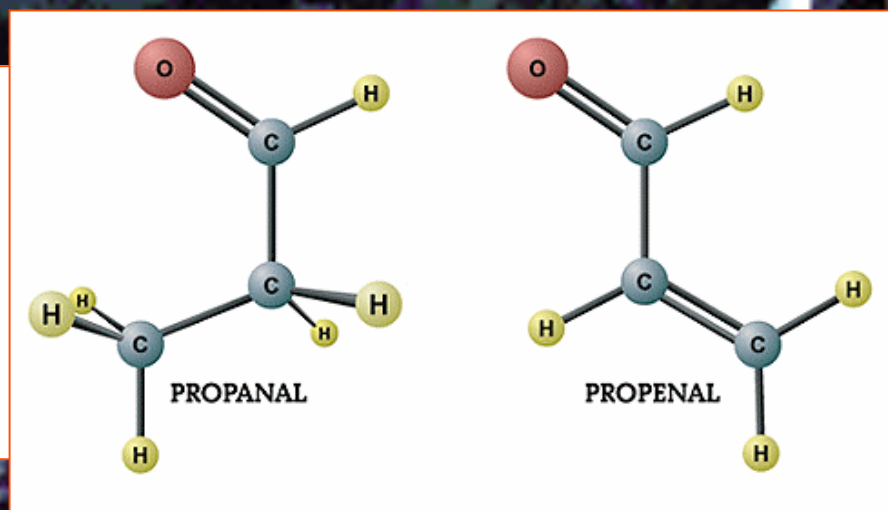


New species!

CH_2CHCHO (propenal)

$\text{CH}_3\text{CH}_2\text{CHO}$ (propanal)

(Hollis et al. 2004 at Green Bank @ 13-20 GHz)



Circa 150 molecules have been detected in space

2 atoms	3 atoms	4 atoms	5 atoms	6 atoms	7 atoms	8 atoms	9 atoms	10 atoms	11 atoms	12 atoms	13 atoms
H ₂	C ₃ [*]	c-C ₃ H	C ₅ [*]	C ₅ H	C ₆ H 2008	CH ₃ C ₃ N	CH ₃ C ₄ H	CH ₃ C ₅ N	HC ₉ N	C ₆ H ₆ [*] (?)	HC ₁₁ N
AlF	C ₂ H	I-C ₃ H	C ₄ H	I-H ₂ C ₄	CH ₂ CHCN 2008	HC(O)OCH ₃	CH ₃ CH ₂ CN	(CH ₃) ₂ CO	CH ₃ C ₆ H	C ₂ H ₅ OCH ₃ ?	
AlCl	C ₂ O	C ₃ N	C ₄ Si	C ₂ H ₄ [*]	CH ₃ C ₂ H	CH ₃ COOH	(CH ₃) ₂ O	(CH ₂ OH) ₂	C ₂ H ₅ OCHO 2009	n-C ₃ H ₇ CN 2009	
C ₂ ^{**}	C ₂ S	C ₃ O	I-C ₃ H ₂	CH ₃ CN	HC ₅ N	C ₇ H	CH ₃ CH ₂ OH	CH ₃ CH ₂ CHO			
CH	CH ₂	C ₃ S	c-C ₃ H ₂	CH ₃ NC	CH ₃ CHO	H ₂ C ₆	HC ₇ N				
CH ⁺	HCN	C ₂ H ₂ [*]	H ₂ CCN	CH ₃ OH	CH ₃ NH ₂	CH ₂ OHCHO	C ₈ H				
CN	HCO	NH ₃	CH ₄ [*]	CH ₃ SH	c-C ₂ H ₄ O	I-HC ₆ H [*] (?)	CH ₃ C(O)NH ₂				
CO	HCO ⁺	HCCN	HC ₃ N	HC ₃ NH ⁺	H ₂ CCHOH	CH ₂ CHCHO (?)	C ₈ H ⁻				
CO ⁺	HCS ⁺	HCNH ⁺	HC ₂ NC	HC ₂ CHO	C ₆ H ⁻	CH ₂ CCHCN	C ₃ H ₆				
CP	HOC ⁺	HNCO	HCOOH	NH ₂ CHO		H ₂ NCH ₂ CN 2008					
SiC	H ₂ O	HNCS	H ₂ CNH	C ₅ N							
HCl	H ₂ S	HOCO ⁺ 2008	H ₂ C ₂ O	I-HC ₄ H ⁺ (?)							
KCl	HNC	H ₂ CO	H ₂ NCN	I-HC ₄ N							
NH	HNO	H ₂ CN	HNC ₃	c-H ₂ C ₃ O							
NO	MgCN	H ₂ CS	SiH ₄ [*]	H ₂ CCNH (?)							

Ca. 150 mol's

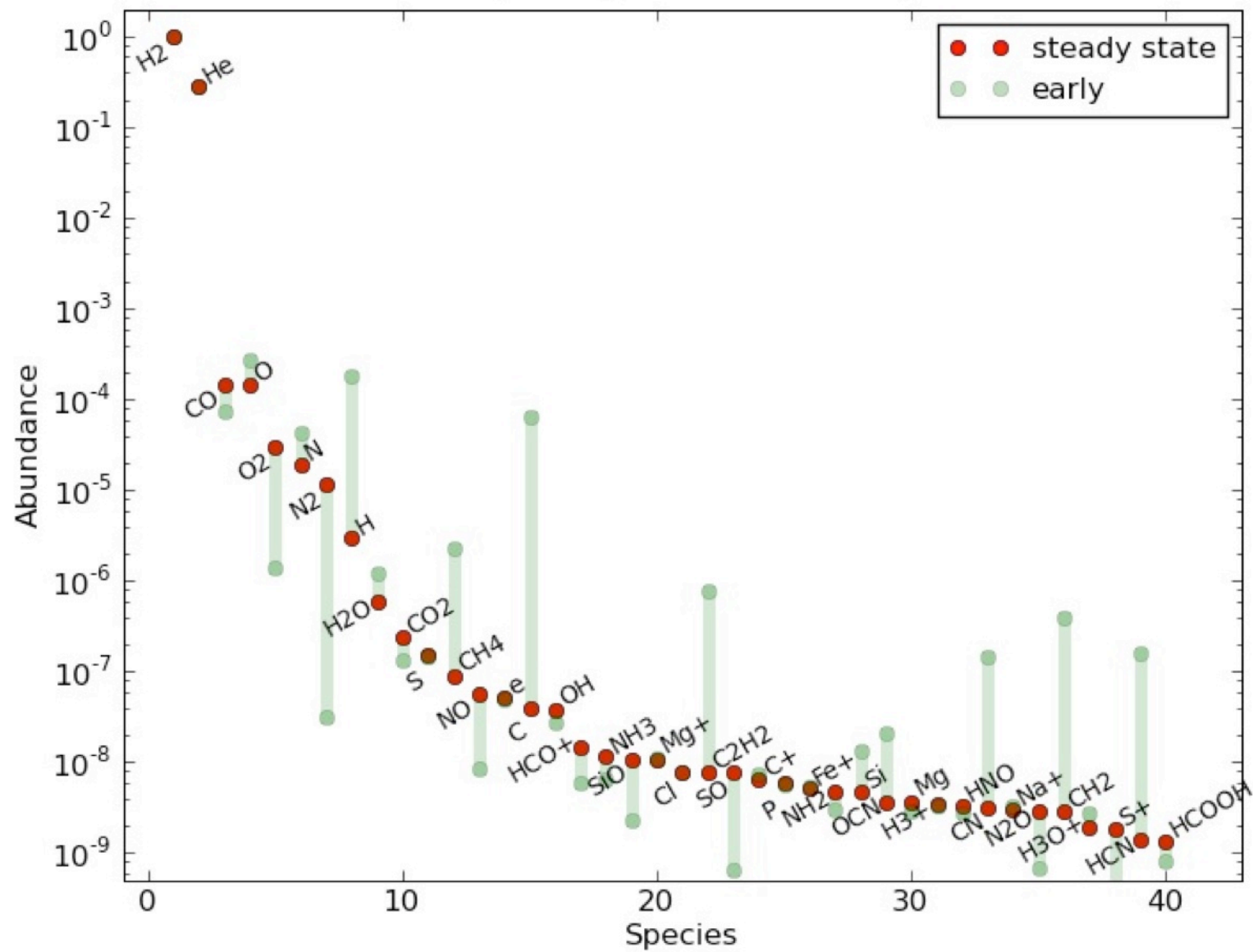
Source: CDMS [Cologne Database for Molecular Spectroscopy]

[illegible]

Extragalactic Molecules (as of 01/2008)

2 atoms	3 atoms	4 atoms	5 atoms	6 atoms	7 atoms
OH	H ₂ O	H ₂ CO	c-C ₃ H ₂	CH ₃ OH	CH ₃ CCH
CO	HCN	NH ₃	HC ₃ N	CH ₃ CN	
H ₂	HCO ⁺	HNCO	CH ₂ NH		
CH **	C ₂ H	H ₂ CS (?)	NH ₂ CN		
CS	HNC	HOCO ⁺			
CH ⁺ **	N ₂ H ⁺	C ₃ H			
CN	OCS	H ₃ O ⁺ 2008			
SO	HCO				
SiO	H ₂ S				
CO ⁺ (?)	SO ₂				
NO	HOC ⁺				
NS	C ₂ S				

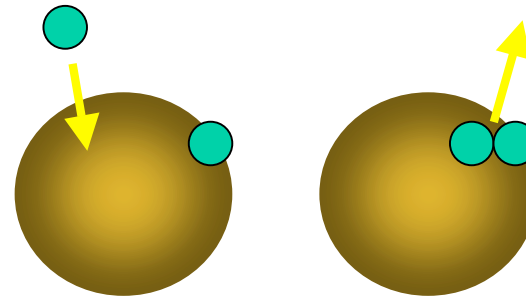
Lee et al. (1996), $n = 10^4 \text{ cm}^{-3}$, $T = 10 \text{ K}$



Astrochemistry. I.

- **Formation of H_2** (Gould & Salpeter 1963; Hollenbach & Salpeter 1970; Pirronello et al. 1999; Katz et al. 1999; Cazaux & Tielens 2002; Habart et al. 2003)

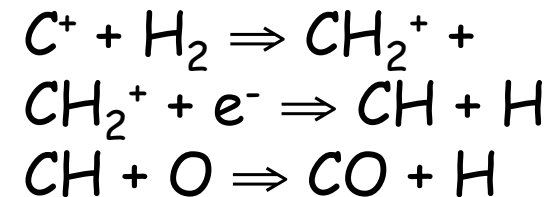
$$R \sim 10^{-17} \text{ cm}^3 \text{ s}^{-1}$$



In gas phase:

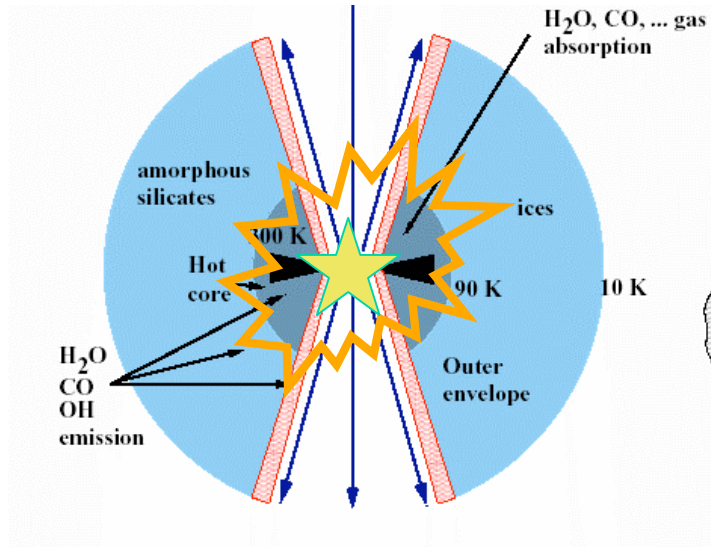


In molecular clouds: ion-neutral reactions

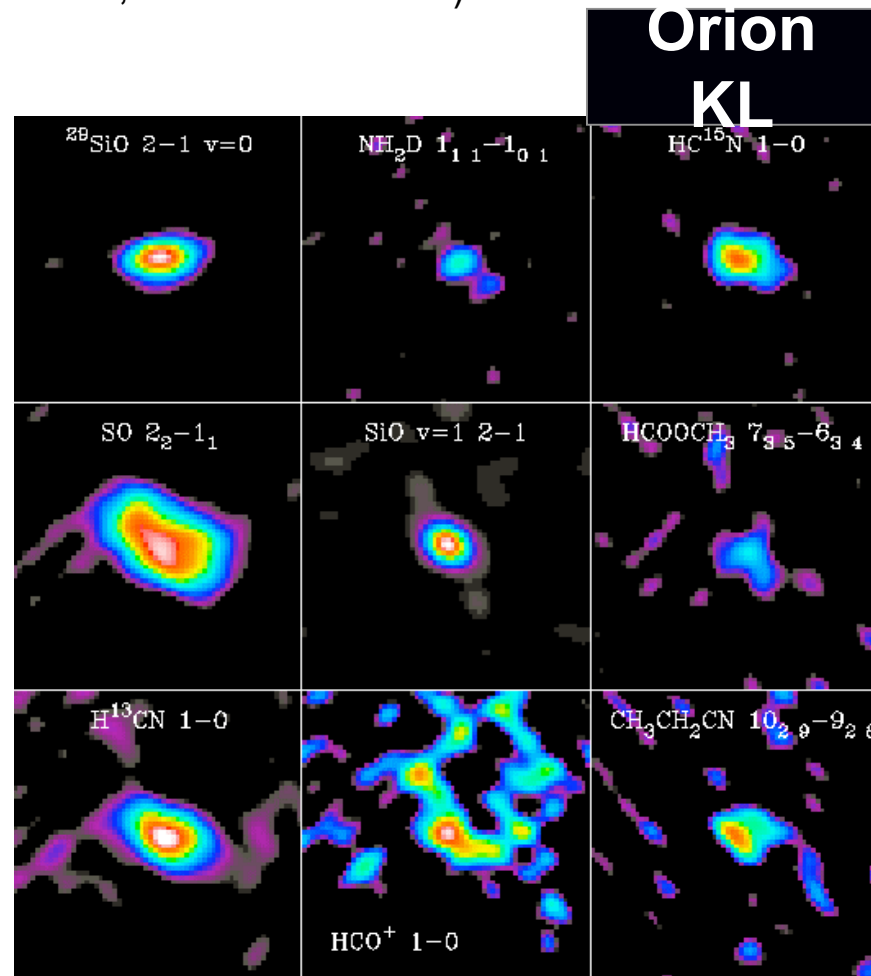


Astrochemistry. II.

- **Complex organic molecules** are easily observed near young stellar objects (e.g. Charnley et al. 1992; Caselli et al. 1993)

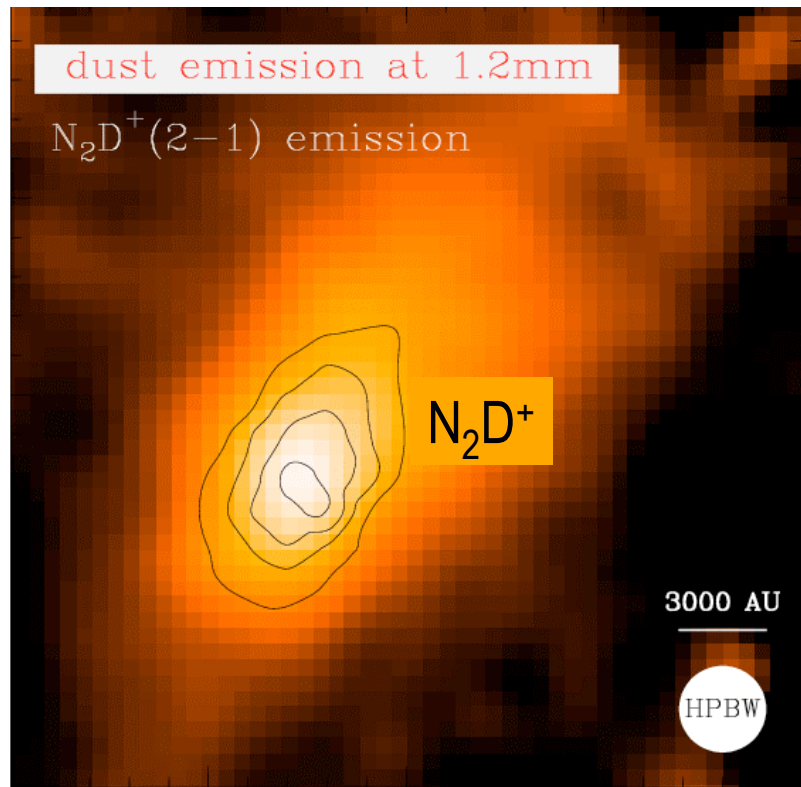


H-rich complex N-bearing and O-bearing molecules:
 CH_3CN , CH_2CHCN ,
 $\text{CH}_3\text{CH}_2\text{CN}$, CH_3OCH_3 ,
 HCOOCH_3 , $\text{C}_2\text{H}_5\text{OH}$..
 (e.g. Blake et al. 1987)



Astrochemistry. III.

- To understand the distribution of the various molecular species to study the physical and kinematical properties of molecular clouds and of star formation.
- Example: CO, typically used to determine the mass of molecular clouds, disappears from the gas phase at densities $n(\text{H}_2) > 10^4 \text{ cm}^{-3}$ and $T < 20 \text{ K}$.



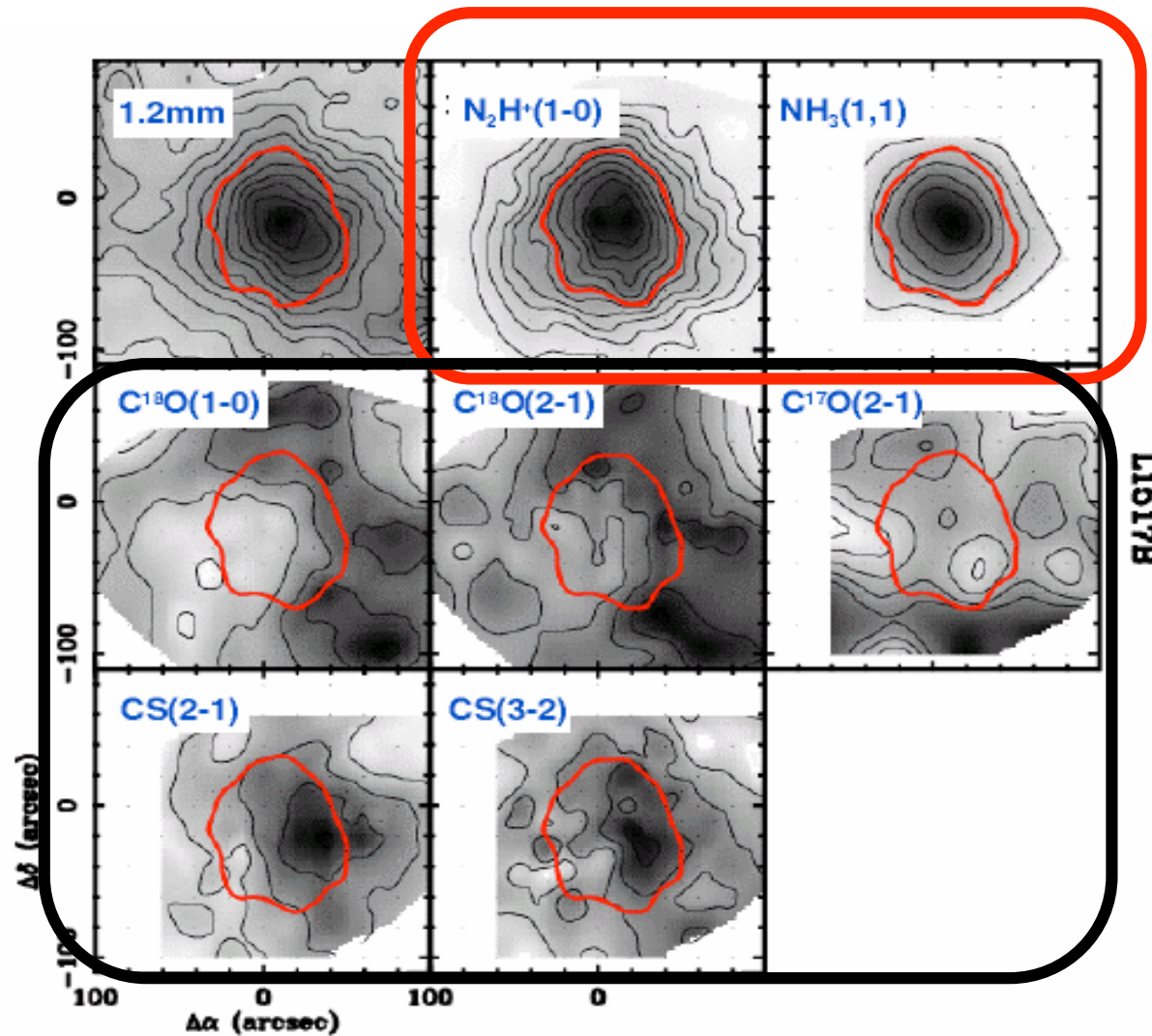
CO disappears
from gas phase
at $R < 7000 \text{ AU}$

N_2 remains in the
gas phase: more
volatile than CO ?

$\text{C}^{17}\text{O}(1-0)$

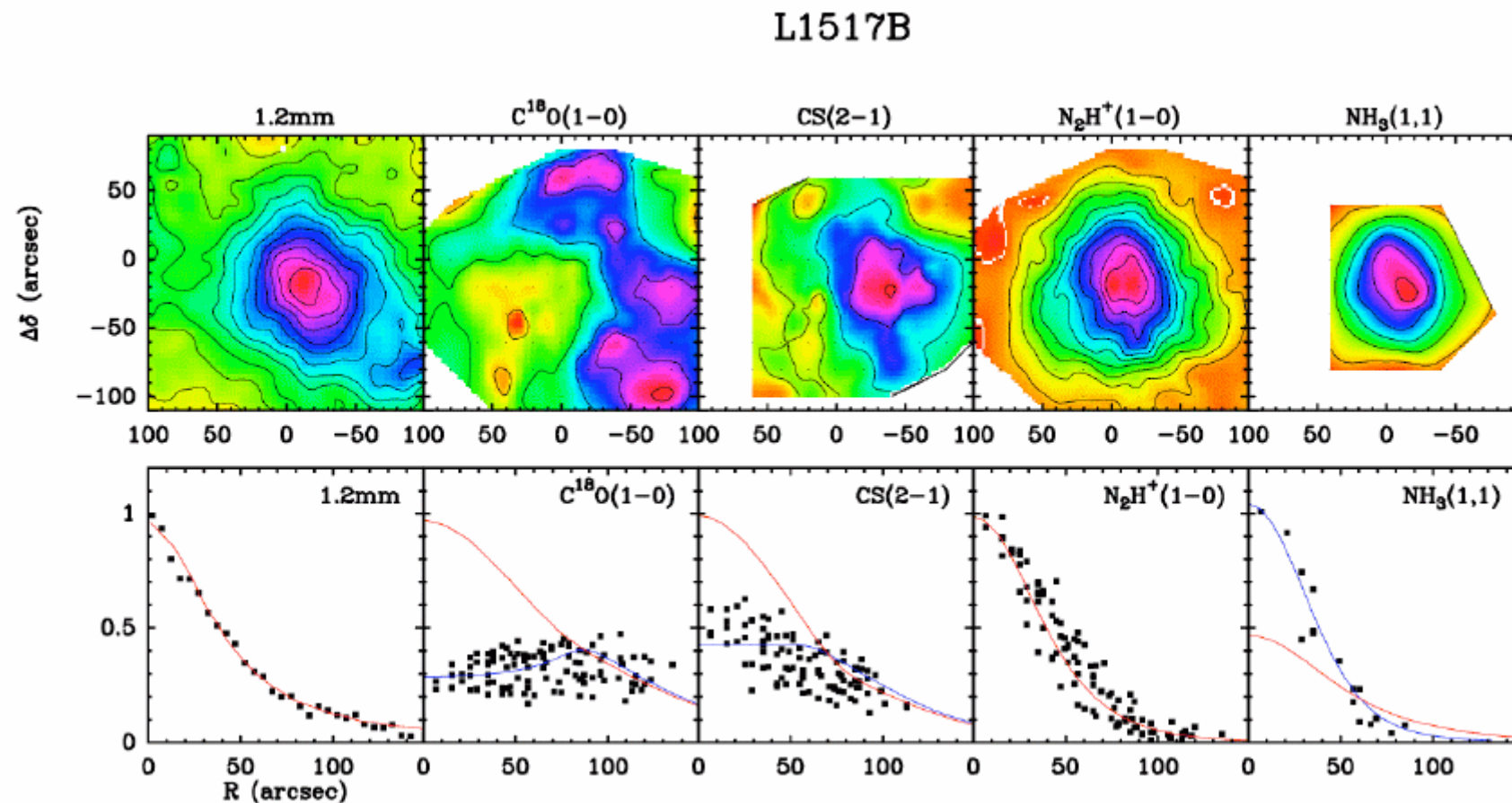
Caselli et al. 1999

L1517B: a low-mass pre-stellar core with depletion

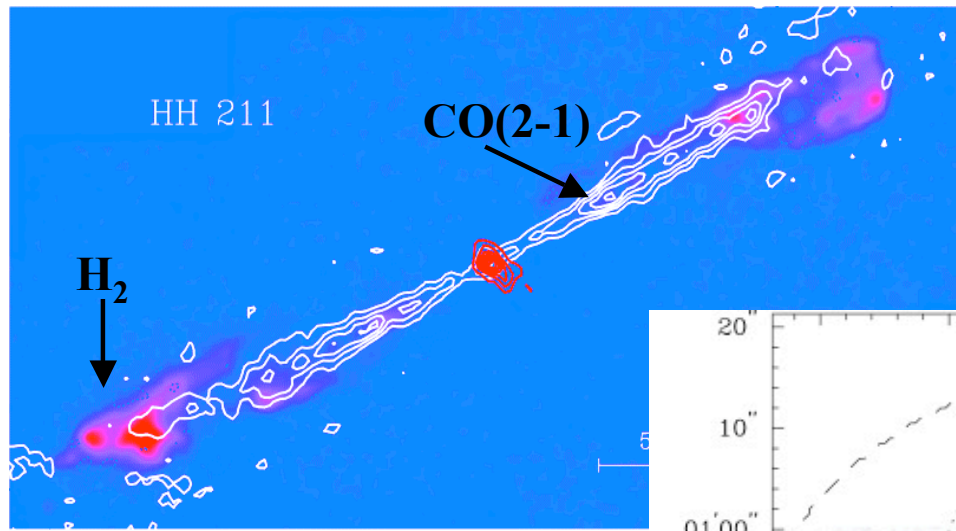


On the other hand,
N-bearing species
well trace the density
profile seen in the dust
continuum emission

C-bearing species
completely miss
the central density
peak



Cores have order-of-magnitude radial CS and CO abundance gradients

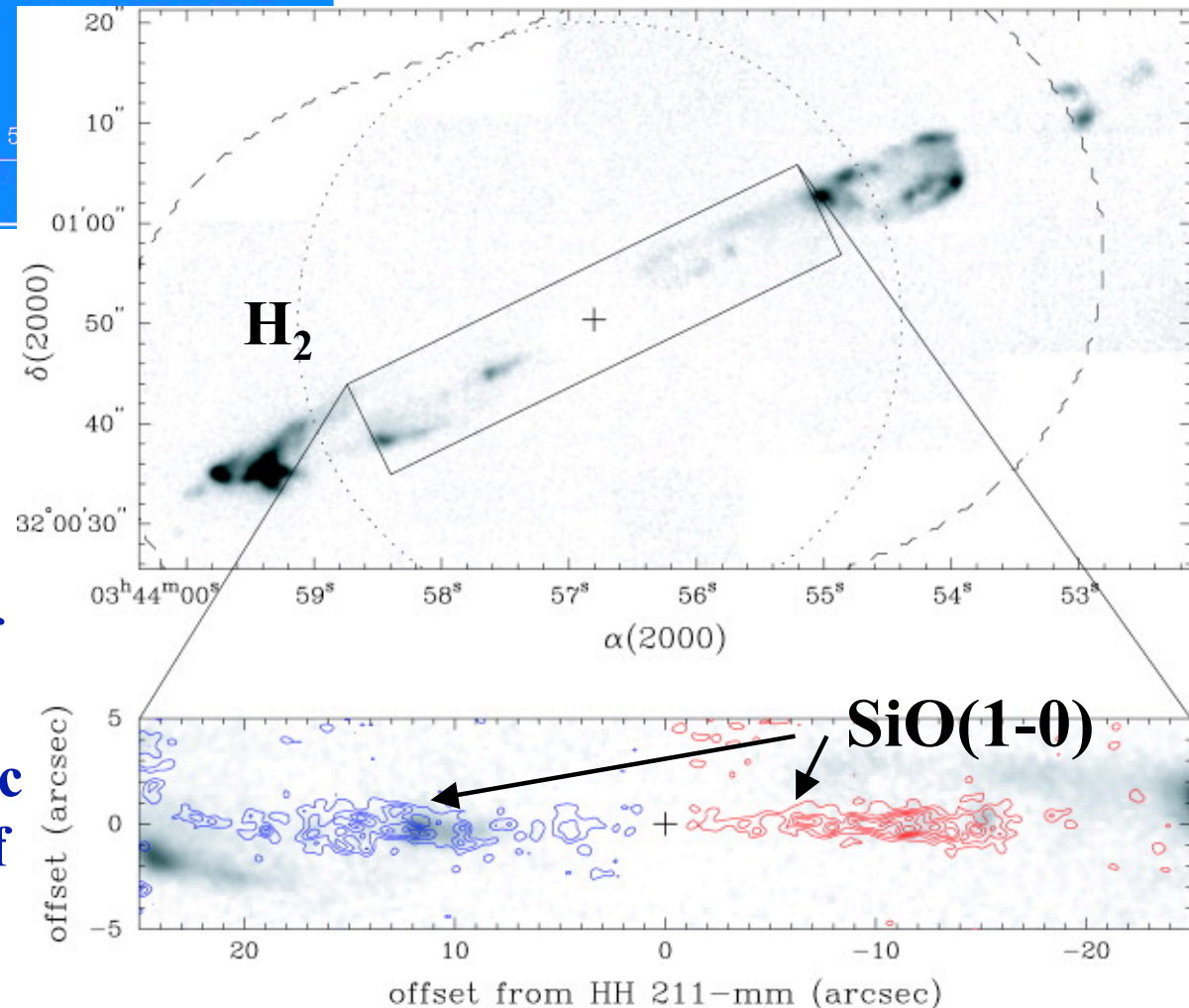


Shock-chemistry!

HH211

Gueth & Guilloteau (1999)

The heating and compression caused by shocks gives rise to dramatic effects in the chemical composition of the surrounding cloud. Dissociation, endothermic reactions, sublimation of ices and disruption of grains lead to a shock-chemistry.



Chandler & Richer (2001)

Chemically rich outflows

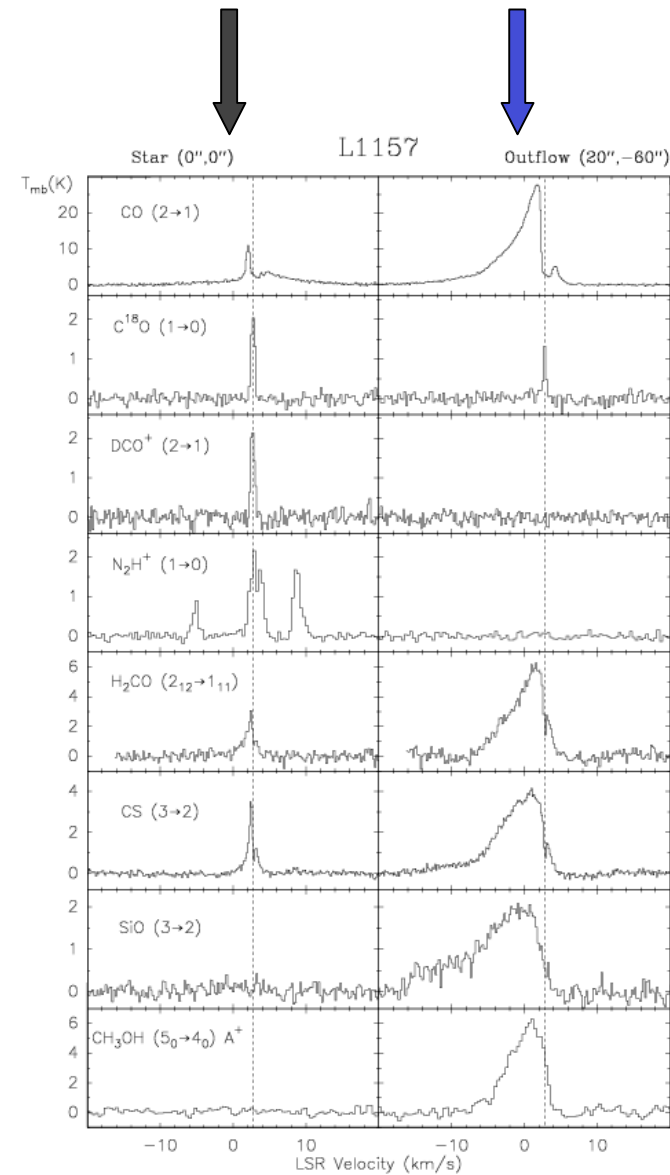
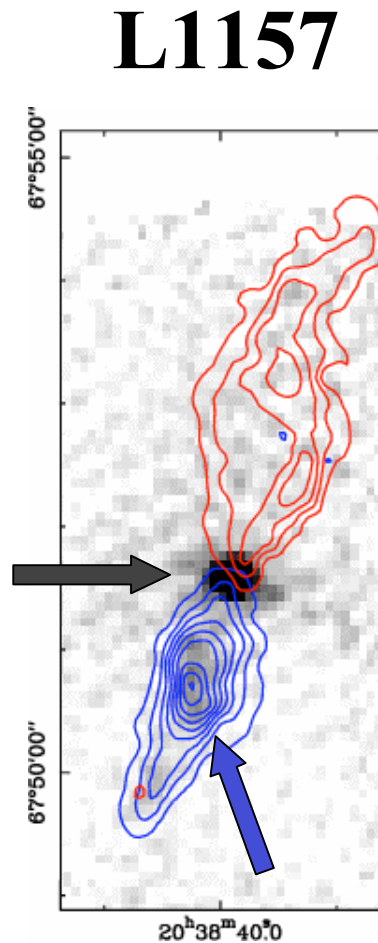
Shock tracers:
 CH_3OH , SiO , H_2O ,
S-bearing species,
 H_2CO

Bachiller & Tafalla
(2000): an empirical
time sequence of low-
mass outflows?

1st stage (Class 0):
jet-like, HV bullets;

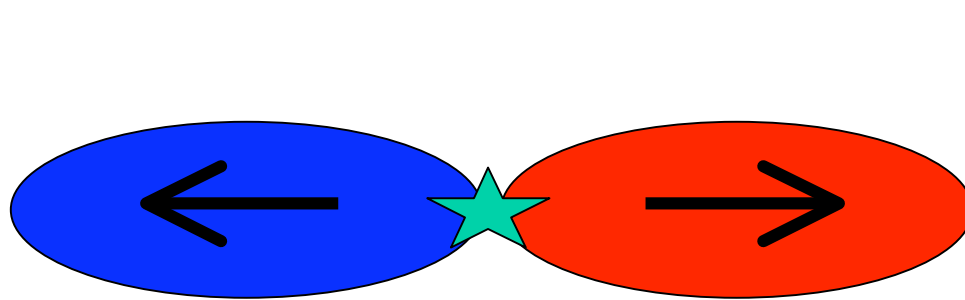
2nd stage (Class 0):
no bullets, rich
chemistry;

3rd stage (Class I):
shell structure,
evacuated cavity.



Bachiller et al. (2001)

Shock-enhanced abundances in outflows



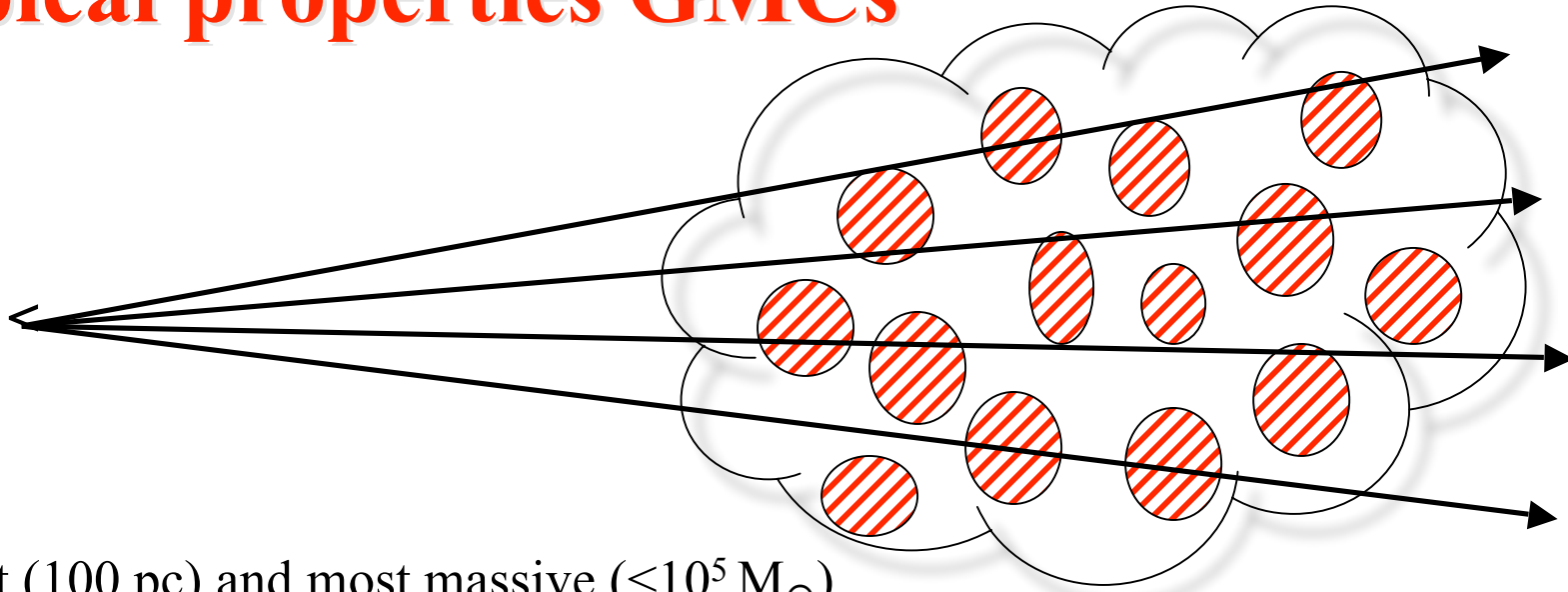
SiO	$10^{-10} - 10^{-6}$
CH ₃ OH	$10^{-7} - 10^{-5}$
NH ₃	$\sim 10^{-6}$
H ₂ CO	$\sim 10^{-7}$
HCN	$\sim 10^{-7}$
SO	$\sim 10^{-7}$

$< 10^{-12}$
$\sim 10^{-9}$
$\sim 10^{-8}$
$\sim 10^{-8}$
$\sim 10^{-8}$
$\sim 5 \times 10^{-9}$

(with respect to H₂)

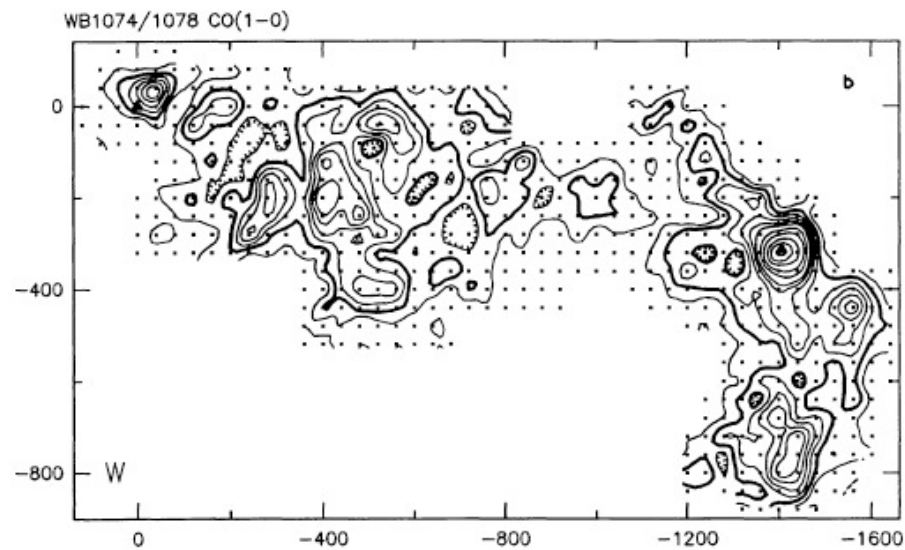
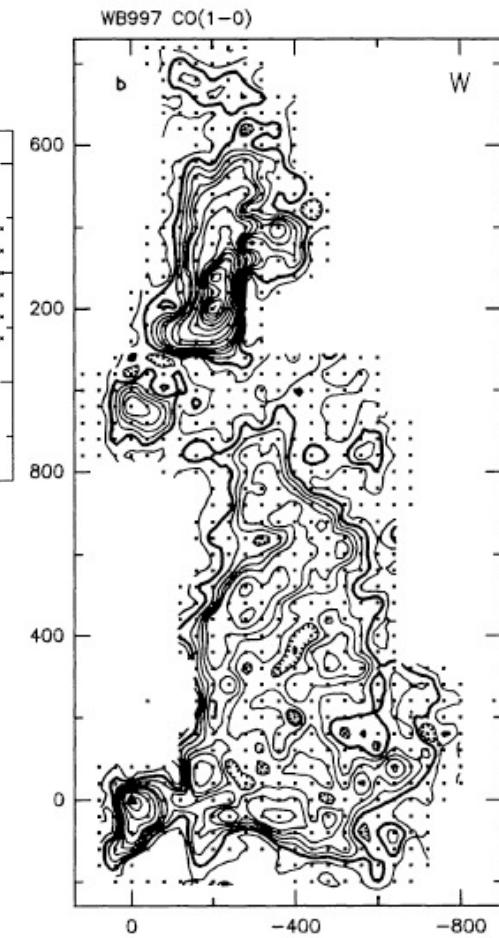
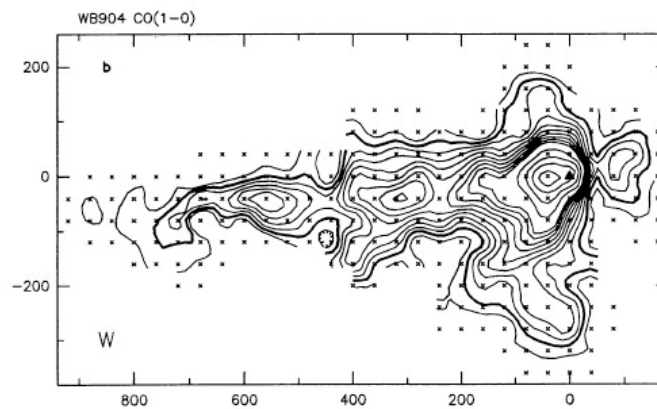
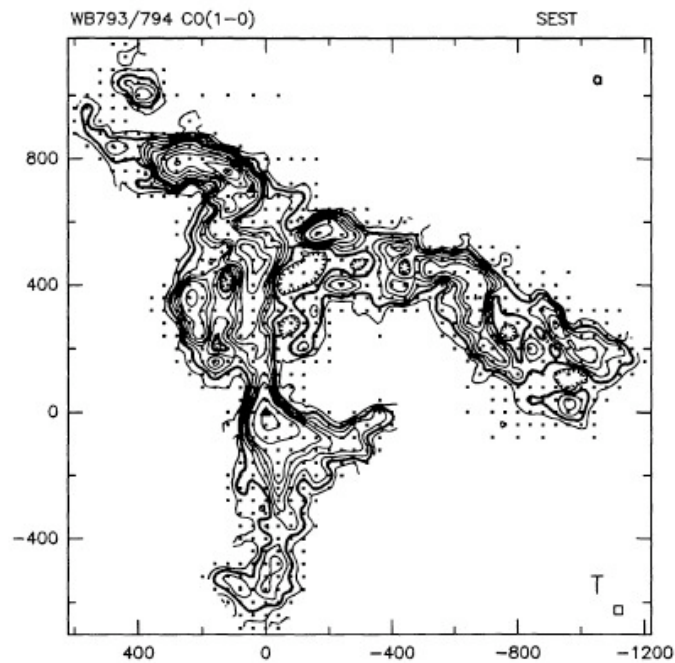
PROPERTIES OF MOLECULAR CLOUDS

Typical properties GMCs



- Largest (100 pc) and most massive ($<10^5 M_{\odot}$) objects in Galaxy
- Not uniform: volume f.f. $\ll 1$
surface f.f. ≈ 1
(≥ 1 clump along the l.o.s.)
- $\Delta V_{\text{obs}} \gg \Delta V_{\text{therm}} \approx (8 \ln 2 \, kT / \mu m_{\text{H}})^{0.5}$
line profile determined by velocity field of clumps: bulk motions.
- Gravitationally bound
 $P_{\text{int}}/k \sim 10^5 \text{ Kcm}^{-3} \gg$
 $< P_{\text{ism}}/k > \sim 10^4 \text{ Kcm}^{-3}$
- All OB stars form in GMCs
- Strong confinement to spiral arms
(contrast arm-interarm $> 28:1$)
- $\Delta V(\text{cloud-cloud}) \approx 3\text{--}9 \text{ km/s}$ (median 4.2)
 $\neq f(M) \neq f(R)$
- GMCs are young ($< \text{few } 10^7 \text{ yr}$)
- Material stays locked up in stars:
replenishment needed
(SFR $\sim 2\text{--}4 M_{\odot}/\text{yr}$, return $\sim 0.8 M_{\odot}/\text{yr}$)

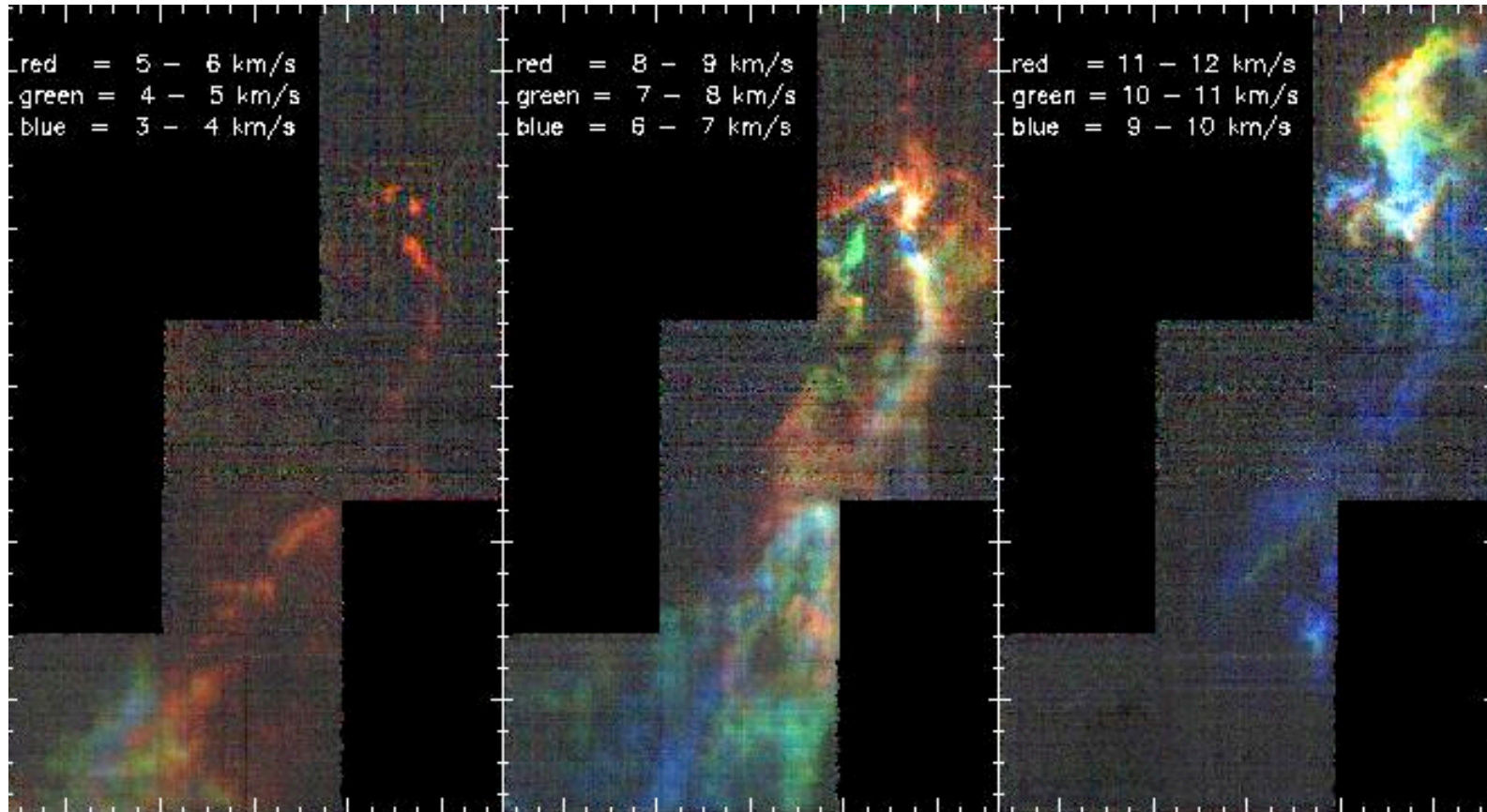
Molecular clouds: elongated



Brand & Wouterloot 1994

Orion A

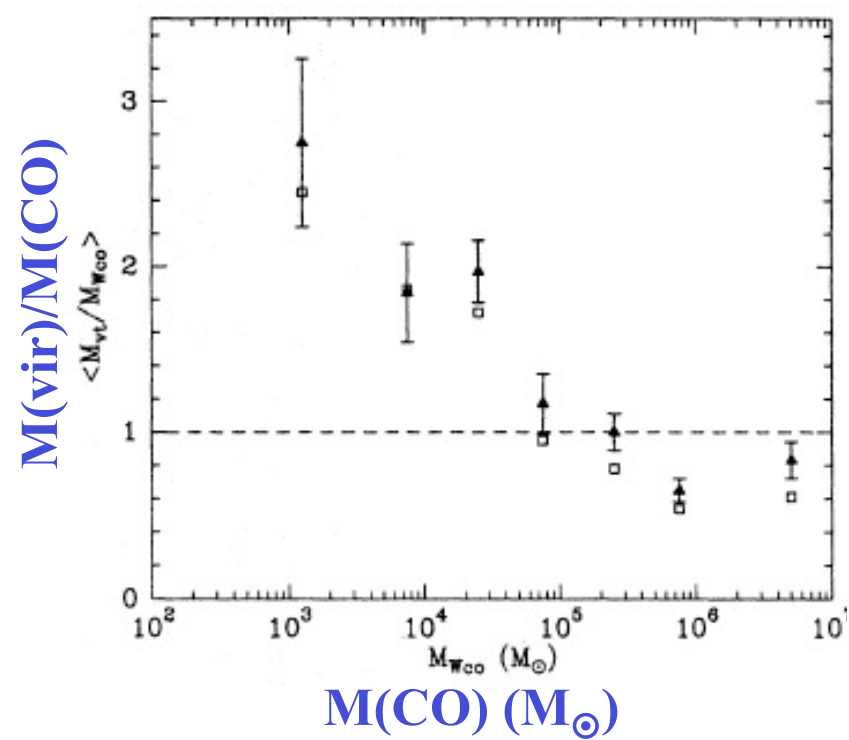
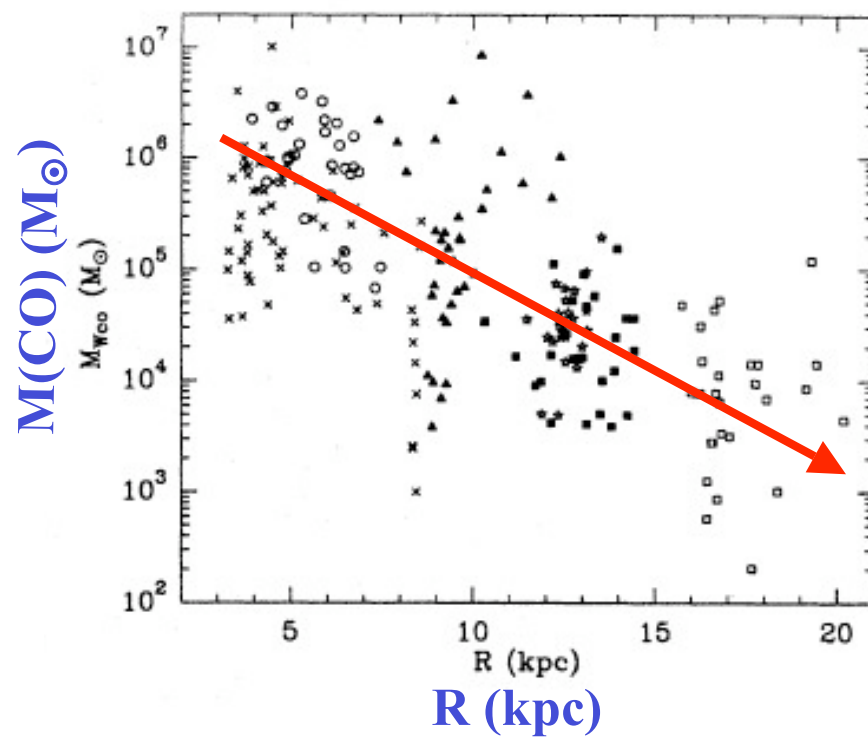
^{13}CO 220 GHz = 1.3 mm



Sheets and filaments

J. Bally (IAU227)

Masses and mass-ratios



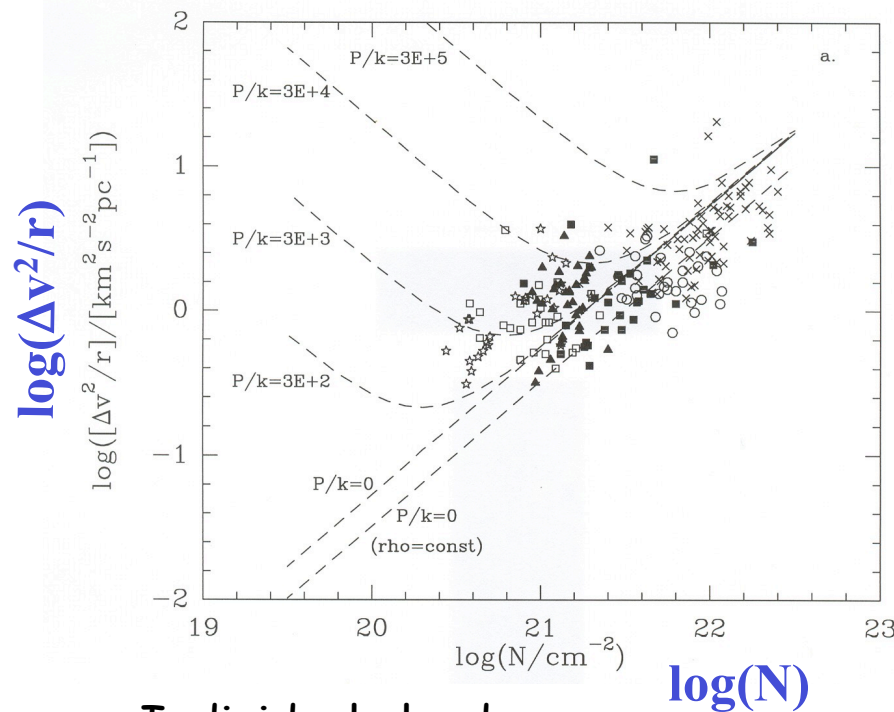
Brand & Wouterloot 1995

Molecular clouds – virial- and pressure equilibrium

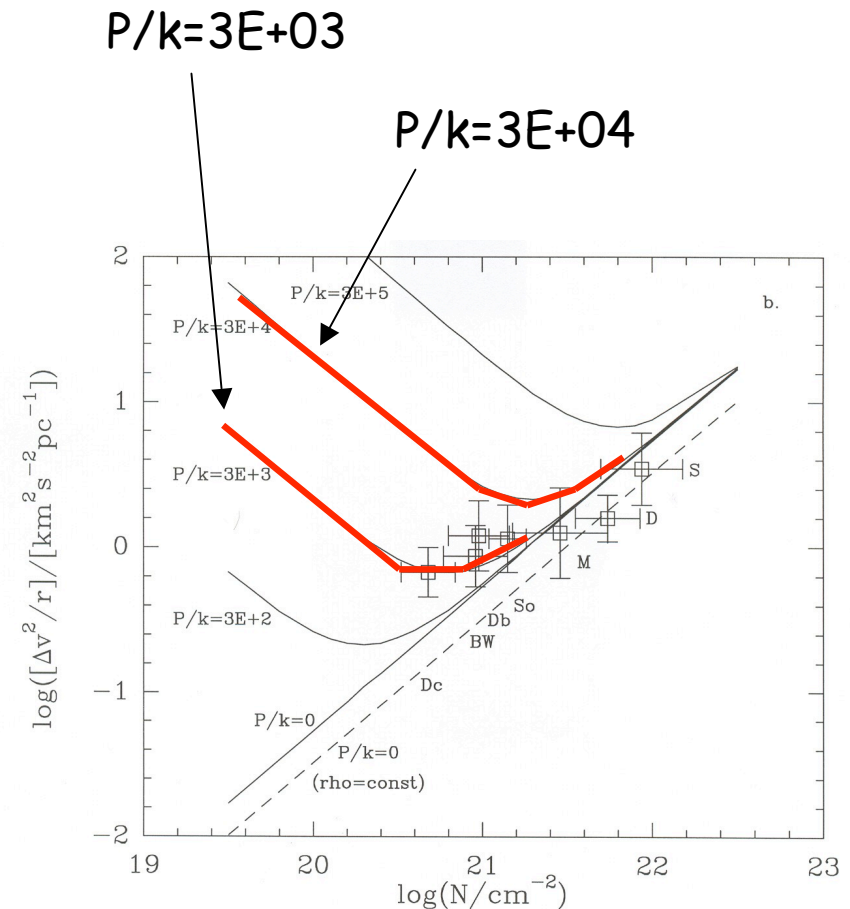
$$4\pi r^3 P_{\text{ext}} = M(\sigma_{3D})^2 - \frac{3}{5} \frac{GM^2}{r} \quad \Rightarrow \quad \frac{\Delta v^2}{r} = \frac{[fac1 * P_{\text{ext}} / k + fac2 * N(H_2)^2]}{[fac3 * N(H_2)]}$$

P_{ext} dominates: $\frac{\Delta v^2}{r} \propto N(H_2)^{-1}$

Self-grav. dominates: $\frac{\Delta v^2}{r} \propto N(H_2)$



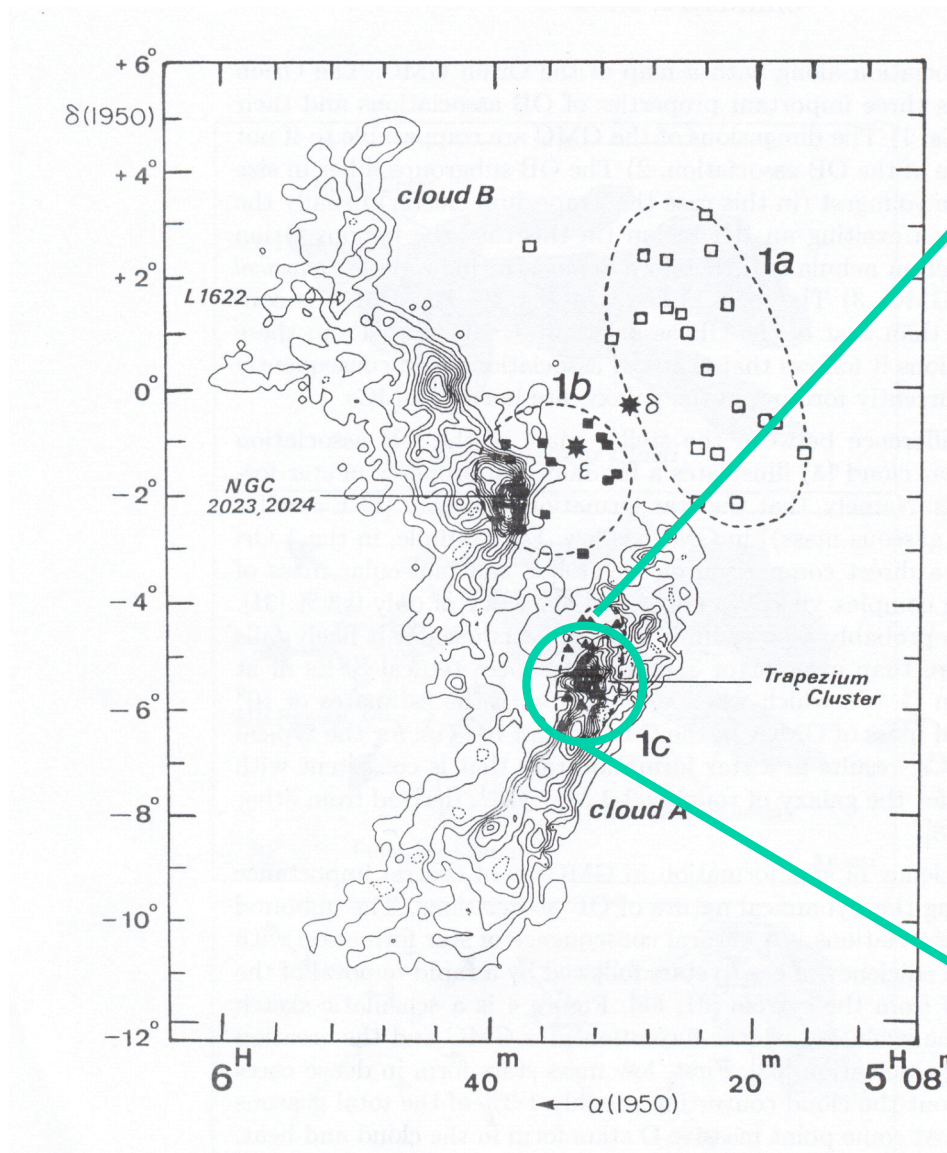
Individual clouds



Sample averages

Brand & Wouterloot 1995

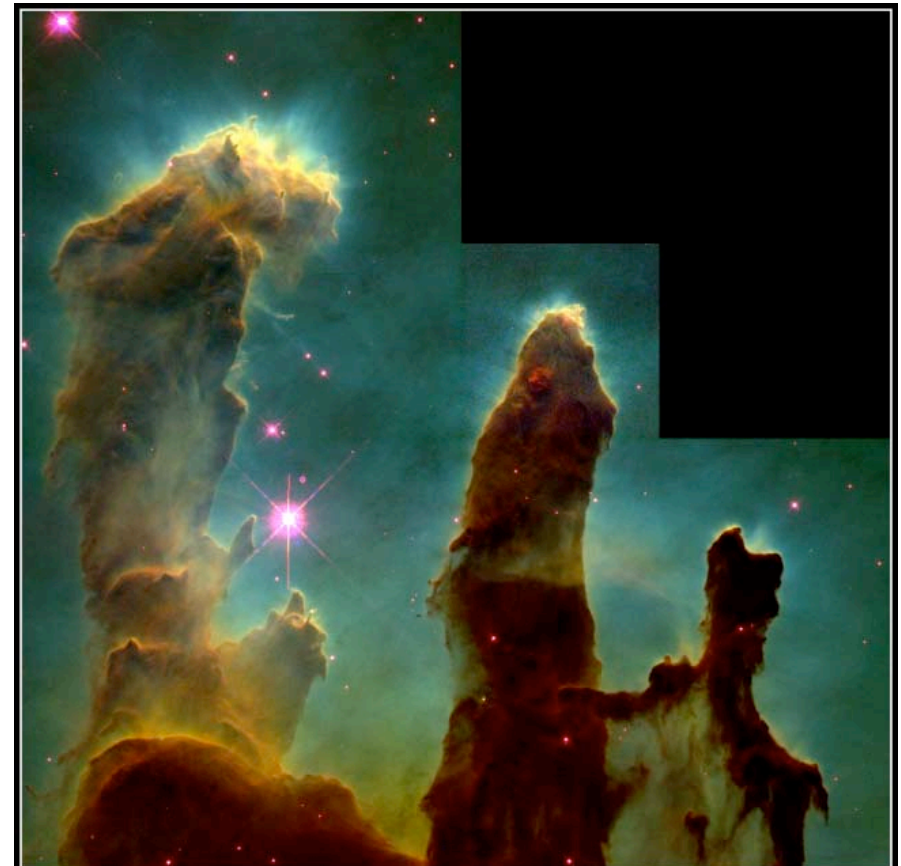
Molecular clouds & star formation



Molecular clouds & star formation



HST: NGC3603



Gaseous Pillars • M16

HST • WFPC2

PRC95-44a • ST ScI OPO • November 2, 1995
J. Hester and P. Scowen (AZ State Univ.), NASA

Star formation sites in outer Galaxy

Projected distribution
WB89-clouds

Wouterloot & Brand
1989 A&AS 80, 149
(WB89)

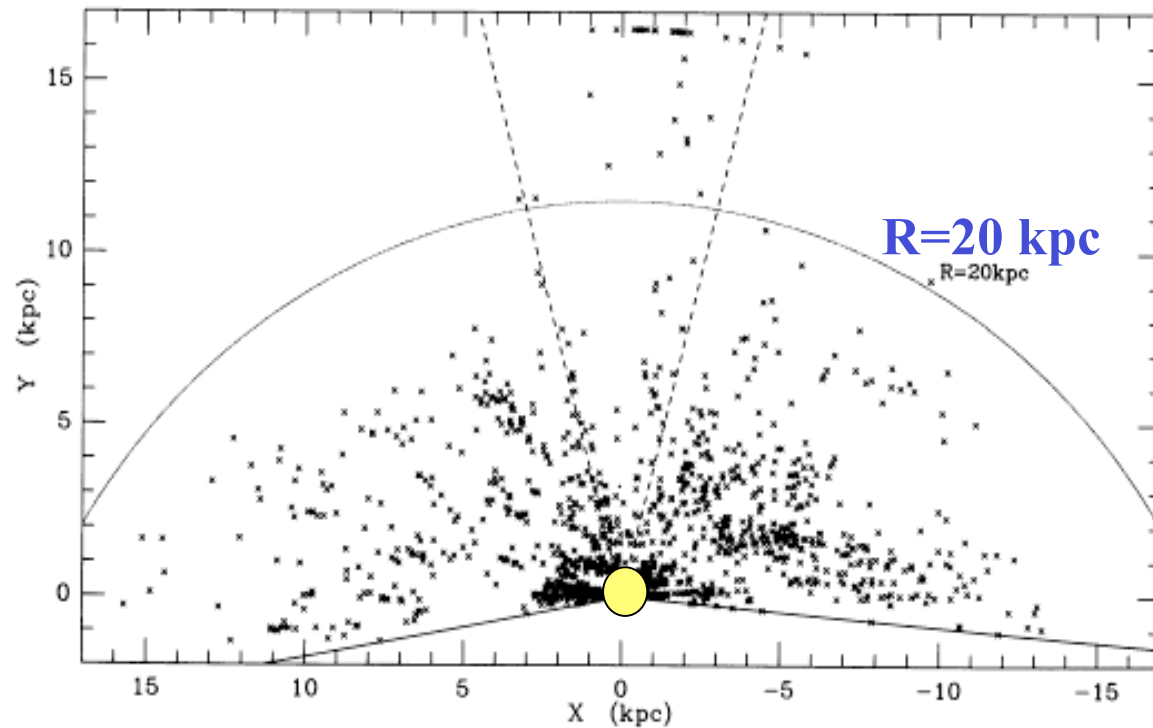
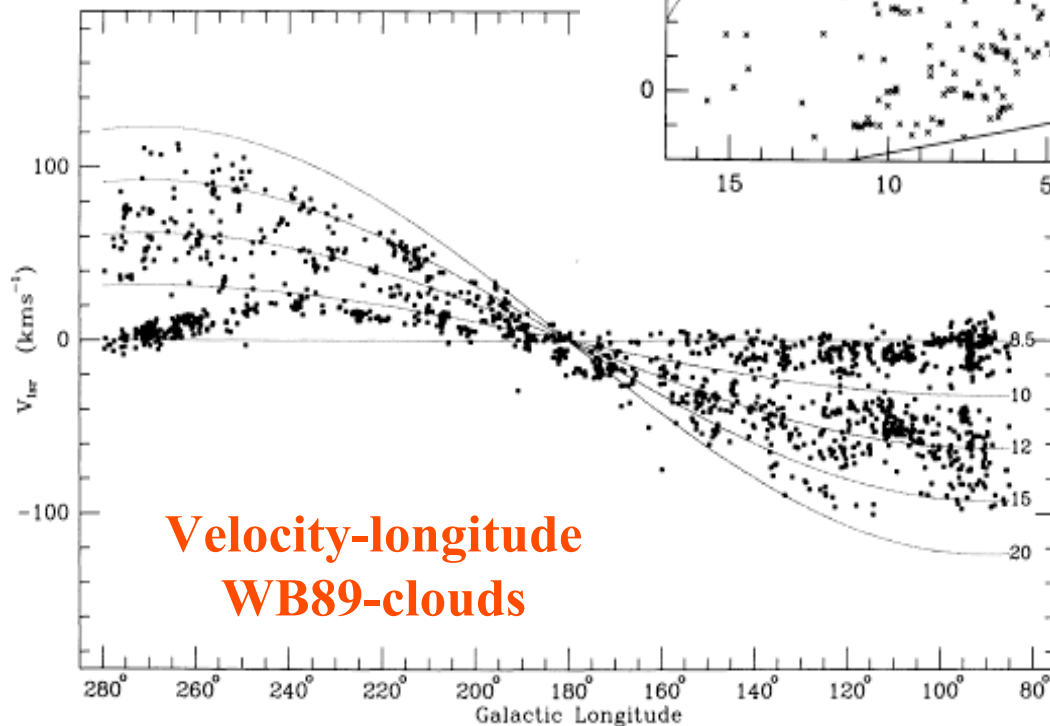
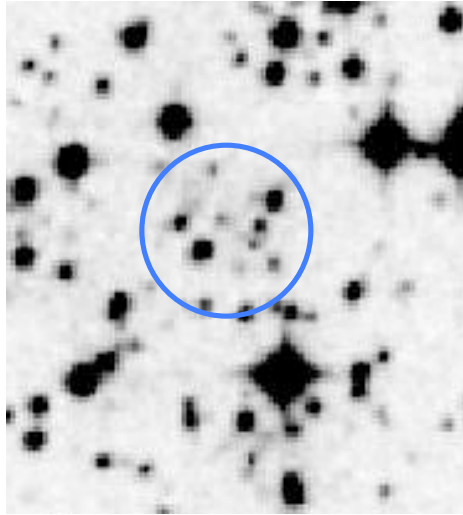
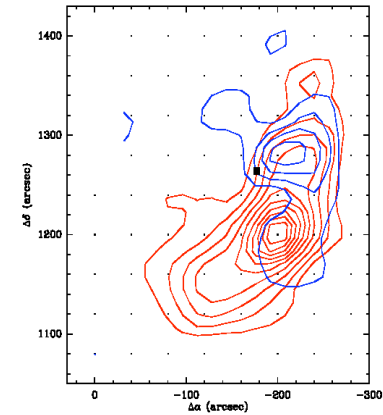


Fig. Distribution of IRAS sources with colours of star-forming regions; shows there IS star formation out to the edge of the galactic molecular disk.

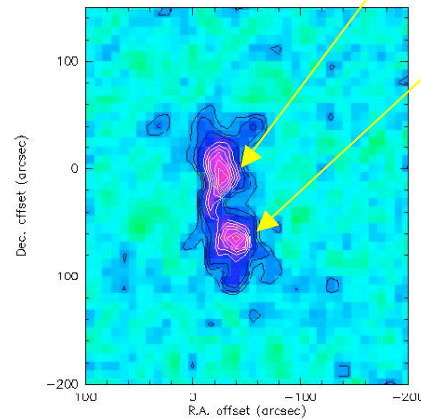
Embedded clusters I



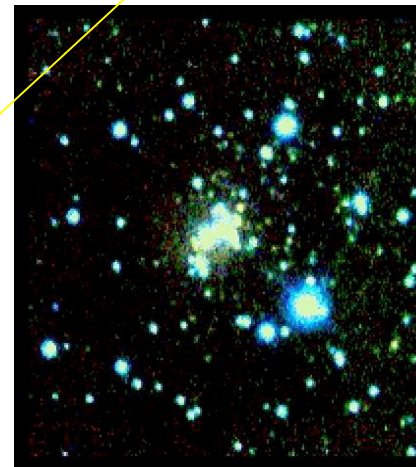
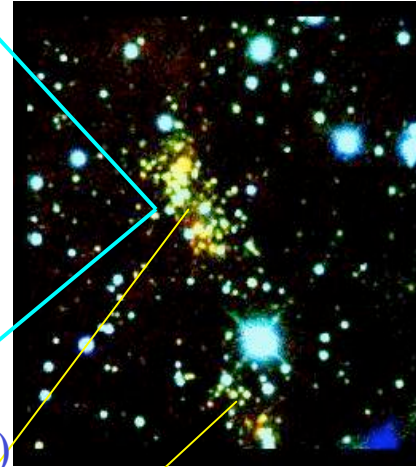
DSS-optical



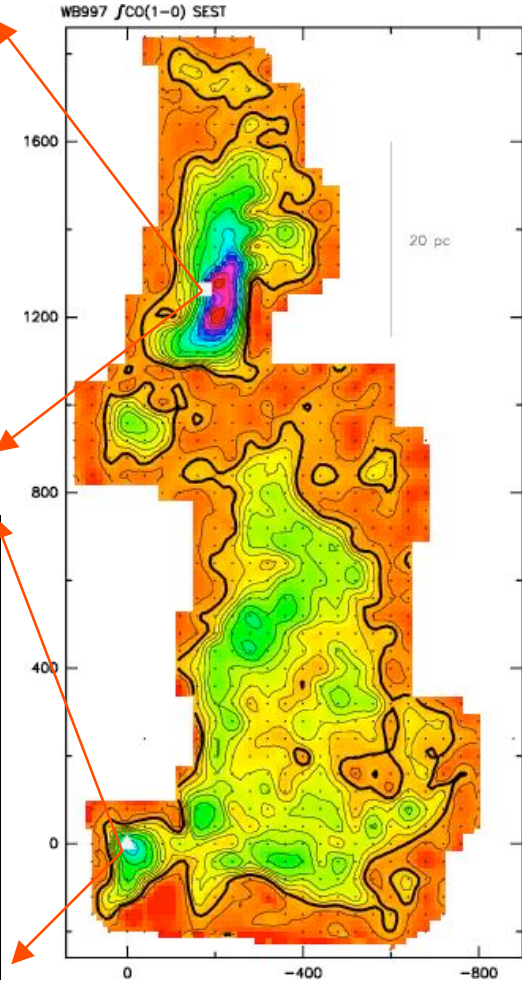
Outflow in $^{12}\text{CO}(1-0)$
(SEST)



1.2 mm continuum
(SEST/SIMBA)



JHK-composite
 $\sim 1'.7 \times 1'.7$



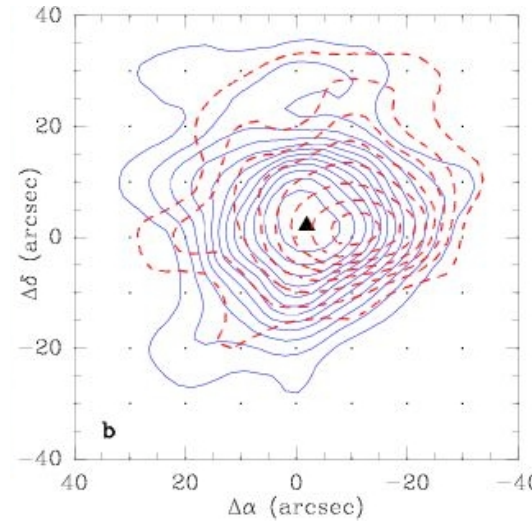
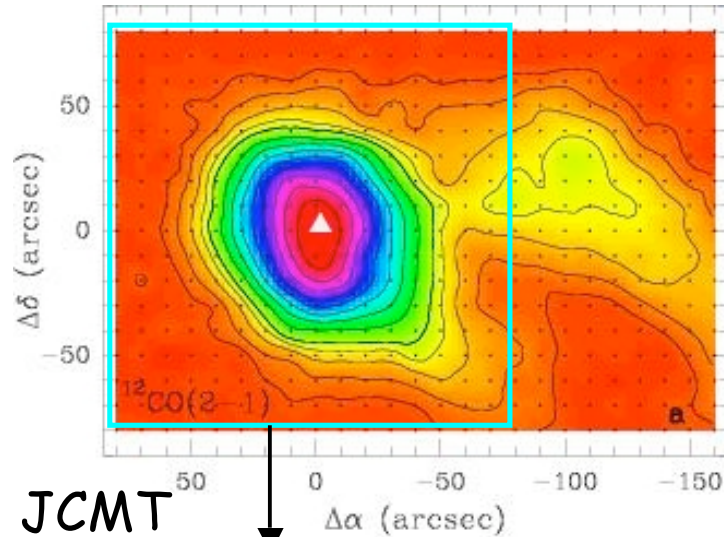
Cloud: $M = 6.0 \times 10^4 M_{\odot}$
 $d, R = 9.3, 15.7 \text{ kpc}$

IRAS07255-2012
IRAS07257-2033

Brand & Wouterloot 2003 & in prep.

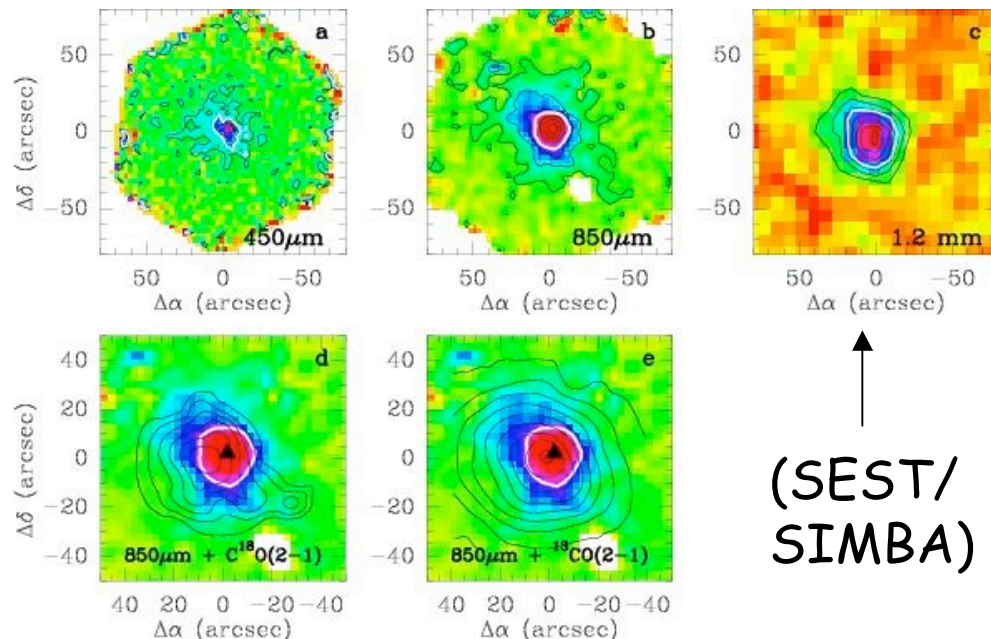
Embedded clusters II

Brand & Wouterloot, A&A 2007



Δ : dust core

White contour: half of the peak value



(SEST/
SIMBA)

$R, d = 20.2, 11.9$ kpc

$M_{\text{cloud}} \approx 5 \times 10^3 M_{\odot}$ (CO);

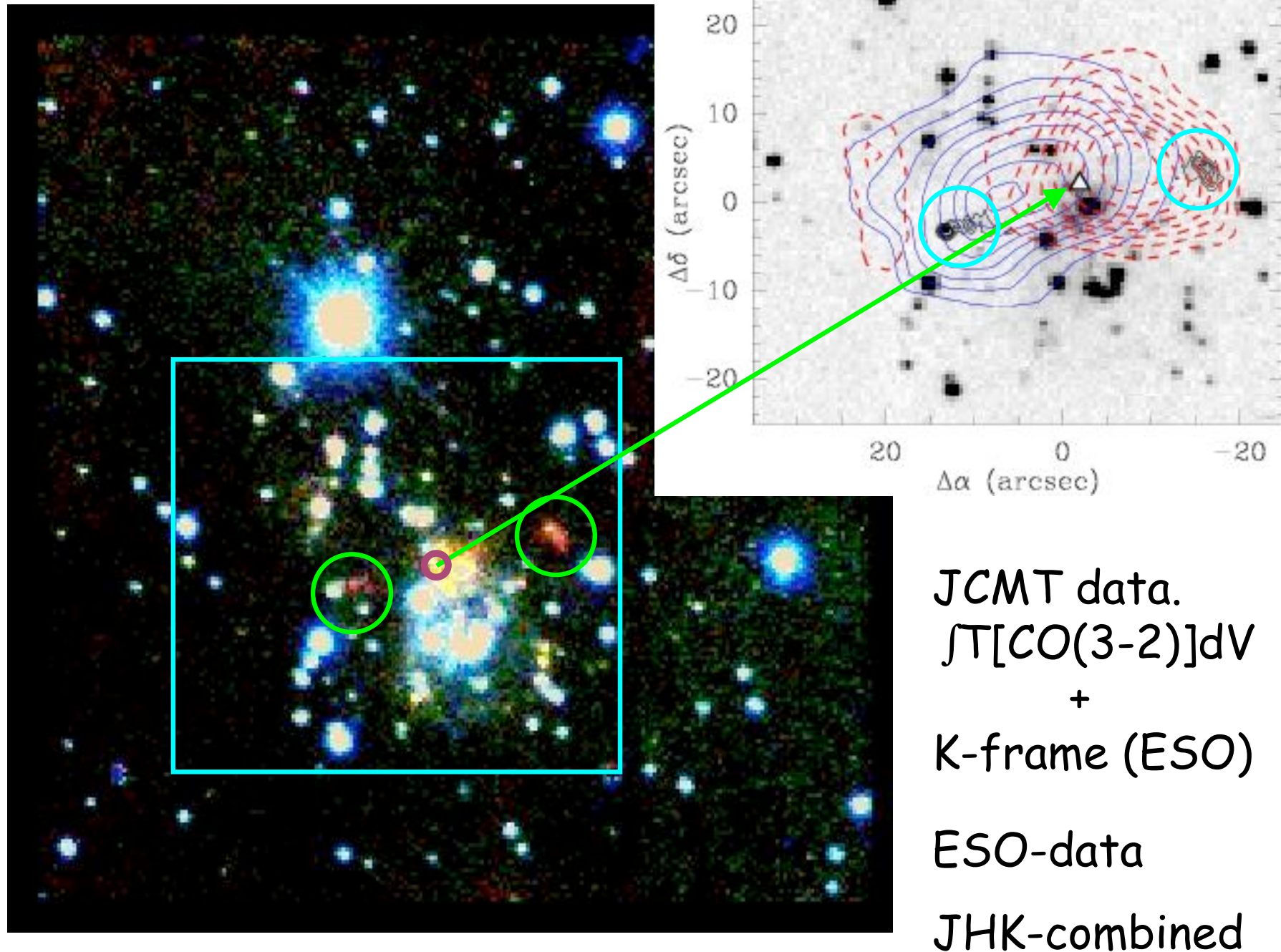
$M_{\text{vir}}(\text{core}) \approx 400 M_{\odot}$ (CS);

$M_{\text{dust}} \approx 10 M_{\odot}$ (SED-fit;

$T_{\text{dust}} \approx 22$ K).

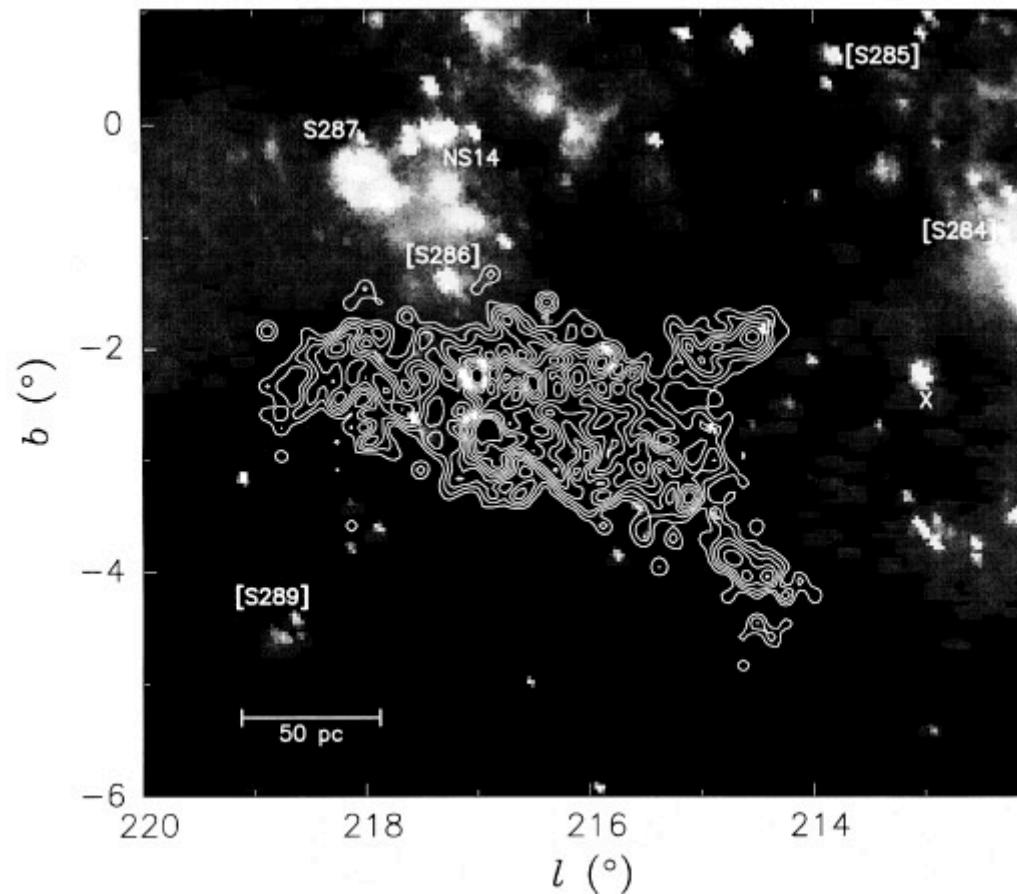
$M_{\text{outflow}} \approx 12 M_{\odot}$ (CO);

$t_{\text{dyn}} \approx 4 \times 10^4$ yrs.



A cloud without star formation

G216-2.5: “Maddalena’s Cloud”



$$L_{\text{IR}}/M_{\text{cloud}} < 0.07 L_{\odot}/M_{\odot}$$

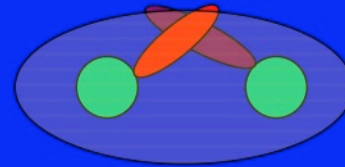
while typically

$$L_{\text{IR}}/M_{\text{cloud}} \sim 1 L_{\odot}/M_{\odot}$$

DERIVING FUNDAMENTAL PROPERTIES

Typical energies involved in molecular transitions

- Electronic transitions



- Vibrational transitions

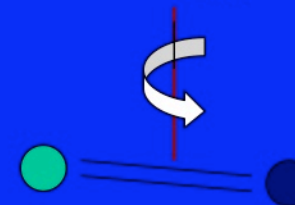


stretching



bending

- Rotational transitions

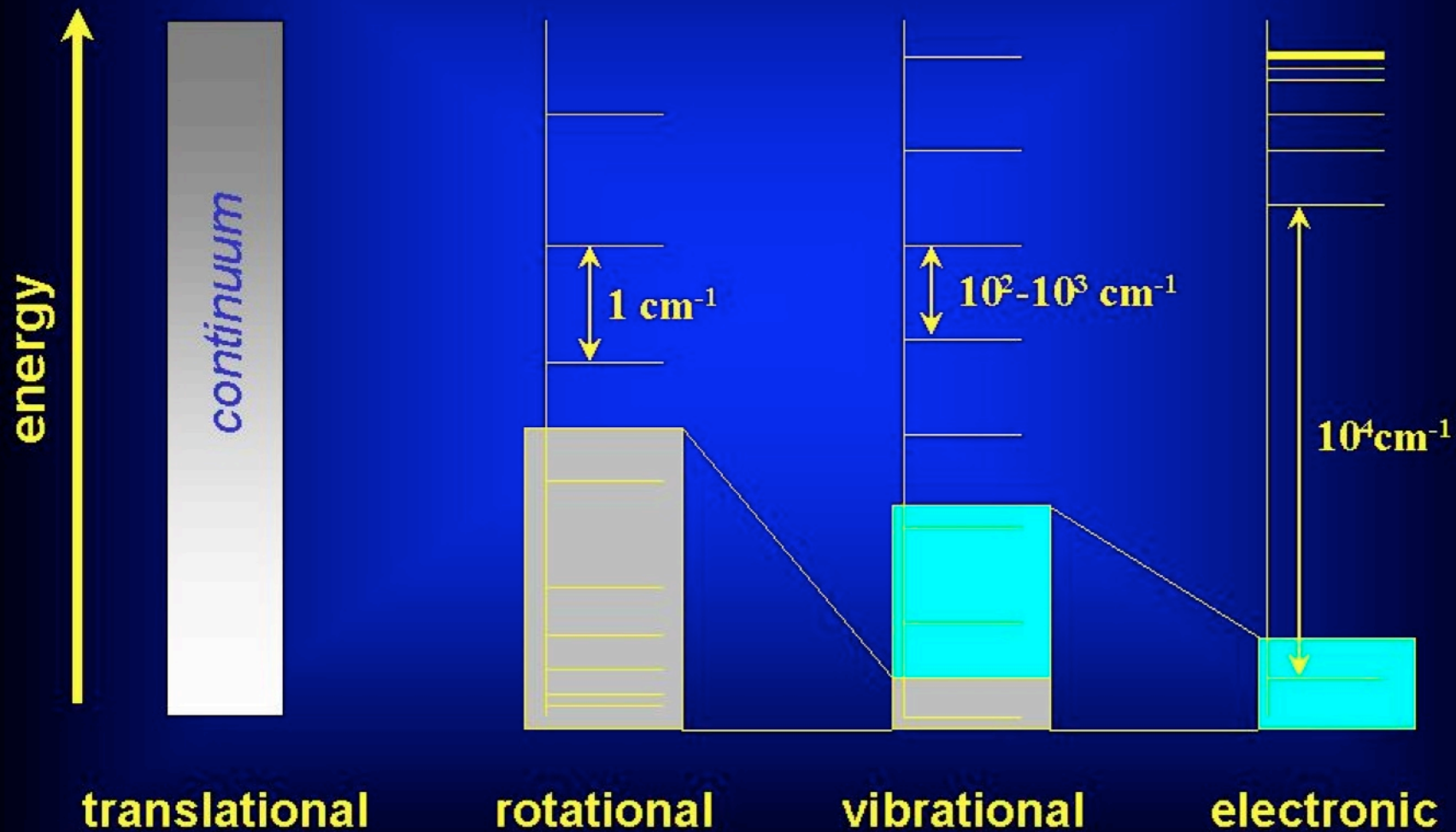


- Electronic/nuclear Spin interactions

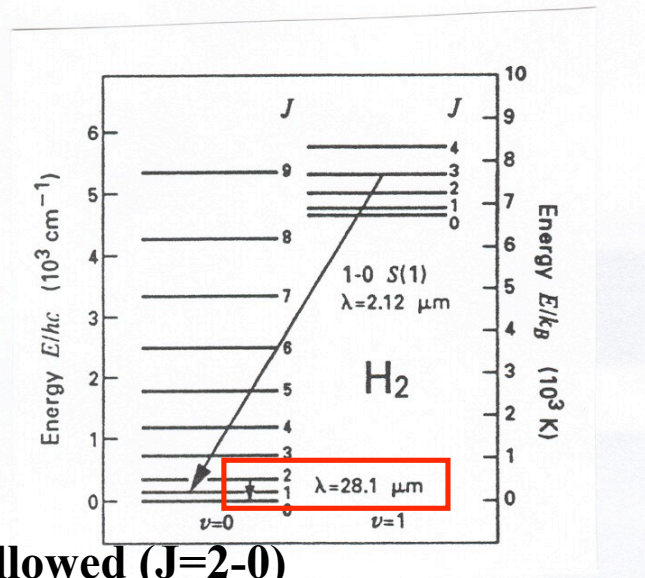


energy level separations

low-energy rotational transitions of small molecules lie at mm wavelength



Observing molecular clouds at large



Lowest allowed ($J=2-0$)

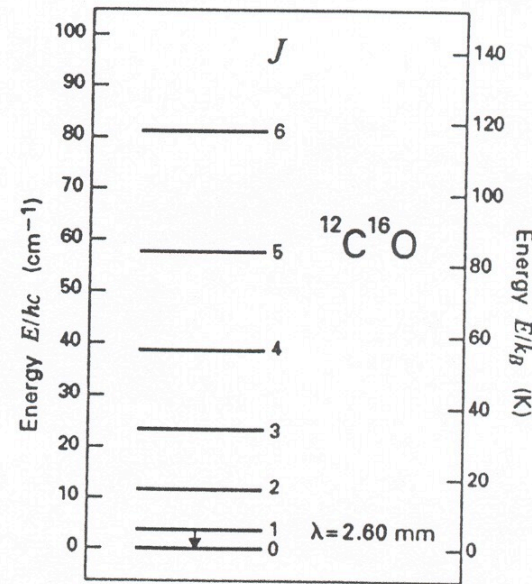
$\Delta E = 510 \text{ K}$

H_2 smallest diatomic molecule: widely-spaced energy levels

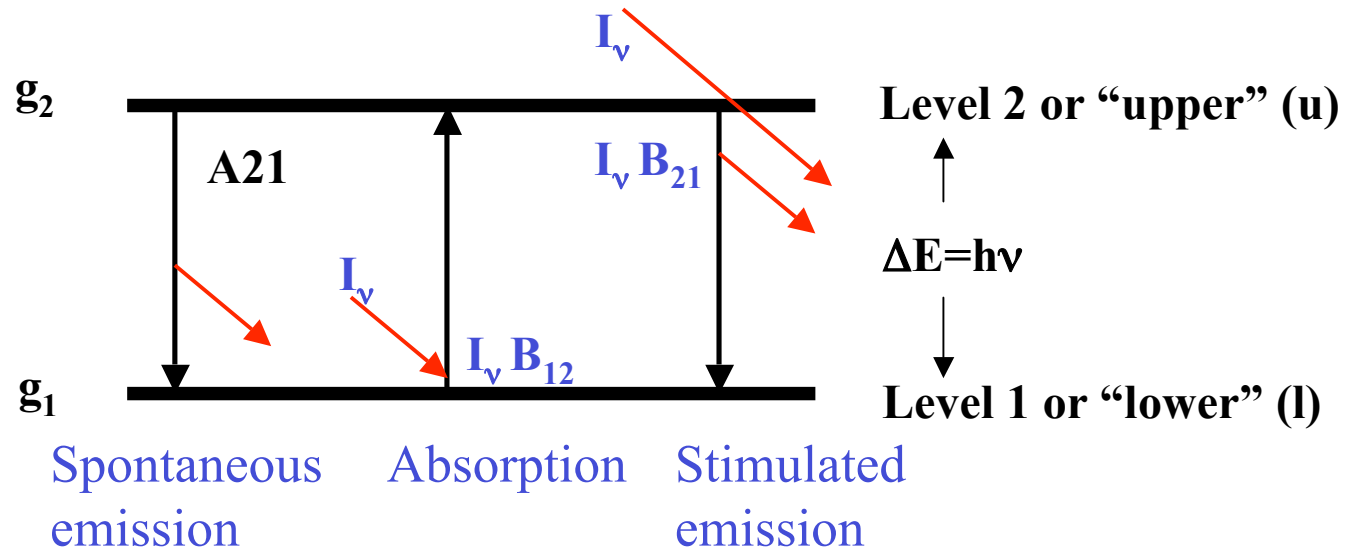
Even lowest excited rot. levels too far above ground state to be easily populated at normal molecular cloud T.

no dipole moment, hence quadrupole radiation (slow)

CO: more closely-spaced energy levels; easily populated also at low T



Two-level system



$$g_1 B_{12} = g_2 B_{21} ; A_{21} = (2h\nu^3/c^2) B_{21}$$

$$n_2/n_1 = (g_2/g_1) \exp(-\Delta E/kT_{ex})$$

Boltzmann equation

Statistical equilibrium: in=out, regardless of process:

$$dn_1/dt = (A_{21} + IB_{21} + C_{21})n_2 - (IB_{12} + C_{12})n_1 = 0 \text{ for each level}$$

Example: CO. In molecular cloud, excitation J=1 level through collisions with H₂.

If n_{tot} low, each upward transition followed by spontaneous emission of photon (rate = $n_1 A_{10}$).

If n_{tot} high, excited CO loses energy in collisions with H₂, without emission photon. Two regimes are separated at critical density $A_{10}/\gamma_{10} = 3 \times 10^3 \text{ cm}^{-3}$.

$$n_1/n_0 = (g_1/g_0) \exp(-\Delta E/kT_{\text{ex}})$$

$n_{\text{tot}} \ll n_{\text{crit}}$: n_1/n_0 small and $\propto n_{\text{tot}}$, $T_{\text{ex}} < T_{\text{kin}}$

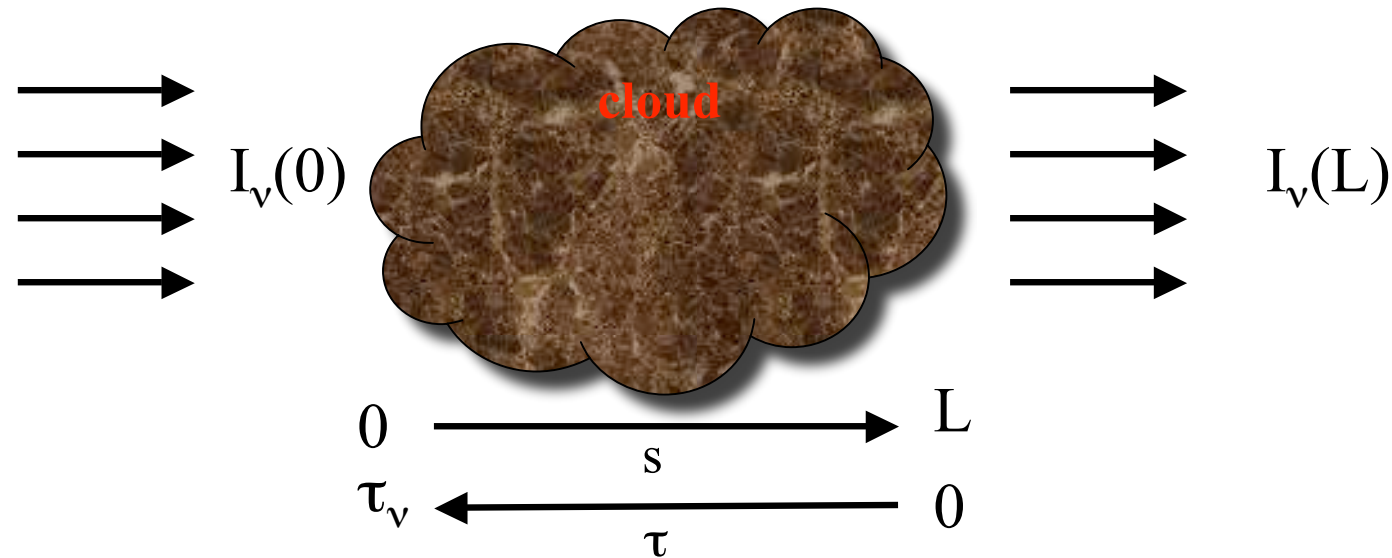
$n_{\text{tot}} \gg n_{\text{crit}}$: CO in LTE and $T_{\text{ex}} = T_{\text{kin}}$

NH₃(1,1) $n_{\text{crit}} = 1.9 \times 10^4 \text{ cm}^{-3}$.

CS $n_{\text{crit}} = 4.2 \times 10^5 \text{ cm}^{-3}$.

H₂O (thermal emission) $n_{\text{crit}} = 1.7 \times 10^7 \text{ cm}^{-3}$.

Radiation transport I



$$dI_v = -k_v I_v ds + j_v ds$$

$$d\tau_v \equiv -k_v ds$$

$$dI_v = I_v d\tau_v + (j_v / k_v) d\tau_v \quad (j_v / k_v) = \text{source function } S_v$$

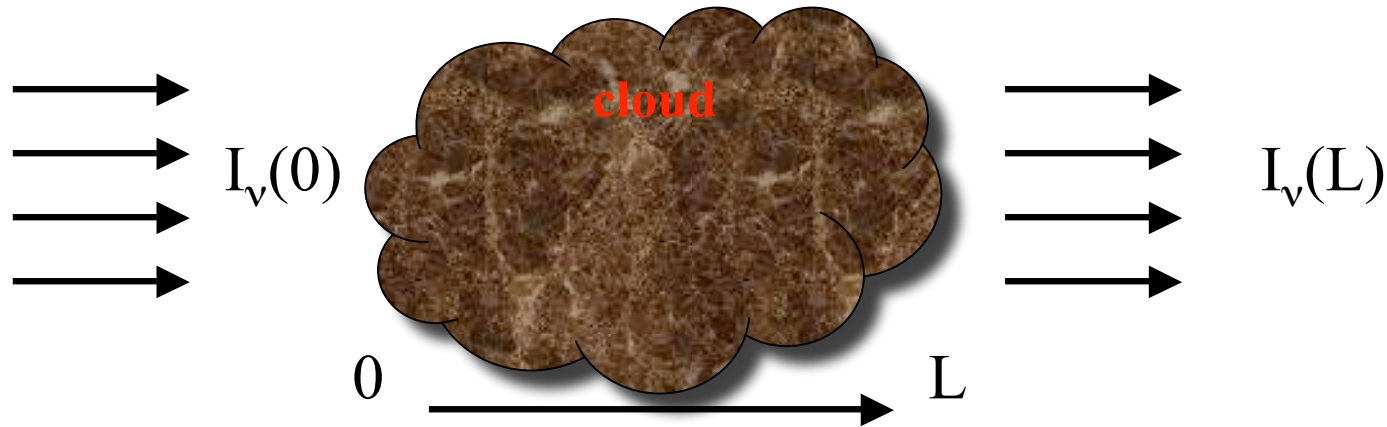
$$j_v = (h\nu/4\pi)n_u A_{ul}\phi(\nu)$$

$$k_v = (h\nu/4\pi)(n_l B_{lu} - n_u B_{ul})\phi(\nu)$$

TE at temperature T : $S_v = B_v(T_{\text{ex}})$: [Planck function](#). Then:

$$I_v = I_v(0)e^{-\tau_v} + B_v(T_{\text{ex}})(1 - e^{-\tau_v})$$

Radiation transport II



So we have: $I_v = I_v(0)e^{-\tau_v} + B_v(T_{\text{ex}})(1 - e^{-\tau_v})$

Define $T_A(\nu) \equiv I_\nu / [2k\nu^2 c^{-2}]$, $T_A(0) = T_{\text{bg}}$, and define $J_\nu(T) = (h\nu/k)(e^{h\nu/kT} - 1)^{-1}$
(Note: in Rayleigh-Jeans limit $h\nu/kT \ll 1$ and $J_\nu(T) = T$)

Then: $T_A = J(T_{\text{ex}})(1 - e^{-\tau_v}) + J(T_{\text{bg}})e^{-\tau_v}$

Detection equation

in Rayleigh-Jeans limit: $T_A = T_{\text{ex}}(1 - e^{-\tau_v}) + T_{\text{bg}}e^{-\tau_v}$

In practice one measures $\Delta T_A = T_A - T_{\text{bg}}$ (ON-OFF) = $(T_{\text{ex}} - T_{\text{bg}})(1 - e^{-\tau_v})$

- 1) $\tau_v \ll 1$: $\Delta T_A \approx T \tau_v$ **measure column density**. All photons escape.
- 2) $\tau_v \gg 1$: $\Delta T_A \approx T$ **measure kinetic temperature**, but independent of col. dens.
Only photons at cloud surface ($\tau_v \leq 1$) escape.

T_{ex} , τ , and column density in LTE

For an optically thick line, e.g. CO(1-0): $\tau_v \gg 1$; the detection equation yields:

$$\begin{aligned} T_{\text{ex}} &= (h\nu/k) \ln^{-1}(h\nu/k [T_A + J(T_{\text{bg}})]^{-1} + 1) \\ &= 5.532 \ln^{-1}(5.532[T_A + 0.818]^{-1} + 1) \end{aligned}$$

For an optically thin line, e.g. $^{13}\text{CO}(1-0)$: $\tau_v \ll 1$; it follows that:

$$\tau_v = -\ln[1 - T_A / (J(T_{\text{ex}}) - J(T_{\text{bg}}))]^{-1}$$

Column density – derived from transition between levels J and J-1.

Detection equation: $T_A = J(T_{\text{ex}}) (1 - e^{-\tau_v}) + J(T_{\text{bg}}) e^{-\tau_v}$ and $\tau_v \ll 1$, solve for τ_v .

From definition of T_{ex} , the definitions of the Einstein-coefficients, the equation for the absorption coefficient, and the definition of τ

$$N_{\text{tot}} = \left(\frac{3h}{8\pi^3 \mu^2} \right) \left(\frac{Z}{J} \right) e^{\frac{h\nu}{kT_{\text{ex}}}} \left[1 - e^{-\frac{h\nu}{kT_{\text{ex}}}} \right]^{-1} [J(T_{\text{ex}}) - J(T_{\text{bg}})] \int T_A dv$$

with Z the partition function (linking N_l to N_{tot}).

or: $N_{\text{tot}} = f(T_{\text{ex}}) \int T_A dv$

Total column density

$$N_{\text{tot}} = f(T_{\text{ex}}) \int T_A dv$$

For $^{13}\text{CO}(1-0)$ and $\text{C}^{18}\text{O}(1-0)$ and $T_{\text{ex}} \approx 5 - 20 \text{ K}$:

$$f(T_{\text{ex}}) \approx (1.1 \pm 0.2) \times 10^{15} \text{ cm}^{-2} / (\text{Kkm/s})$$

Hence:

$$N_{\text{tot}} = (1.1 \pm 0.2) \times 10^{15} \int T_A dv \text{ cm}^{-2} \Rightarrow \text{Mass!}$$

If $\tau_v \leq 2$ then correction factor $\tau_0 / [1 - \exp(-\tau_0)]$, with τ_0 the opt. depth at line center $\tau_0 = -\ln(1-1/R)$ and $R = T_A(^{12}\text{CO}) / T_A(^{13}\text{CO})$.

Therefore:

$$N_{\text{tot}} = (1.1 \pm 0.2) \times 10^{15} \times \tau_0 / [1 - \exp(-\tau_0)] \times \int T_A dv \text{ cm}^{-2}$$

Mass follows via abundances: $N(^{12}\text{CO})/N(^{13}\text{CO}) \sim 90$ and $N(^{12}\text{CO})/N(\text{H}_2) \sim 1 \times 10^{-4}$

Typical medium
Temperature

Critical
density
proportional
to A

Table 2. Parameters of the commonly observed short cm/mm molecular lines

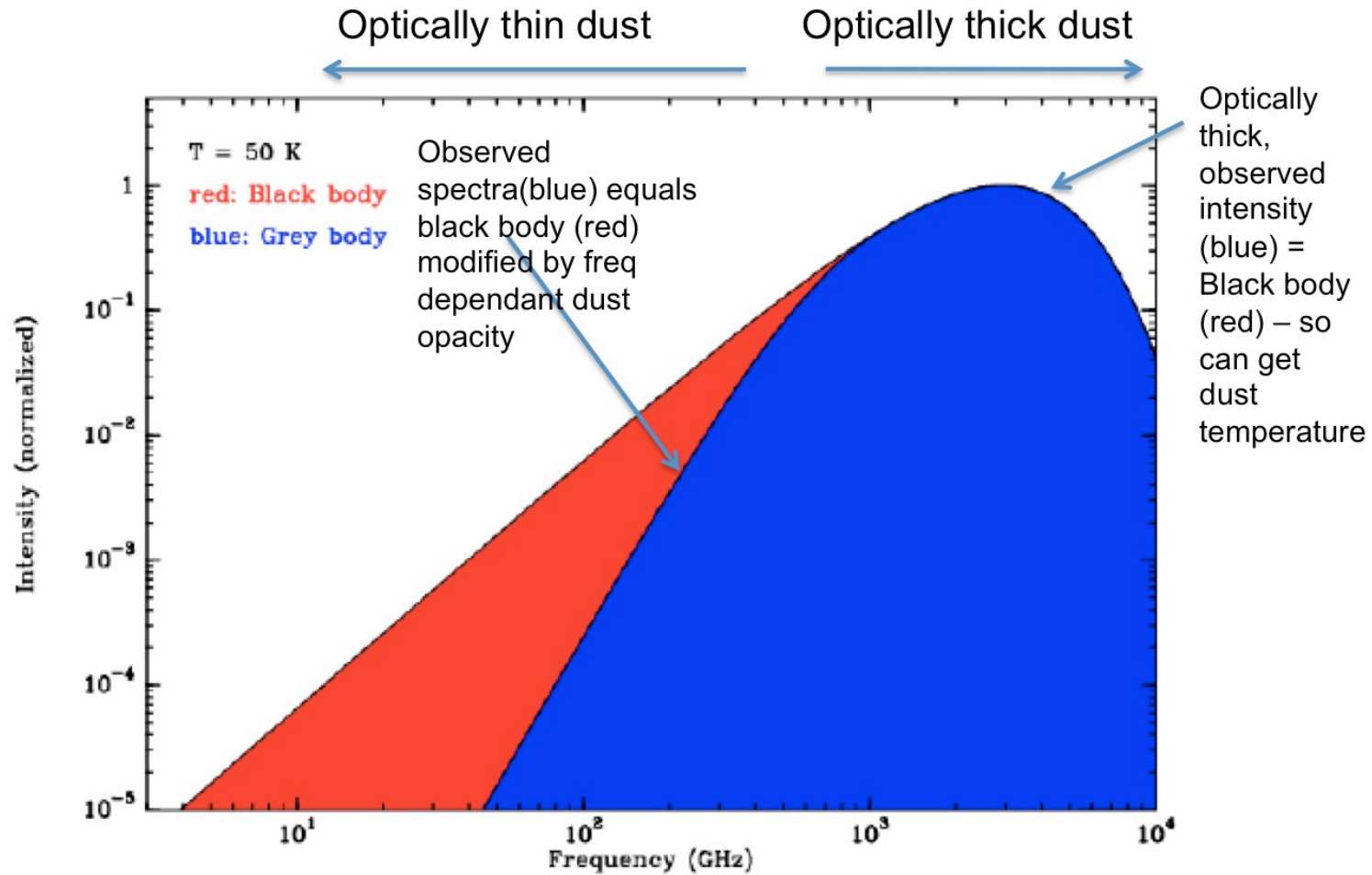
Chemical ^a formula	Molecule name	Transition	ν /GHz	E_u /K ^b	A_{ij} /s ^{-1c}
H ₂ O	ortho-water*	$J_{K_a K_c} = 6_{16} - 5_{23}$	22.235253	640	1.9×10^{-9}
NH ₃	para-ammonia	$(J, K) = (1, 1) - (1, 1)$	23.694506	23	1.7×10^{-7}
NH ₃	para-ammonia	$(J, K) = (2, 2) - (2, 2)$	23.722634	64	2.2×10^{-7}
NH ₃	ortho-ammonia	$(J, K) = (3, 3) - (3, 3)$	23.870130	122	2.5×10^{-7}
SiO	silicon monoxide*	$J = 1 - 0, v = 2$	42.820587	3512	3.0×10^{-6}
SiO	silicon monoxide*	$J = 1 - 0, v = 1$	43.122080	1770	3.0×10^{-6}
SiO	silicon monoxide	$J = 1 - 0, v = 0$	43.423858	2.1	3.0×10^{-6}
CS	carbon monosulfide	$J = 1 - 0$	48.990964	2.4	1.8×10^{-6}
DCO ⁺	deuterated formylium	$J = 1 - 0$	72.039331	3.5	2.2×10^{-5}
SiO	silicon monoxide*	$J = 2 - 1, v = 2$	85.640456	3516	2.0×10^{-5}
SiO	silicon monoxide*	$J = 2 - 1, v = 1$	86.243442	1774	2.0×10^{-5}
H ¹³ CO ⁺	formylium	$J = 1 - 0$	86.754294	4.2	3.9×10^{-5}
SiO	silicon monoxide	$J = 2 - 1, v = 0$	86.846998	6.2	2.0×10^{-5}
HCN	hydrogen cyanide	$J = 1 - 0, F = 2 - 1$	88.631847	4.3	2.4×10^{-5}
HCO ⁺	formylium	$J = 1 - 0$	89.188518	4.3	4.2×10^{-5}
HNC	hydrogen isocyanide	$J = 1 - 0, F = 2 - 1$	90.663574	4.3	2.7×10^{-5}
N ₂ H ⁺	diazanylium	$J = 1 - 0, F_1 = 2 - 1,$ $F = 3 - 2$	93.173809	4.3	3.8×10^{-5}
CS	carbon monosulfide	$J = 2 - 1$	97.980968	7.1	2.2×10^{-5}
C ¹⁸ O	carbon monoxide	$J = 1 - 0$	109.782182	5.3	6.5×10^{-8}
¹³ CO	carbon monoxide	$J = 1 - 0$	110.201370	5.3	6.5×10^{-8}
CO	carbon monoxide	$J = 1 - 0$	115.271203	5.5	7.4×10^{-8}
H ₂ ¹³ CO	ortho-formaldehyde	$J_{K_a K_c} = 2_{12} - 1_{11}$	137.449959	22	5.3×10^{-5}
H ₂ CO	ortho-formaldehyde	$J_{K_a K_c} = 2_{12} - 1_{11}$	140.839518	22	5.3×10^{-5}
CS	carbon monosulfide	$J = 3 - 2$	146.969049	14.2	6.1×10^{-5}
C ¹⁸ O	carbon monoxide	$J = 2 - 1$	219.560319	15.9	6.2×10^{-7}
¹³ CO	carbon monoxide	$J = 2 - 1$	220.398714	15.9	6.2×10^{-7}
CO	carbon monoxide	$J = 2 - 1$	230.538001	16.6	7.1×10^{-7}
CS	carbon monosulfide	$J = 5 - 4$	244.935606	33.9	3.0×10^{-4}
HCN	hydrogen cyanide	$J = 3 - 2$	265.886432	25.5	8.5×10^{-4}
HCO ⁺	formylium	$J = 3 - 2$	267.557625	25.7	1.4×10^{-3}
HNC	hydrogen isocyanide	$J = 3 - 2$	271.981067	26.1	9.2×10^{-4}

Choose molecular species depending on n, T of gas you want to probe. Also must consider expected strength of line, depends on intrinsic strength (prop to A) + chemical abundance. Must be strong enough to detect, but may want to avoid being optically thick

TABLE 1 Properties of density probes

Molecule	Transition	ν (GHz)	E_{up} (K)	$n_c(10\text{ K})$ (cm^{-3})	$n_{eff}(10\text{ K})$ (cm^{-3})	$n_c(100\text{ K})$ (cm^{-3})	$n_{eff}(100\text{ K})$ (cm^{-3})
CS	$J = 1 \rightarrow 0$	49.0	2.4	4.6×10^4	7.0×10^3	6.2×10^4	2.2×10^3
CS	$J = 2 \rightarrow 1$	98.0	7.1	3.0×10^5	1.8×10^4	3.9×10^5	4.1×10^3
CS	$J = 3 \rightarrow 2$	147.0	14	1.3×10^6	7.0×10^4	1.4×10^6	1.0×10^4
CS	$J = 5 \rightarrow 4$	244.9	35	8.8×10^6	2.2×10^6	6.9×10^6	6.0×10^4
CS	$J = 7 \rightarrow 6$	342.9	66	2.8×10^7	...	2.0×10^7	2.6×10^5
CS	$J = 10 \rightarrow 9$	489.8	129	1.2×10^8	...	6.2×10^7	1.7×10^6
HCO ⁺	$J = 1 \rightarrow 0$	89.2	4.3	1.7×10^5	2.4×10^3	1.9×10^5	5.6×10^2
HCO ⁺	$J = 3 \rightarrow 2$	267.6	26	4.2×10^6	6.3×10^4	3.3×10^6	3.6×10^3
HCO ⁺	$J = 4 \rightarrow 3$	356.7	43	9.7×10^6	5.0×10^5	7.8×10^6	1.0×10^4
HCN	$J = 1 \rightarrow 0$	88.6	4.3	2.6×10^6	2.9×10^4	4.5×10^6	5.1×10^3
HCN	$J = 3 \rightarrow 2$	265.9	26	7.8×10^7	7.0×10^5	6.8×10^7	3.6×10^4
HCN	$J = 4 \rightarrow 3$	354.5	43	1.5×10^8	6.0×10^6	1.6×10^8	1.0×10^5
H ₂ CO	$2_{12} \rightarrow 1_{11}$	140.8	6.8	1.1×10^6	6.0×10^4	1.6×10^6	1.5×10^4
H ₂ CO	$3_{13} \rightarrow 2_{12}$	211.2	17	5.6×10^6	3.2×10^5	6.0×10^6	4.0×10^4
H ₂ CO	$4_{14} \rightarrow 3_{13}$	281.5	30	9.7×10^6	2.2×10^6	1.2×10^7	1.0×10^5
H ₂ CO	$5_{15} \rightarrow 4_{14}$	351.8	47	2.6×10^7	...	2.5×10^7	2.0×10^5
NH ₃	(1,1)inv	23.7	1.1	1.8×10^3	1.2×10^3	2.1×10^3	7.0×10^2
NH ₃	(2,2)inv	23.7	42	2.1×10^3	3.6×10^4	2.1×10^3	4.3×10^2

... means no value; inv means inversion transition.



$\lambda \sim 100\text{-}500 \text{ } \mu\text{m}$ good diagnostic T_d
 $\lambda \sim 800 \text{ } \mu\text{m} - 3 \text{ mm}$ good tracer of mass

$$M_d = \frac{S_v d^2}{B_v(T_d) \kappa_d}$$

$$\kappa_d = \kappa_0 \left(\frac{\nu}{230 \text{ GHz}} \right)^\beta \text{ cm}^2 \text{ g}^{-1}$$

Deriving $N(\text{H}_2)$, total mass

1. Lines (Planck & Boltzmann)

Detection eqn., LTE, $\tau(^{12}\text{CO}) \gg 1$ ($\Rightarrow T_{\text{ex}}$), $\tau(^{13}\text{CO}) \ll 1$

$$N(^{13}\text{CO}) = f(\tau_{13}, T_{\text{ex}}, \Delta v_{13}) + [\text{H}_2]/[^{13}\text{CO}] = \dots \Rightarrow N(\text{H}_2)_{\text{LTE}}$$

$^{12}\text{C}/\text{H}$, $^{12}\text{C}/^{13}\text{C}$ gradients $\Rightarrow [\text{H}_2]/[^{13}\text{CO}] = f(R)$

Non-LTE transitions: LVG model (full radiation transport eqns.)

2. Lines (empirical)

$$N(\text{H}_2)/\int T_{12} dv \equiv X \Rightarrow N(\text{H}_2)_{\text{Wco}}$$

$X = \text{constant or } f(R)$? Works better for ensembles than for individual clouds

3. Virial theorem

Cloud radius (r), linewidth (Δv), assumptions about density distribution. For spherical cloud, $n \propto r^{-2} \Rightarrow M_{\text{vir}} = 126 r \Delta v^2$

Exclude non-bound motions (e.g. outflows); actual density distribution?

4. Dust continuum

$$M = (g S_{\nu} d^2) / \kappa_{\nu} B(T_{\text{dust}})$$

κ_{ν} , T-structure, gas-to-dust ratio (g) uncertain

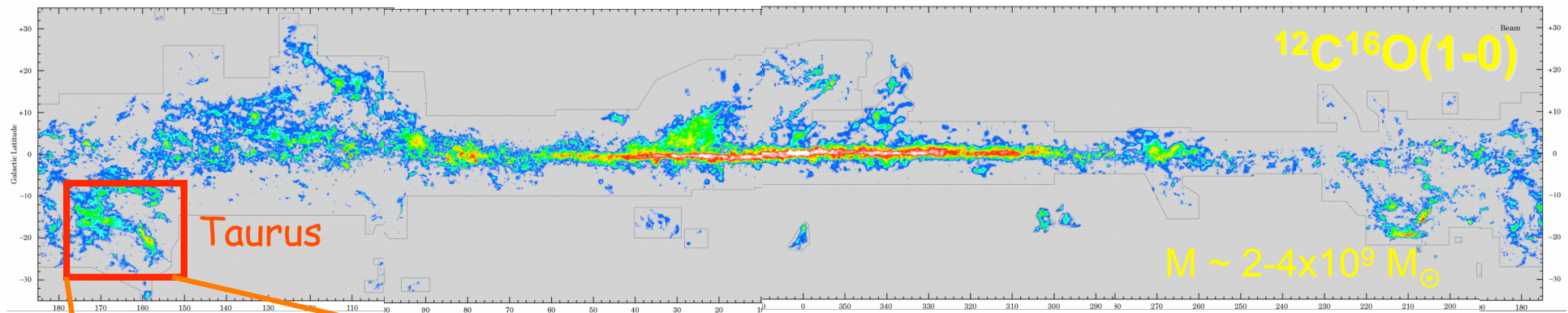
Results of molecular cloud mapping

Type	R (pc)	n (cm ⁻³)	M (M _⊙)	ΔV (km/s)	T (K)	Cores & stars
Diffuse	0.3-3	30-500	0.5-10 ²	0.7-1.5	10?	Low-mass
Dark	3-10	10 ²⁻³	10 ³⁻⁴	1-3	10	Low-mass
Giant	20-100	10-300	10 ⁵⁻⁶	5-15	10-20	High-mass (+Low-mass)

Total molecular mass in Galaxy $\sim 2\text{-}4 \times 10^9 M_{\odot} \approx M(\text{HI})$

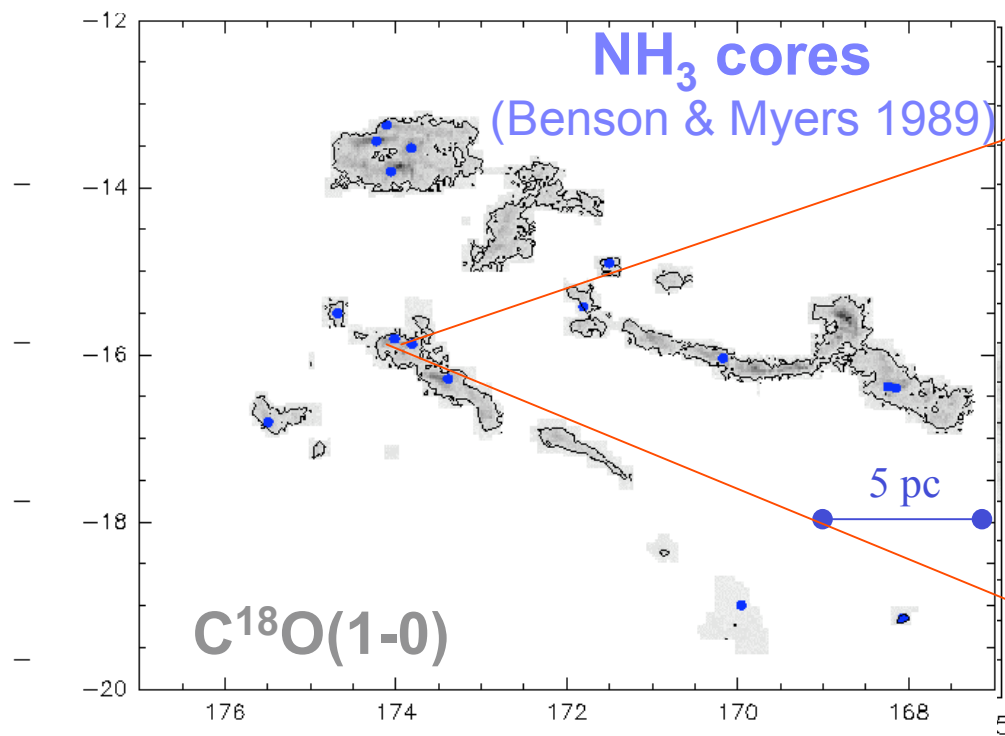
CLUMPY STRUCTURE AND MASS DISTRIBUTIONS

Our Galaxy at 115 GHz

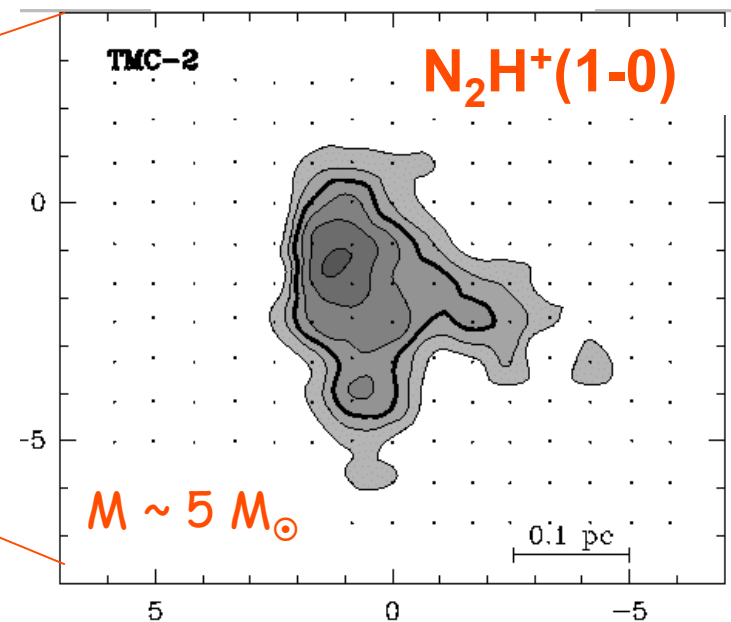


Dame, Hartmann and Thaddeus 2001

Onishi et al. 1998

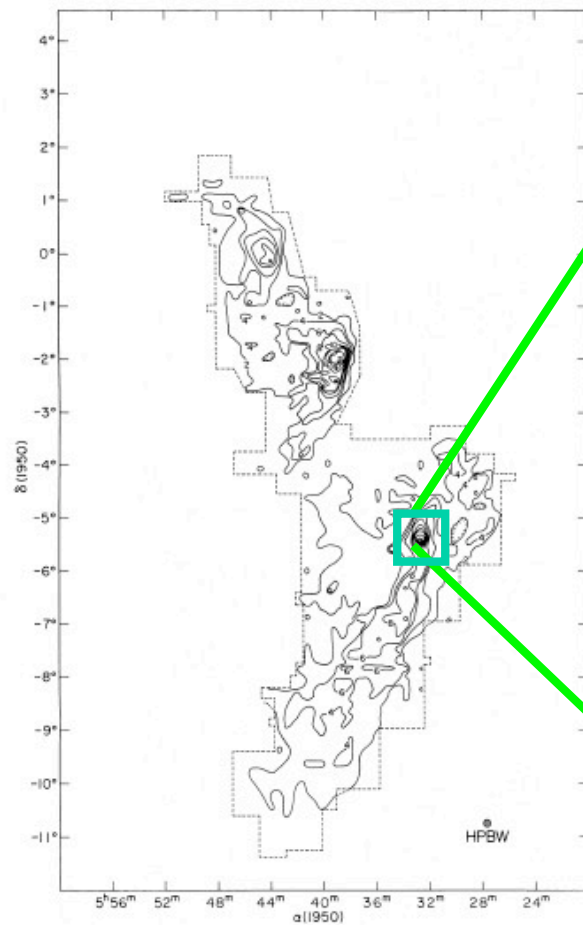


Caselli et al. 2002a



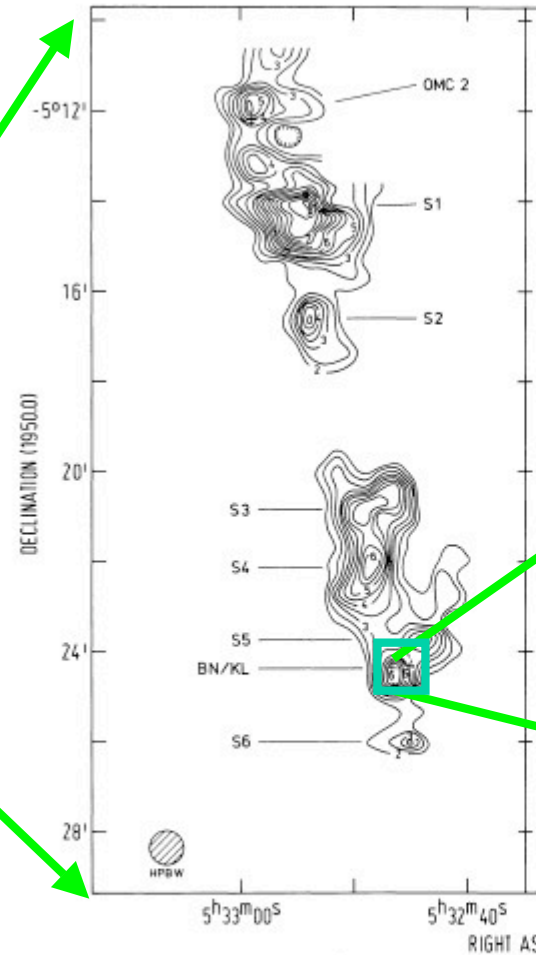
Clumpy structure - Self-similarity

CO [$\varnothing \approx 8' \approx 1$ pc]



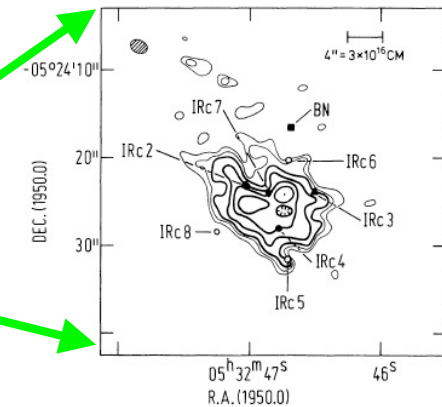
Kutner et al. 1977

NH₃ [$\varnothing \approx 43'' \approx 0.1$ pc]



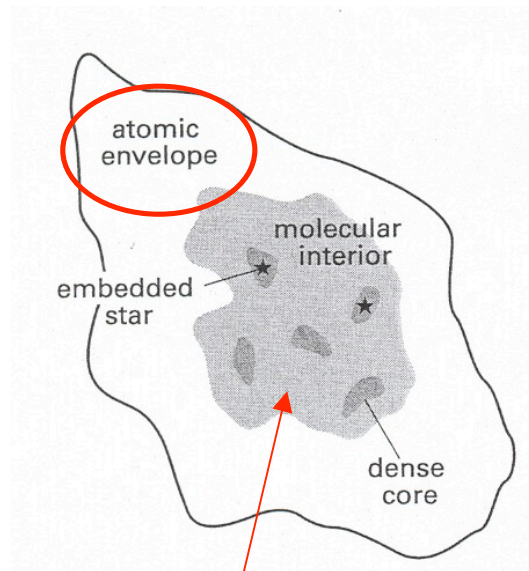
Batrla et al. 1983

NH₃ [$\varnothing \approx 1''.5 \times 2''.2$
 $\approx 4 \times 10^{-3}$ pc]



Pauls et al. 1983

Cloud structure



Interclump gas:
predominantly
atomic

Self-similar, fractal structure

Cloud , clump, core

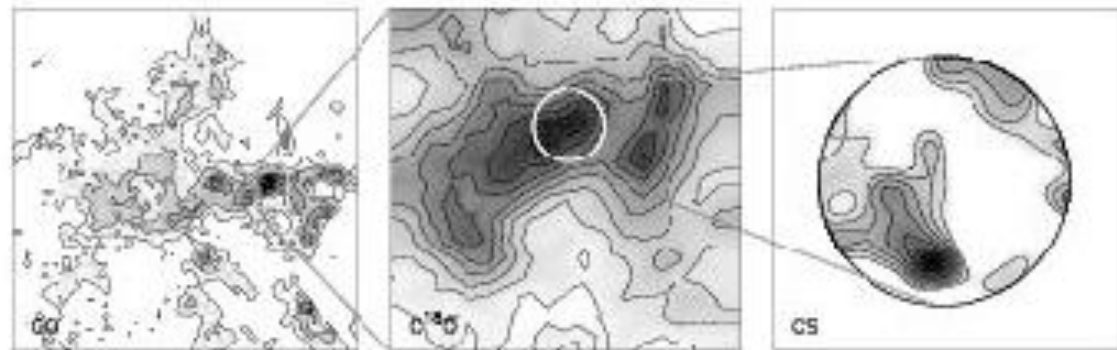
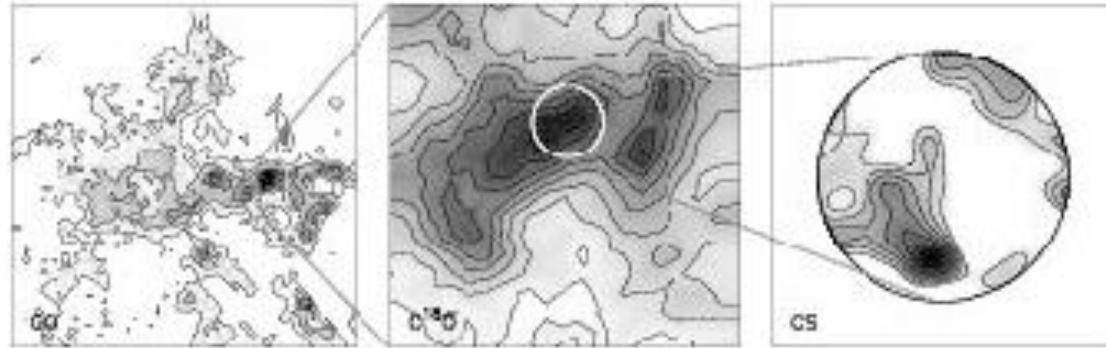


Figure 4. Hierarchical cloud structure. The three panels show a representative view from cloud to clump to core. The bulk of the molecular gas (cloud; left panel) is best seen in CO which, although optically thick, faithfully outlines the location of the H₂. Internal structure (clumps; middle panel) is observed at higher resolution in an optically thin line such as C¹⁸O. With a higher density tracer such as CS, cores (right panel) stand out. The observations here are of the Rosette molecular cloud and are respectively, Bell Labs (90"), FCRAO data (50"), and BIMA data (10").



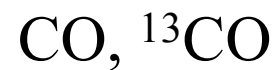
Clouds

$$D \geq 10 \text{ pc}$$

$$n(\text{H}_2) \approx 10^2\text{-}10^3 \text{ cm}^{-3}$$

$$M \geq 10^4 M_{\odot}$$

$$T \approx 10 \text{ K}$$



$$N(\text{CO})/N(\text{H}_2) \approx 10^{-4}$$

clumps

$$D \approx 1 \text{ pc}$$

$$n(\text{H}_2) \approx 10^5 \text{ cm}^{-3}$$

$$M \approx 10^3 M_{\odot}$$

$$T \approx 50 \text{ K}$$



$$N(\text{CS})/N(\text{H}_2) \approx 10^{-8}$$

cores

$$D \approx 0.1 \text{ pc}$$

$$n(\text{H}_2) \approx 10^7 \text{ cm}^{-3}$$

$$M \approx 10\text{-}10^3 M_{\odot}$$

$$T \approx 100 \text{ K}$$



$$N(\text{CH}_3\text{CN})/N(\text{H}_2) \approx 10^{-10}$$

Typical clump properties

(based on a study of the RMC – Rosette Molecular Cloud)

- 60 –90% of H_2 in clumps
- $\langle n \rangle \sim 10^3 \text{ cm}^{-3}$; $\langle n_{\text{vol}} \rangle \sim 25 \text{ cm}^{-3}$. Thus: volume filling factor $\sim 2.5\%$
Hence: $n(\text{interclump}) \sim 2.5\text{-}12.5 \text{ cm}^{-3}$
- $\Sigma(r) \propto r^{-1}$, i.e. $\rho(r) \propto r^{-2}$
- Mass spectrum $dN/dM \propto M^\alpha$, $\alpha = -1.4$ to -1.7 for $M = 1\text{-}3000 M_\odot$.
Idem for clouds as a whole

Self-similarity – Clump mass distribution

Kramer et al. 1998

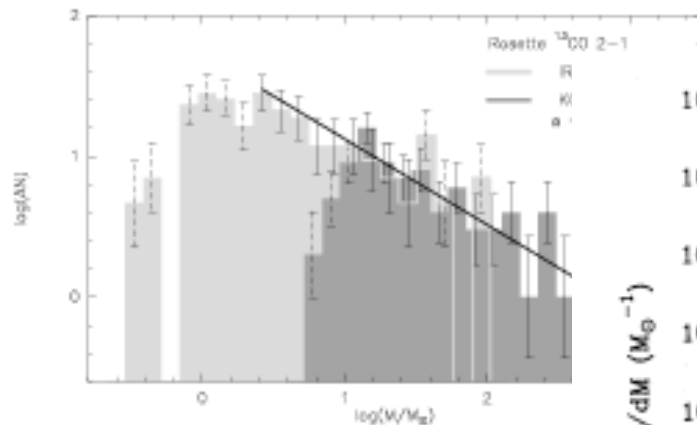
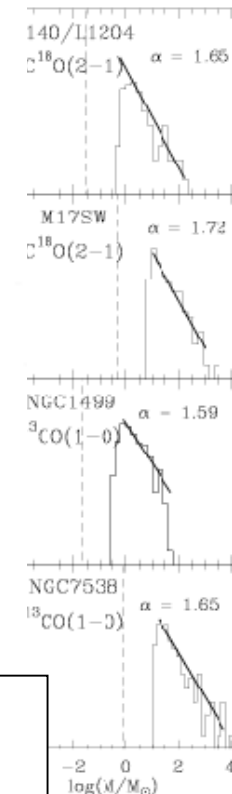
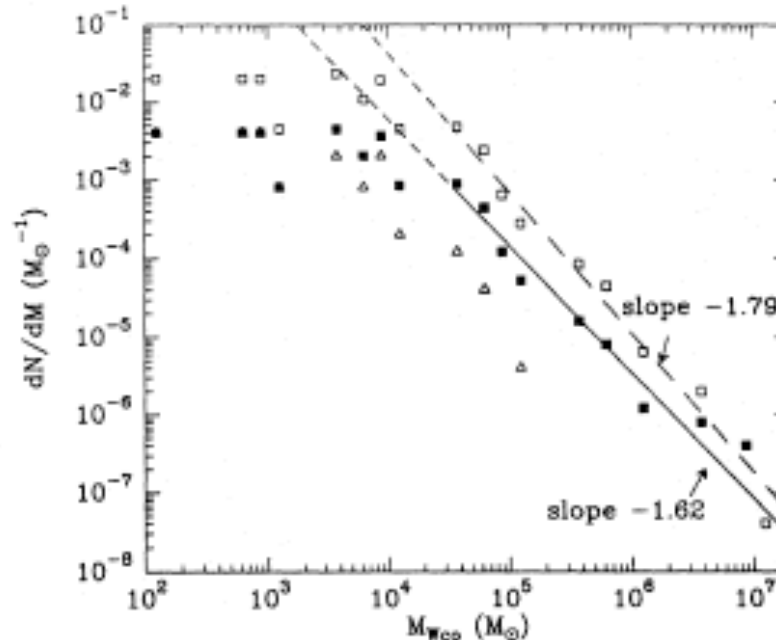


Fig. 16. Clump mass spectrum derived from $^{13}\text{CO } J=2 \rightarrow 1$ with KOSMA (85 clumps) and IRAM. The continuous line is a fit to the power law function $dN/dM \propto M^{-\alpha}$. The result is $\alpha=1.61$. The dashed lines of the error bars mark the region beyond the turnover points and the IRAM high-mass clumps are not included in the fit.

Rosette Molecular Cloud
Schneider et al. 1998



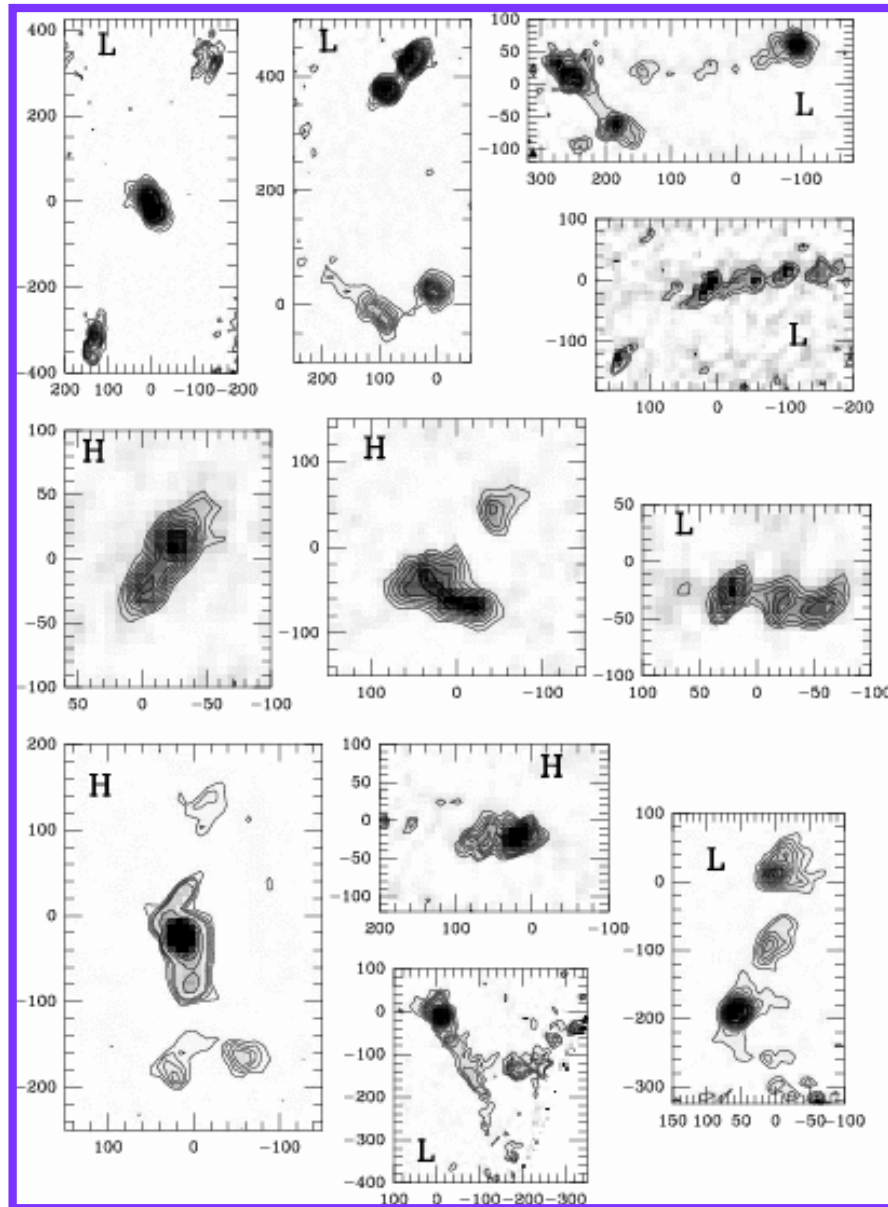
Power-law mass distribution 10
Most clumps at low-mass end,
clumps

204 clouds between
R=2-25kpc: same slope!

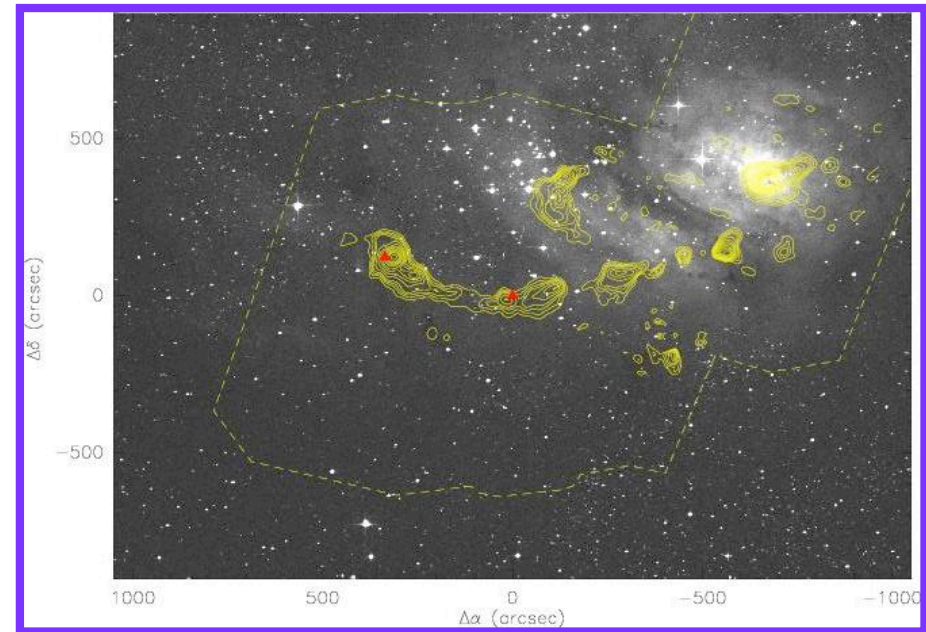
Mass distribution of sample of GMCs has **same slope**

Brand & Wouterloot 1995

Simba results 1



Multiple cores & chains



DSS + SIMBA (1.2-mm cont.)

AND: 95 pre-stellar or
pre-cluster cores!

Beltran, Brand, Cesaroni et al. 2006

Simba results 2: clump mass function

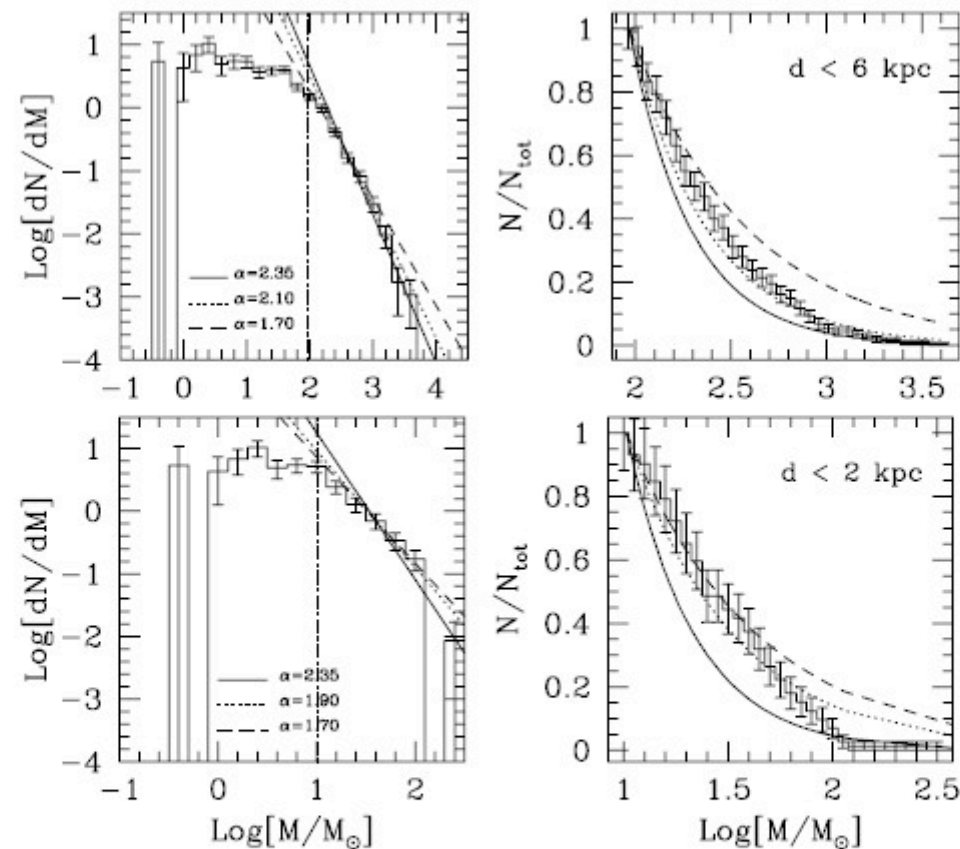
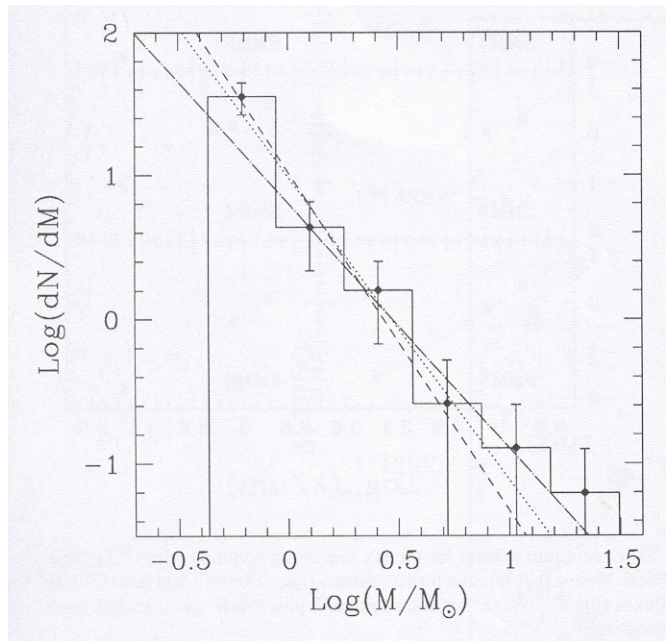


Fig. 10. *Left top panel*: the mass spectrum of the 1.2 mm clumps detected at a distance <6 kpc. The solid line represents the Salpeter IMF, $dN/dM \propto M^{-2.35}$; the dotted line is a -2.1 power law, obtained from the least square fit to the data, and the dashed line is a -1.7 power law. The vertical dot-dashed line indicates the completeness limit at 6 kpc. *Right top panel*: the normalized cumulative mass distribution of clumps with masses above the completeness limit at 6 kpc. The solid, and dashed lines are the same as in the left panel, and the dotted line is a -1.9 power law, obtained from the least square fit to the data. *Left bottom panel*: same as above for clumps detected at a distance <2 kpc. The vertical dot-dashed line indicates the completeness limit at 2 kpc. *Right bottom panel*: same as above for clumps with masses above the completeness limit at 2 kpc.

Slope 10-100 M_{\odot} : $-(1.5-1.9)$; $>100 M_{\odot}$: -2.1

Beltran, Brand, Cesaroni et al. 2006



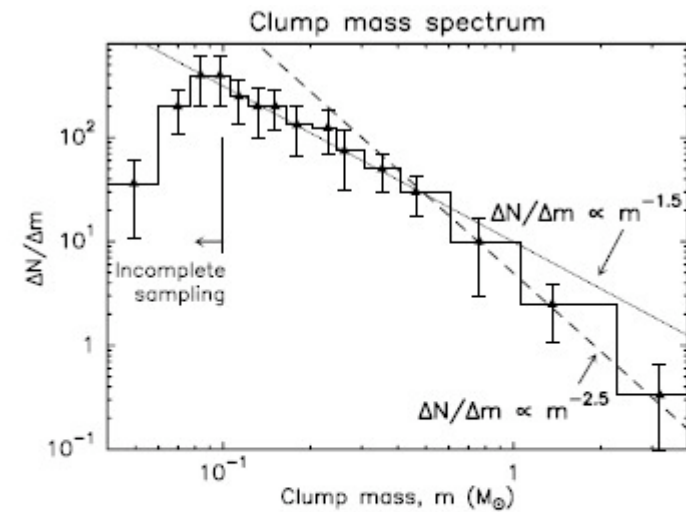
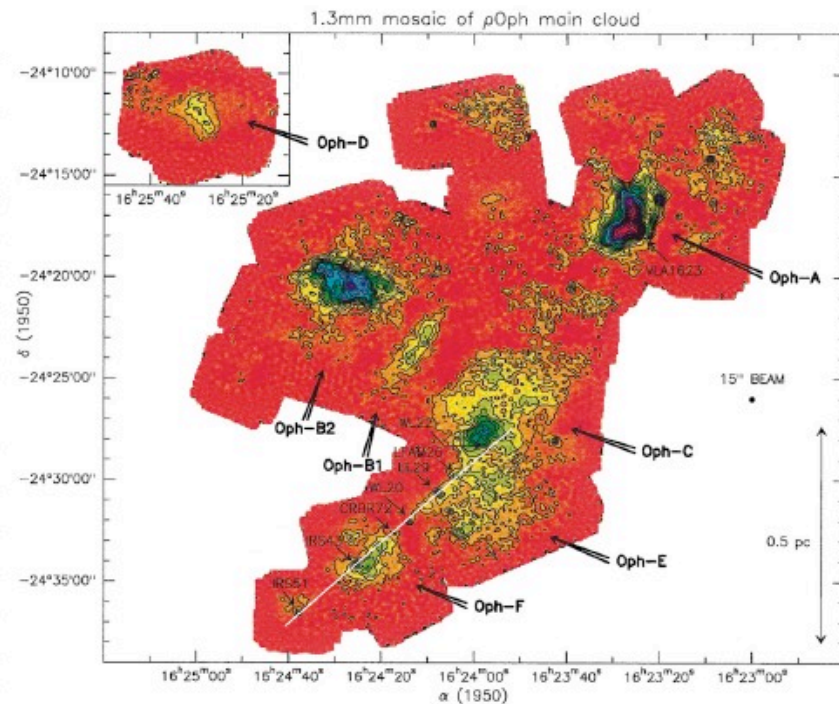
Serpens: Testi & Sargent 1998

26 pre-stellar clumps
Slope -2.1

IMF:

Salpeter: -2.5 for $M = 1-10 M_{\odot}$.

Miller-Scalo: -1.5 for $M < 1 M_{\odot}$.



60 pre-stellar clumps in ρ Oph
Slope -1.5 for $M = 0.1-0.5 M_{\odot}$.
-2.5 $0.5-3 M_{\odot}$.

Ophiuchus: Motte et al. 1998

Typical clump properties

(based on a study of the RMC – Rosette Molecular Cloud; Blitz et al.)

- 60 –90% of H_2 in clumps
- $\langle n \rangle \sim 10^3 \text{ cm}^{-3}$; $\langle n_{\text{vol}} \rangle \sim 25 \text{ cm}^{-3}$. Thus: volume filling factor $\sim 2.5\%$
Hence: $n(\text{interclump}) \sim 2.5\text{-}12.5 \text{ cm}^{-3}$
- $\Sigma(r) \propto r^{-1}$, i.e. $\rho(r) \propto r^{-2}$
- Mass spectrum $dN/dM \propto M^\alpha$, $\alpha = -1.4$ to -1.7 for $M = 1\text{-}3000 M_\odot$.
Idem for clouds as a whole
- Most clumps not gravitationally bound, but most mass is in clumps that are.
Yet clumps are not expanding: pressure-confinement
- Inside clump: $P_{\text{int}}/k \sim 6\text{-}12 \times 10^4 \text{ Kcm}^{-3}$ (bulk gas motions)
Inside GMC, due to gravity: $P_{\text{grav}}/k \sim 8 \times 10^4 \text{ Kcm}^{-3}$
 $P_{\text{HI}}/k \sim 10 \times 10^4 \text{ Kcm}^{-3}$
 \Rightarrow clumps confined by interclumps gas (which is HI)

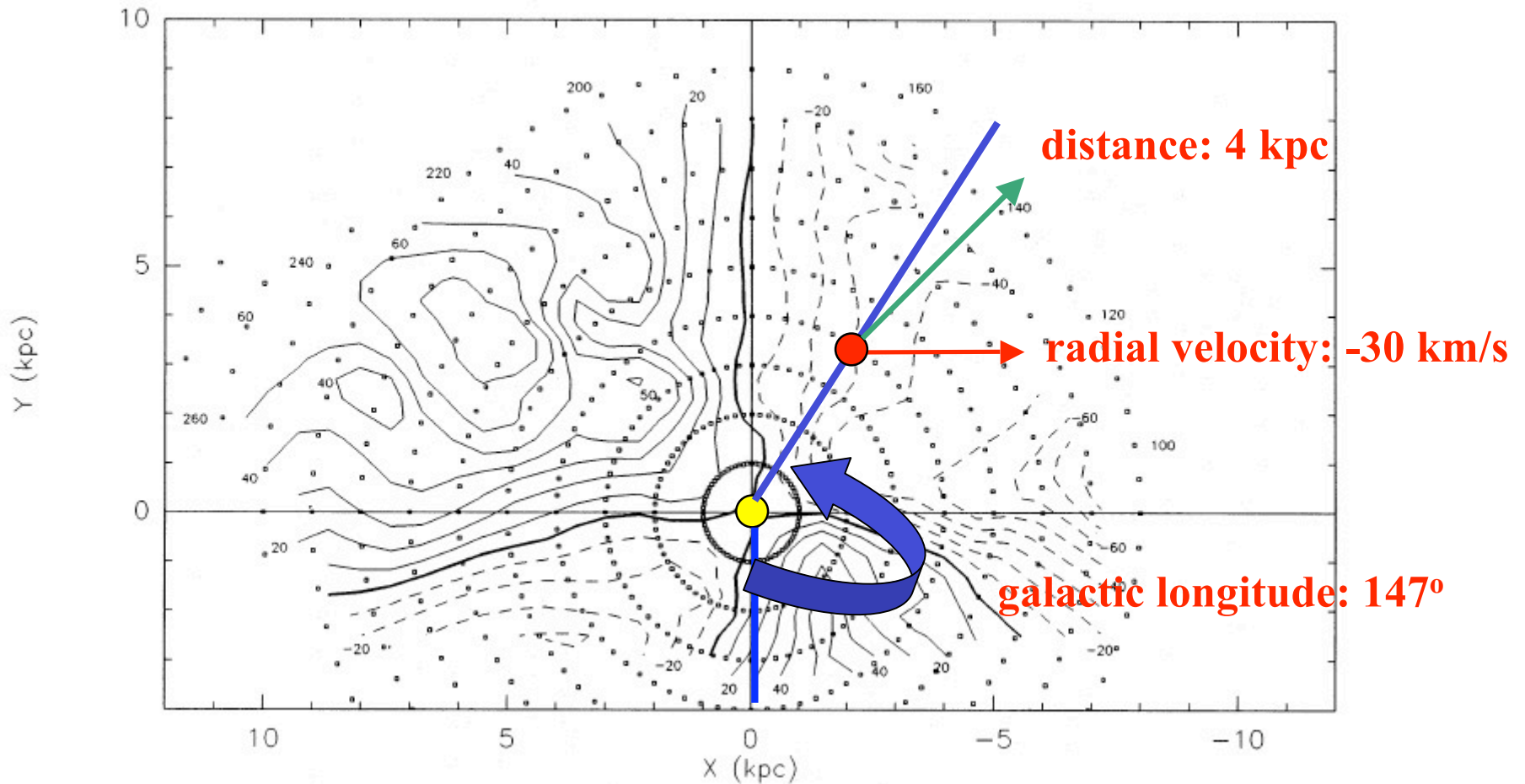
MOLECULAR GAS KINEMATICS

rotation curve and kinematic distances

The observed velocity field

(Brand & Blitz 1993)

Radial velocity as a function of distance



Kinematic distances I

Observed velocity field is useful to determine kinematic distances, but its range of use is limited (e.g., <2 kpc from Sun in inner Galaxy)

Therefore: **construct the rotation curve** (Θ versus R)

Transform observed radial velocities and spectro-photometric distances into galactic rotation velocity Θ and galactocentric distance R :

$V_{\text{lsr}} = (\Theta R_0 / R - \Theta_0) \sin l \cos b$ for circular rotation.

$\omega = \Theta / R$: angular rotation velocity $\Rightarrow V_{\text{lsr}} = R_0(\omega - \omega_0) \sin l \cos b \Rightarrow$

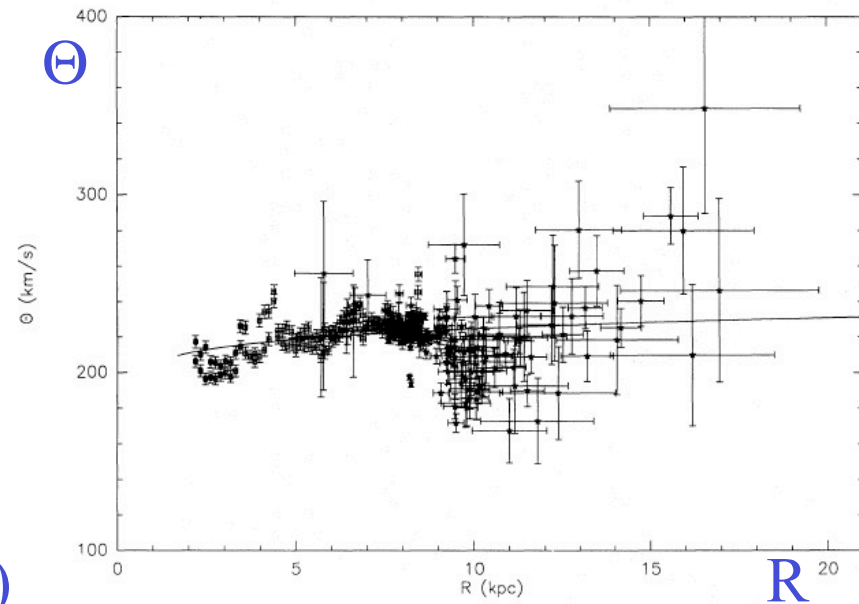
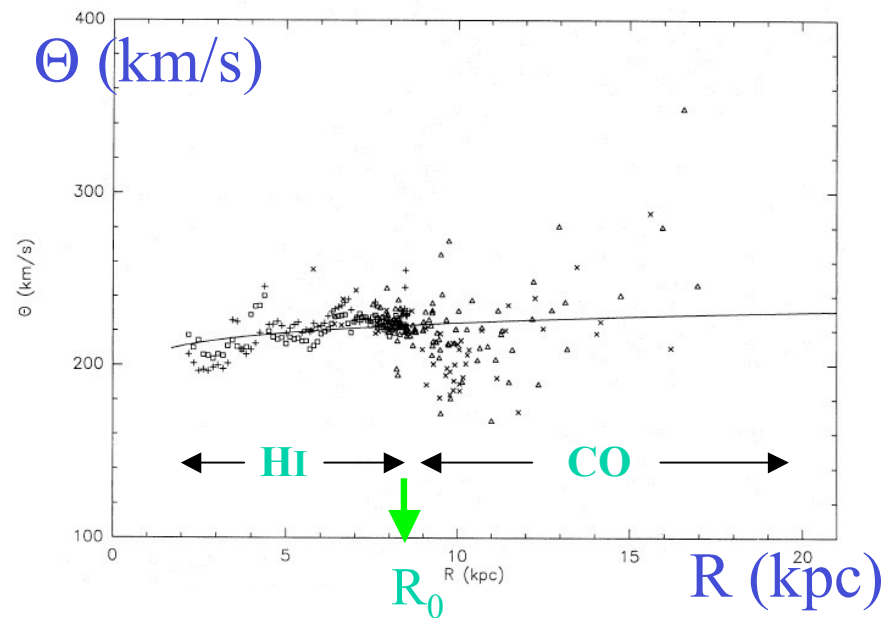
$\omega = V_{\text{lsr}} / (R_0 \sin l \cos b) + \omega_0$

$R = (d^2 \cos^2 b + R_0^2 - 2 R_0 d \cos b \cos l)^{1/2}$

Advantage: get distances everywhere.

Disadvantage: in some regions erroneous because **streaming motions** are not included.

Rotation curve from HI and CO



Fit a function of type:

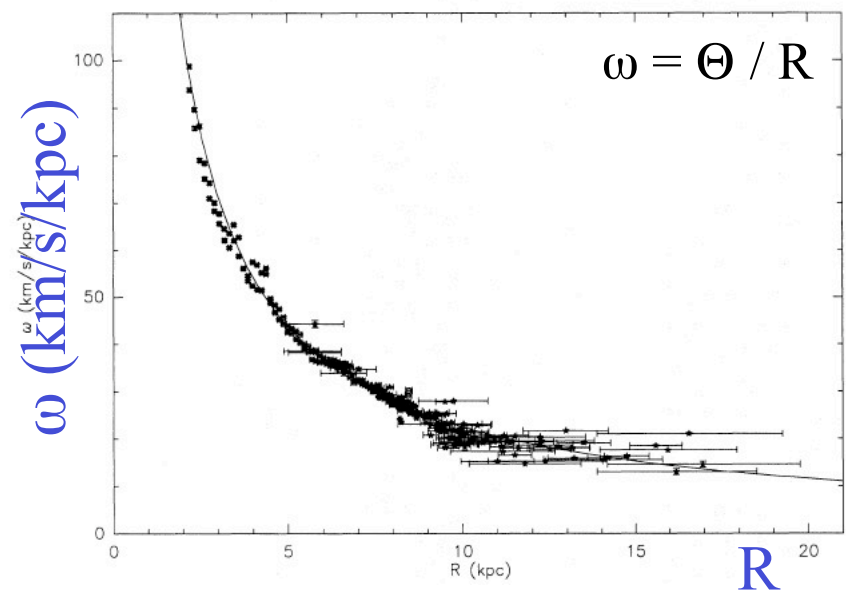
$$\omega/\omega_0 = a_1(R/R_0)^{a_2-1} + a_3(R/R_0)$$

Implying

$$\Theta/\Theta_0 = a_1(R/R_0)^{a_2} + a_3$$

$$a_1 = 1.0077, a_2 = 0.0394, a_3 = 0.00712$$

(Brand & Blitz 1993)



Kinematic distances II

Rotation curve: $\Theta = \Theta_0 (R/R_0)^a$ with $\Theta_0 = 220$ km/s, $R_0 = 8.5$ kpc

In general: $V_{\text{lsr}} = R_0(\omega - \omega_0) \sin l \cos b$, and $\omega = \Theta/R$.

It follows that:

$$R = ([(V_{\text{lsr}} / \sin l \cos b) + \Theta_0] / \Theta_0 R_0^{1-a})^{1/(a-1)} \text{ and}$$

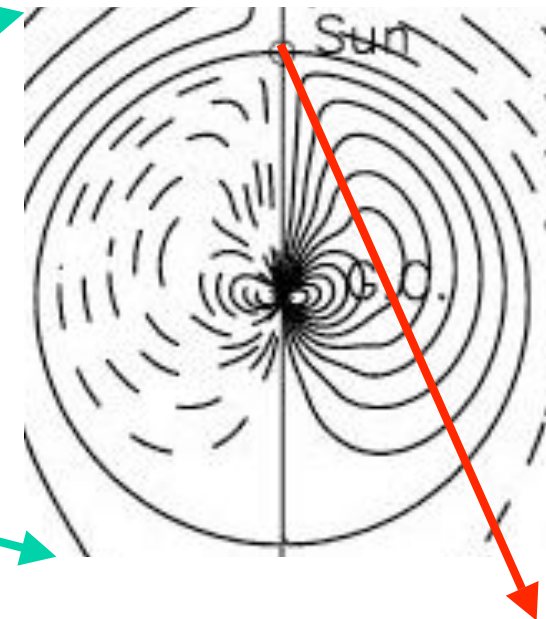
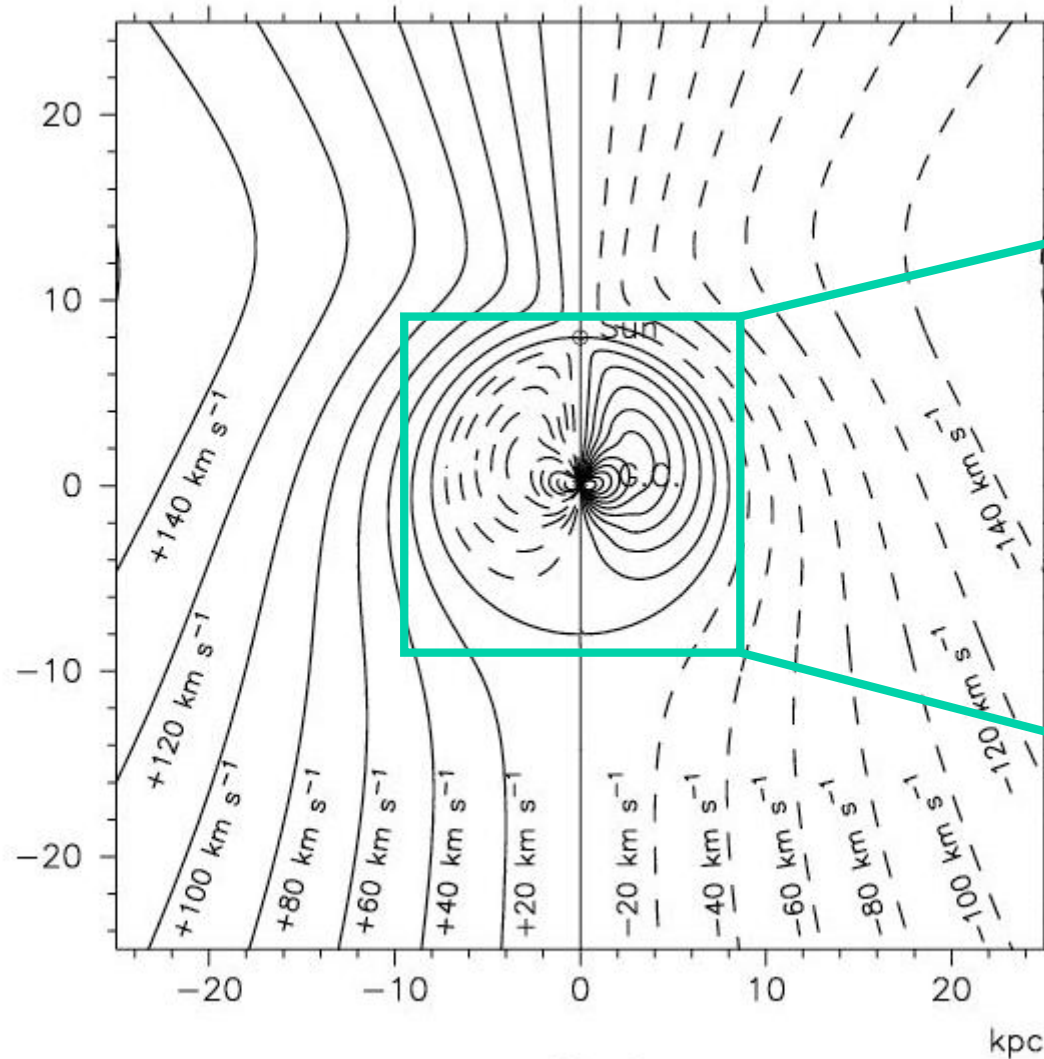
$$d = [R_0 \cos l \pm (R^2 - R_0^2 \sin^2 l)]^{0.5} / \cos b$$

For outer Galaxy: choose ‘+’

For inner Galaxy, there are 2 solutions: distance ambiguity!

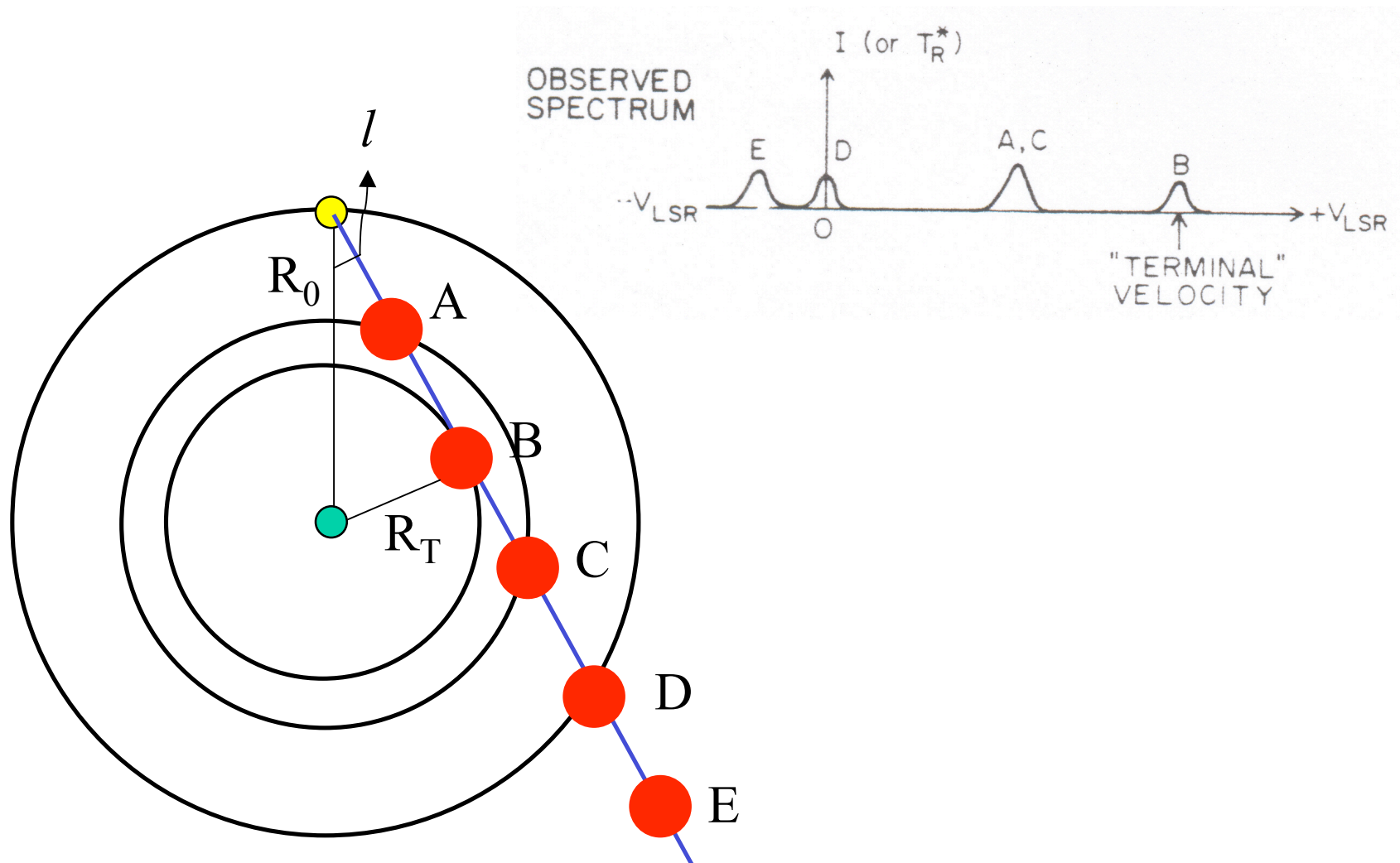
Distance ambiguity in inner Galaxy

Velocity field from rotation curve



Two values for d at the same V_{lsr} : ambiguity

Nakanishi & Sofue 2003 PASJ

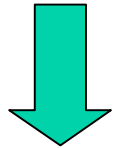


$R_T = R_0 \sin l$: subcentral (tangent) point. Maximum V_{lsr} long l.o.s.

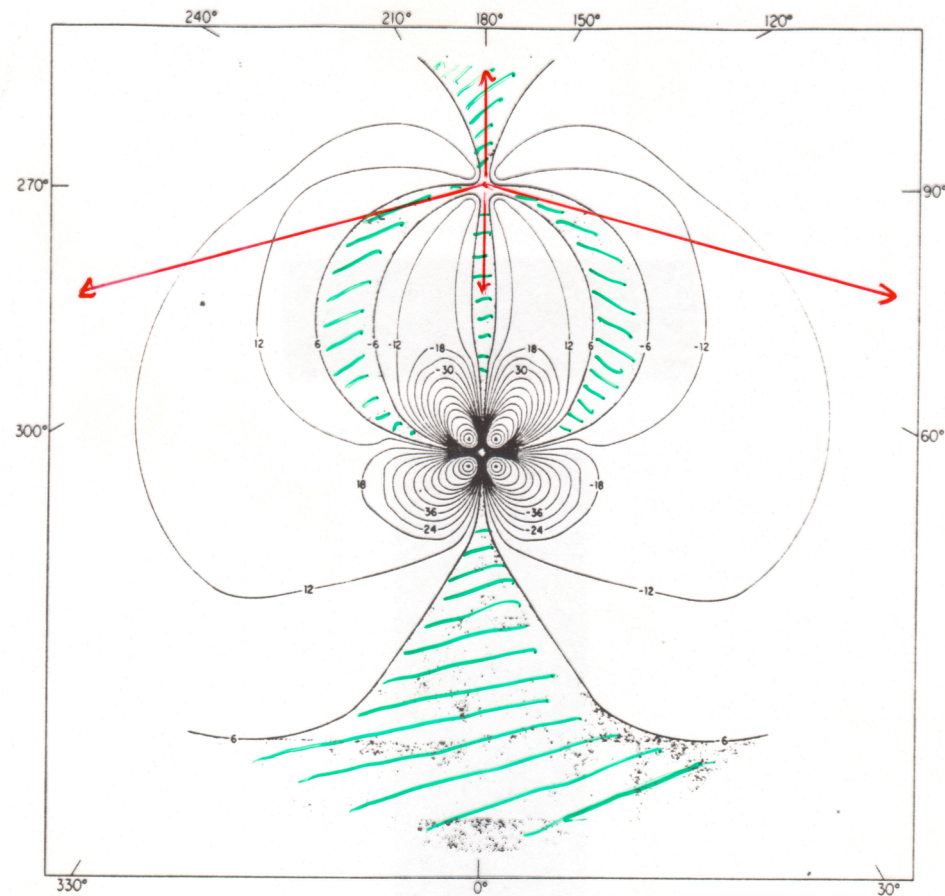
Velocity crowding

Contours of dV/dr

Arched in green:
 $dV/dr \leq 6 \text{ km/s/kpc}$



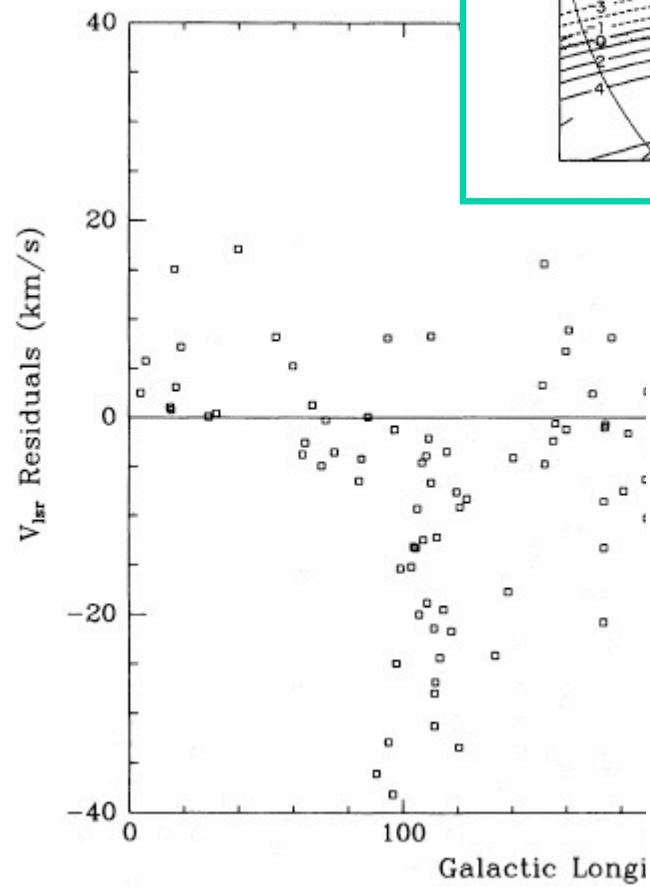
Artificial density structures



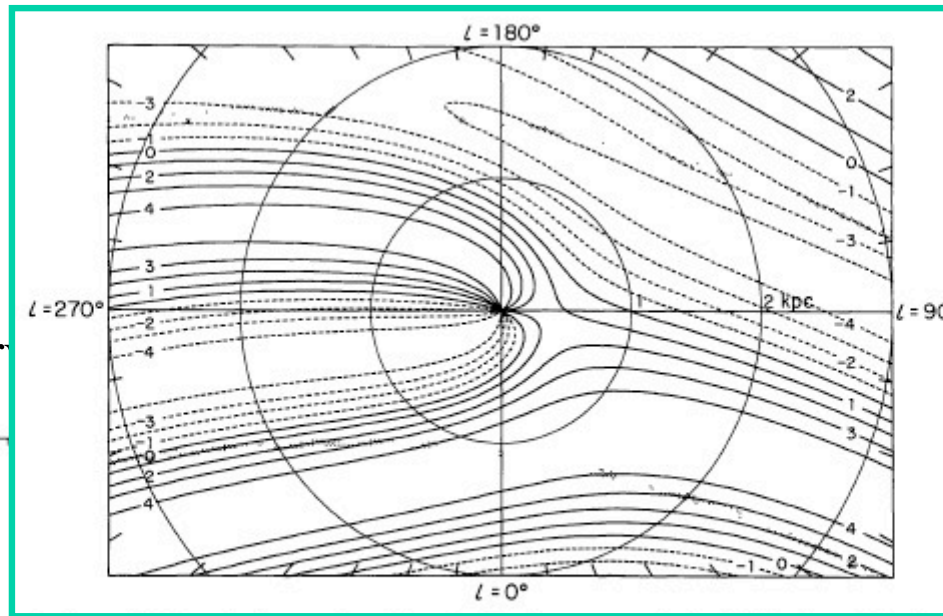
(Burton 1988)

(Burton & Bania 1974)

V_{lsr} - residuals: obser

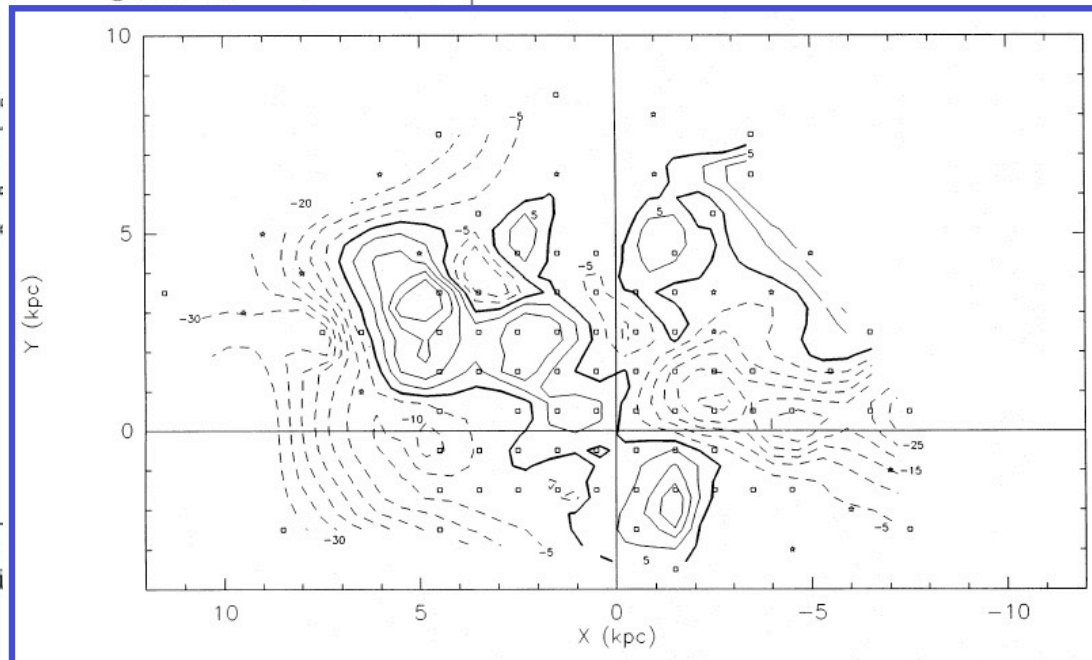


(Brand & Blitz 1993)

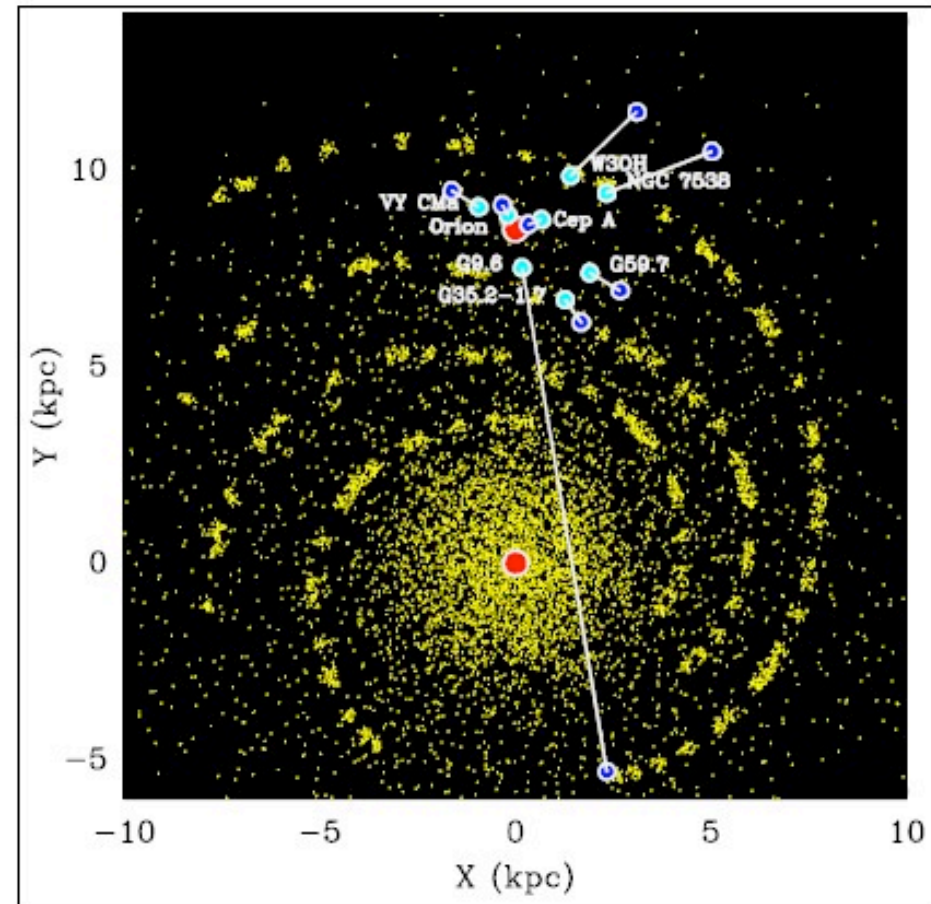
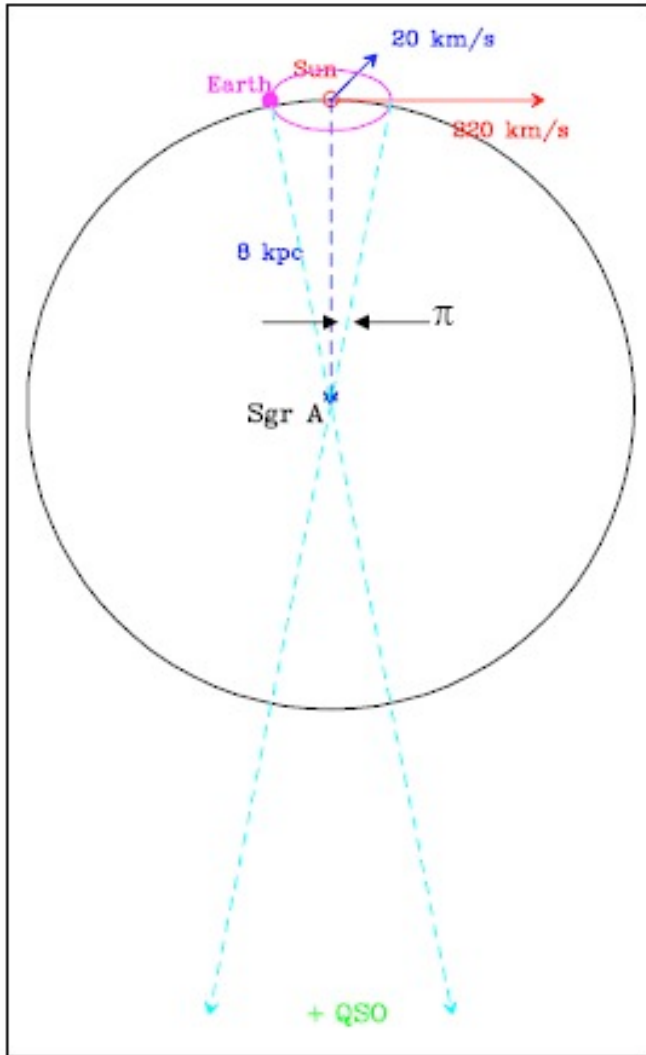


HI: V-residuals

CO: Streaming motions pattern

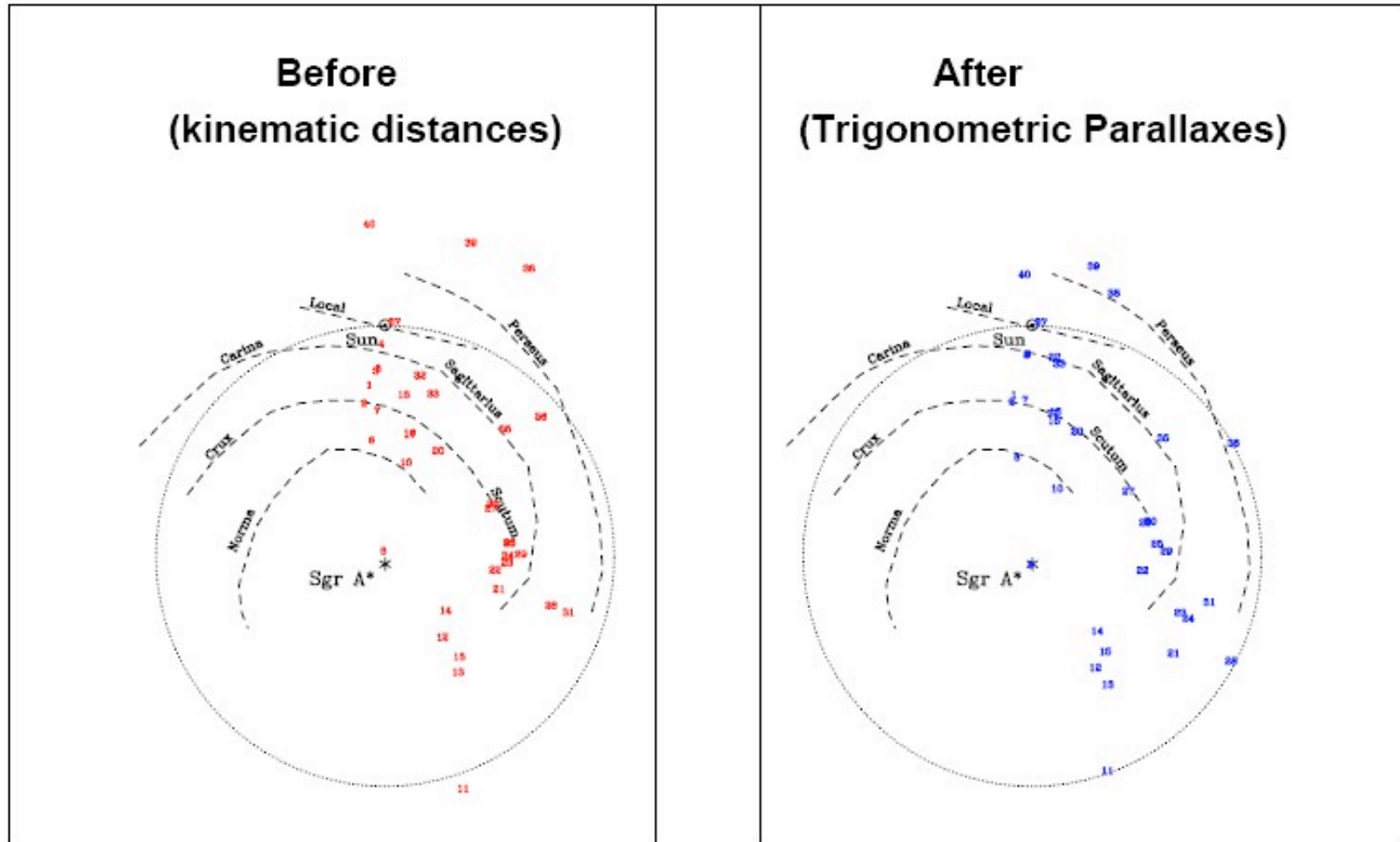


Trigonometric parallax



(Reid – IAU242, 2007; ApJ 700, 137 2009)

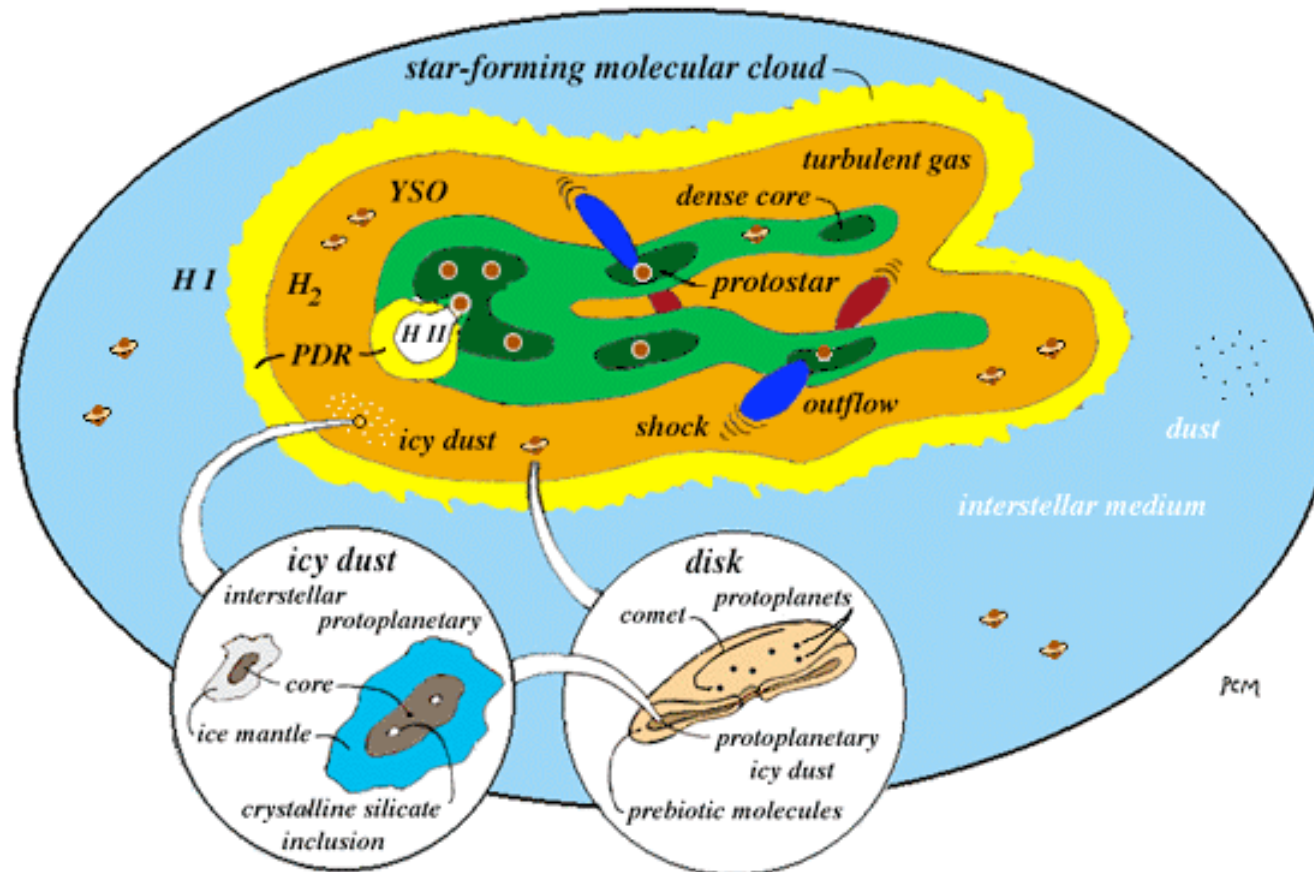
The new Galaxy



(Reid - IAU242, 2007; 2009)

STAR FORMATION

Star formation: in molecular clouds



Star formation catastrophe?

$M_{\text{cloud}} \approx 10^{4-5} M_{\odot} \gg M_{\text{Jeans}} \approx 10^2 M_{\odot} \Rightarrow$ collapse on
free-fall timescale $t_{\text{ff}} \approx \sqrt{(3\pi/32G\rho)} \approx 10^6 \text{ yrs.}$

On galactic scale:

$$\text{SFR} = M_{\text{GMC}} / t_{\text{ff}} \approx 10^9 M_{\odot} / 10^6 \text{ yrs} \approx 10^3 M_{\odot} / \text{yr}$$

$$\gg \text{SFR}_{\text{obs}} \approx 3 M_{\odot} / \text{yr}$$

Clouds are prevented from total collapse!

SFE: Star formation efficiency

TABLE 2 Star-formation efficiencies for nearby embedded clusters

Cluster name	Core mass (M_{\odot})	Stellar mass (M_{\odot})	SFE	References
Serpens	300	27	0.08	Olmi & Testi 2002
Rho Oph	550	53	0.09	Wilking & Lada 1983
NGC 1333	950	79	0.08	Warin et al. 1996
Mon R2	1000	341	0.25	Wolf et al. 1990
NGC 2024	430	182	0.33	E.A. Lada et al. 1991a,b
NGC 2068	266	113	0.30	E.A. Lada et al. 1991a,b
NGC 2071	456	62	0.12	E.A. Lada et al. 1991a,b

Cloud support

Virial theorem: $2T + 2U + W + M = 0$

The equation $2T + 2U + W + M = 0$ is shown with each term circled in red. Four red arrows originate from the circles: one from '2T' pointing to 'Kinetic energy', one from '2U' pointing to 'Thermal energy', one from 'W' pointing to 'Gravitational energy', and one from 'M' pointing to 'Magnetic field term'.

Gravitational energy

Thermal energy (random motions): $U/W \approx 3 \times 10^{-3} \rightarrow$ irrelevant

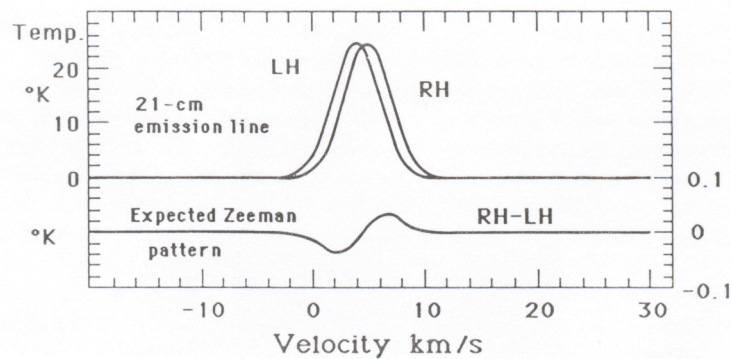
Magnetic field term: $M/W = 0.3$

Kinetic energy (bulk motions, mostly from clumps): $T/W \approx 0.5$

Clouds are supported by turbulence and magnetic fields

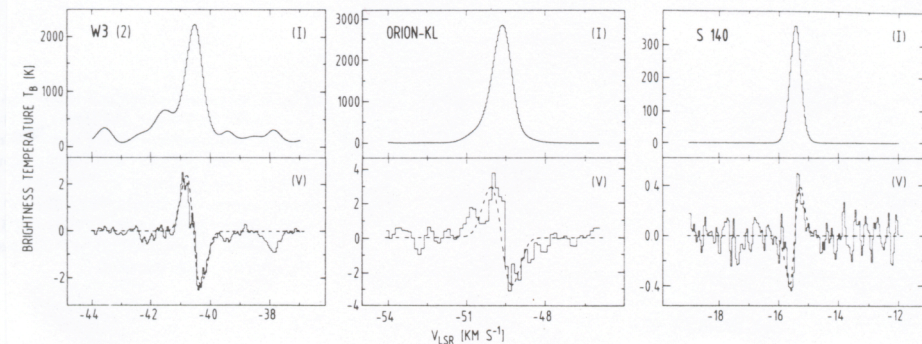
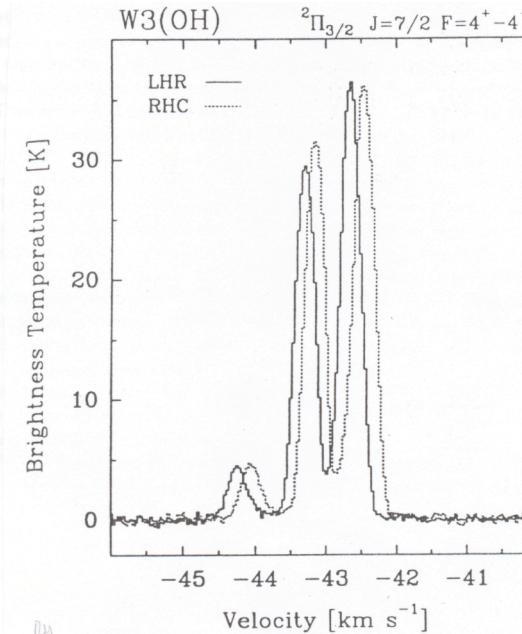
B-field: Zeeman splitting

In presence of B-field, hyperfine splitting of levels is modified: spectral line splits in 2, centered on primary component, with opposing polarisations.



$$\frac{\Delta \nu_{\text{mag}}}{\Delta \nu_{\text{therm}}} \approx 10^{-3} \left(\frac{B}{\mu\text{G}} \right) \left(\frac{T_k}{10\text{K}} \right)^{-1/2}$$

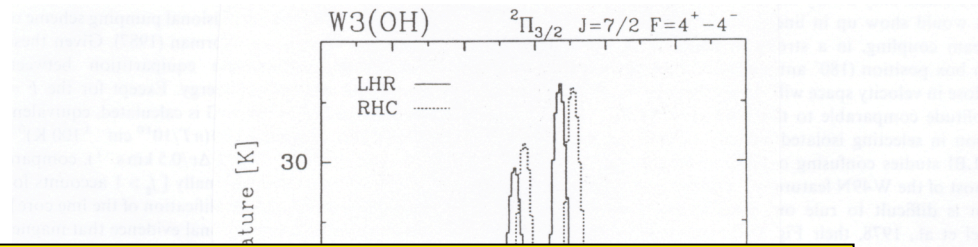
3.27 Hz/ μG OH @ 1665 MHz
 1.96 Hz/ μG OH @ 1665 MHz
 $7.2 \cdot 10^{-4}$ Hz/ μG NH₃ @ 22 GHz
 $2.3 \cdot 10^{-3}$ Hz/ μG H₂O @ 22 GHz



Güsten et al. 1994

B-field: Zeeman splitting

In presence of B-field, hyperfine splitting of levels is modified:
spectral line splits in 2, centered on primary component, with opposing pol



Measured values:

HI 21cm, OH 18cm: few μG (diffuse ISM; $n < 100 \text{ cm}^{-3}$)

few μG (dark cloud envelopes; $n \sim 10^3 \text{ cm}^{-3}$)

few μG (OH masing layers; $n \sim 10^{7-8} \text{ cm}^{-3}$)

H₂O 22GHz: 50mG (maser spots; $n \sim 10^{10} \text{ cm}^{-3}$)

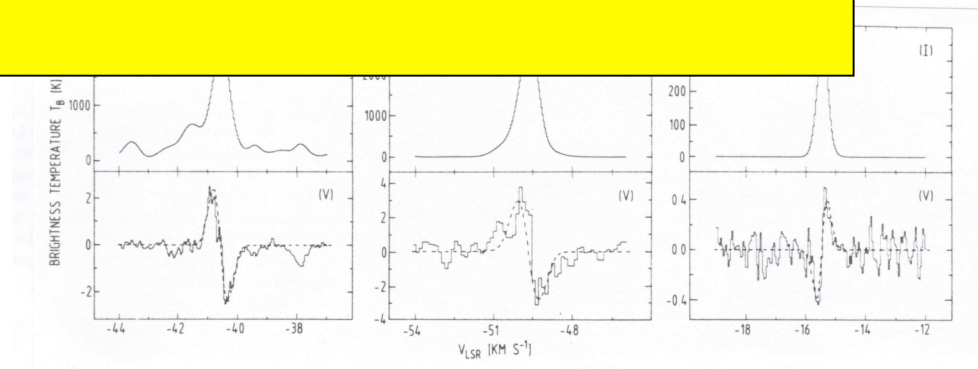
$$\frac{\Delta \nu_{\text{mag}}}{\Delta \nu_{\text{therm}}} \approx 10^{-3} \left(\frac{B}{\mu\text{G}} \right) \left(\frac{T_k}{10\text{K}} \right)$$

3.27 Hz/ μG OH @ 1665 MHz

1.96 Hz/ μG OH @ 1665 MHz

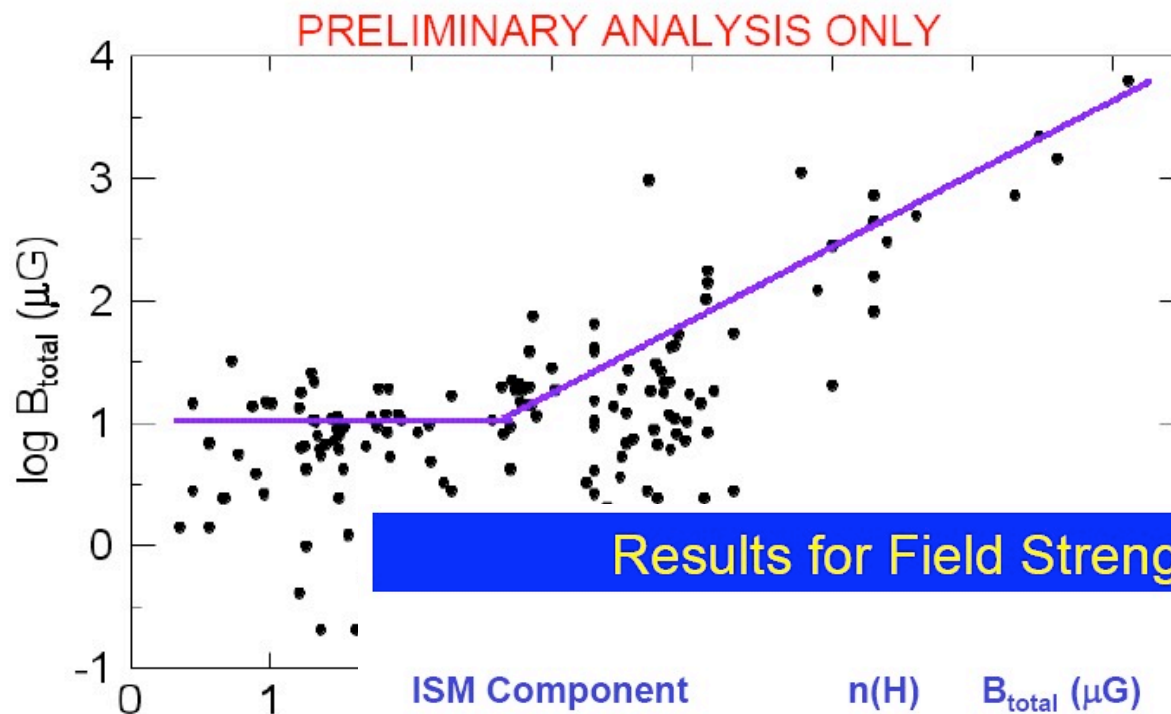
$7.2 \cdot 10^{-4}$ Hz/ μG NH₃ @ 22 GHz

$2.3 \cdot 10^{-3}$ Hz/ μG H₂O @ 22 GHz



Güsten et al. 1994

Results for Field Strength



Results for Field Strength

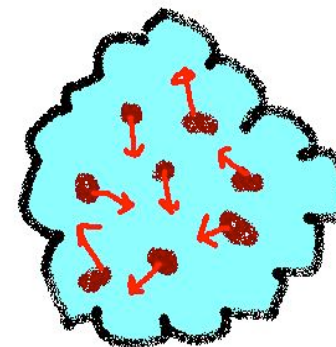
ISM Component	$n(\text{H})$	B_{total} (μG)	λ_{C}	κ ($B \propto n^{\kappa}$)
diffuse ionized medium (synchrotron equipartition, RMs)	~ 0.1	7 ± 3	-	} ~ 0
H I clouds (H I Zeeman)	~ 50	6 ± 2	~ 0.1	
molecular clouds (OH, CN Zeeman)	$10^3\text{--}10^7$	$10\text{--}3,000+$	~ 1	~ 0.5

(Crutcher – IAU242, 2007)

Clump stability

Forces working on clumps:

- Clump (self-) gravity
- Clump turbulence (and thermal pressure)
- Interclump pressure
- Magnetic fields



Clump virial theorem (e.g. Fleck 1988):

$$4\pi r^3 P = 3M_{\text{CO}}\sigma^2 - GM_{\text{CO}}^2/r + B^2/8\pi$$

Expressed in pressures:

$$P/k = \rho\sigma^2/k - GM_{\text{CO}}\rho/3rk + B^2/8\pi k$$

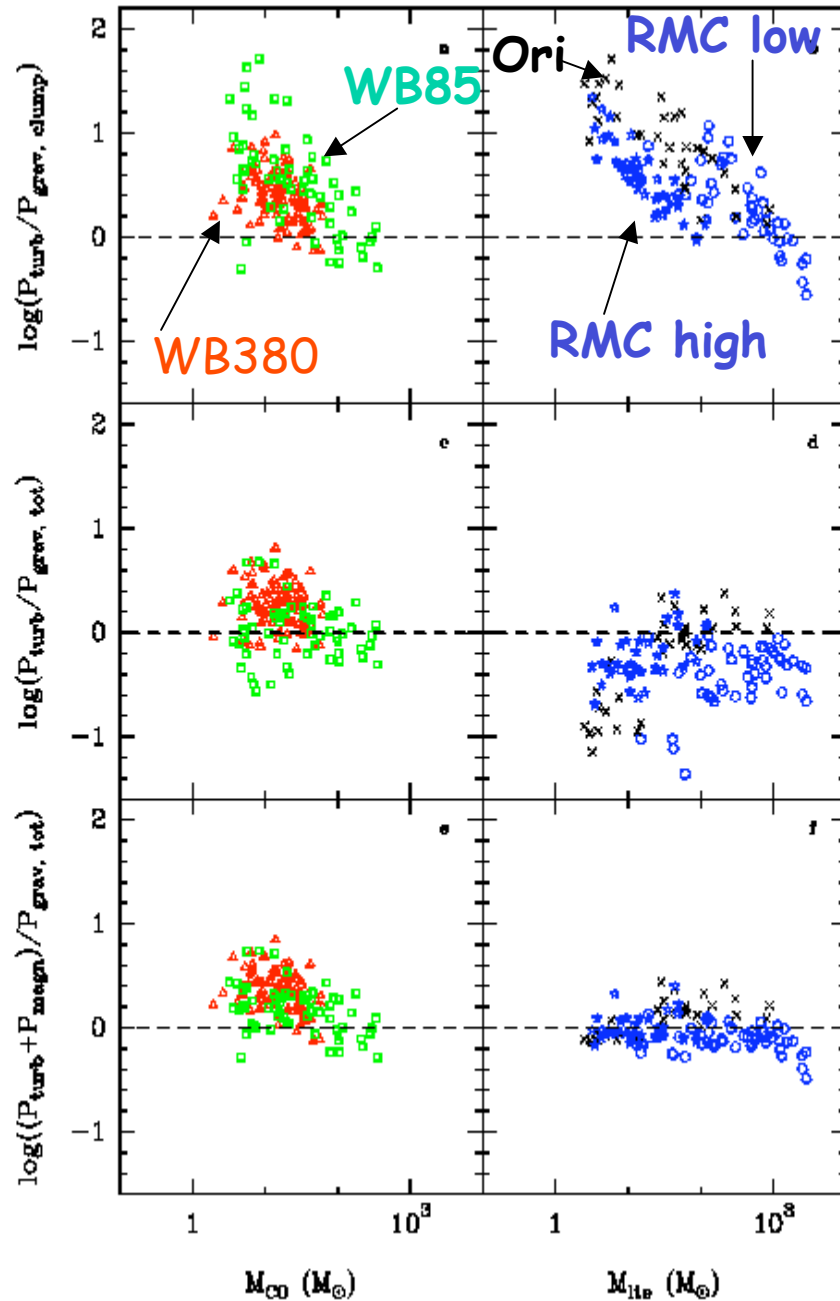
$$P_{\text{ext}}/k = P_{\text{turb}}/k + P_{\text{grav}}/k + P_{\text{magn}}/k$$

$$P_{\text{turb}}/P_{\text{grav}} = \alpha = 126 r[\text{pc}] \Delta v[\text{kms}^{-1}]^2 / M_{\text{CO}} = M_{\text{vir}}/M_{\text{CO}} : \text{virial parameter}$$

$$P_{\text{magn}}/k = 2.9 \times 10^4 \text{ Kcm}^{-3} \text{ for } 10\mu\text{G}$$

Interclump pressure (self-gravity GMC): $P_{\text{ext}}/k = 1.7 \times 10^4 - 5.9 \times 10^4 \text{ Kcm}^{-3}$

Clump pressure ratios



Turbulence
&
gravity

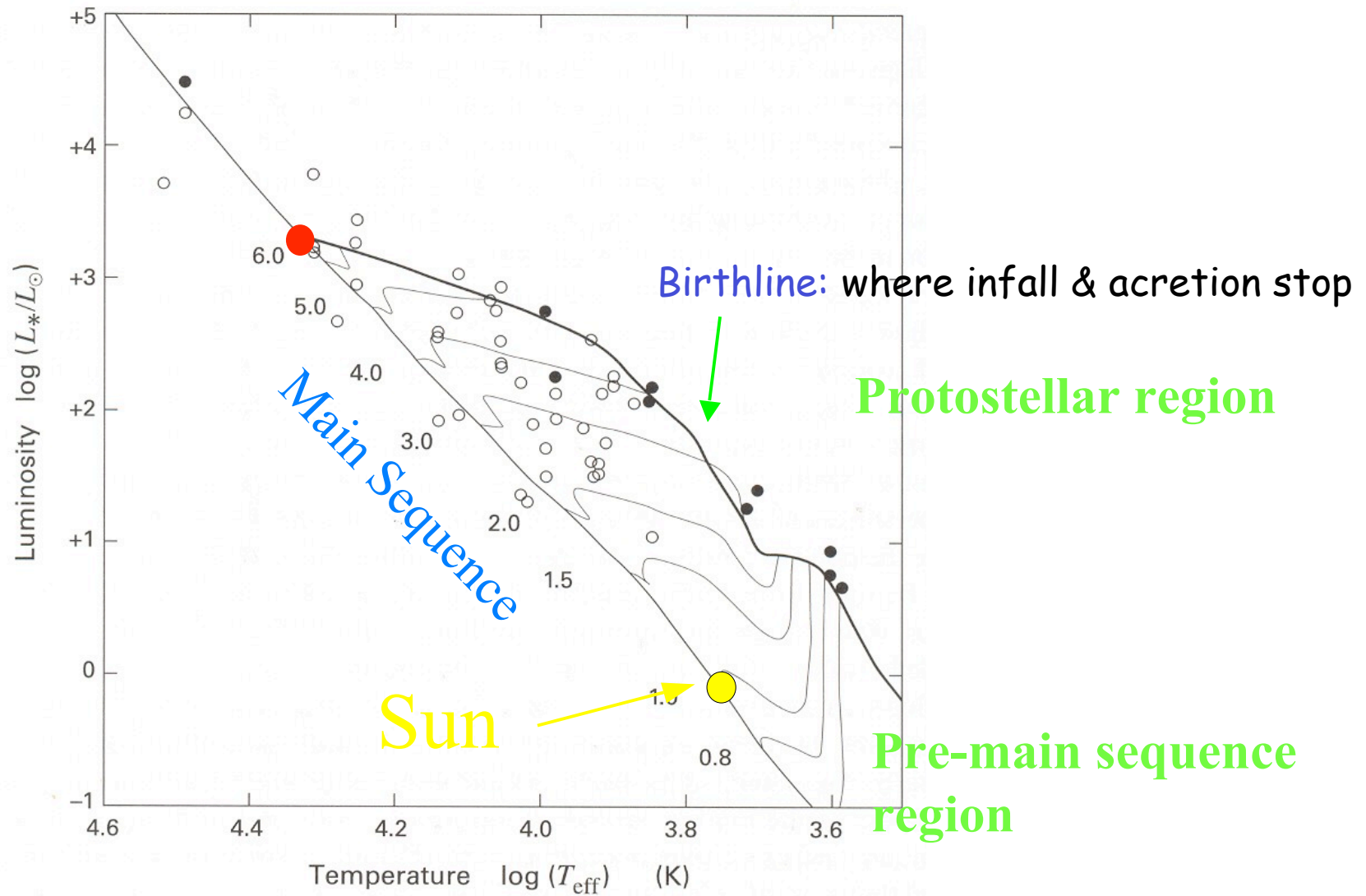
Turbulence
&
total gravity

Turbulence,
total gravity
&
magnetic field
pressure

Brand et al. 2001

Herzsprung-Russel diagram

Palla & Stahler (1990)



Normal star: evolutionary status determined by location HRD:

L, T_{eff}

Embedded YSOs: associated with natal gas & dust

Cannot be placed in HRD

Protostellar stage: circumstellar gas & dust:

absorbs and reprocesses radiation embedded object

Has extent \gg stellar photosphere \rightarrow dust has wide range of T

SED wider than single- T BB;

shape SED depends on nature & distribution of circumstellar material

More evolved object (pre-ms, ms): envelope, disk almost gone

Shape of SED is $f(\text{evolutionary state})$

Observationally:

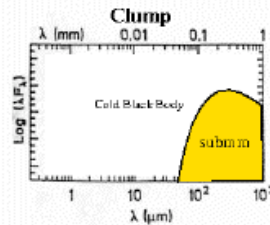
YSOs fall into 4 classes, based on shape of SED

Infrared/Submillimeter Young Stellar Object Classification

(Lada 1987 + André, Ward-Thompson, Barsony 1993)

Stars < 8M_O

sub-mm



Beginning of gravitational collapse

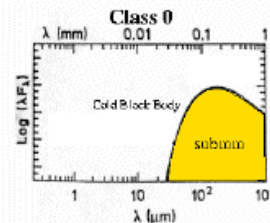
Prestellar dense core

~ 1 000 000 yr

unstable **isothermal** clump

Embedded phase

far-IR



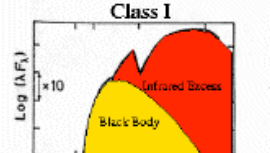
Submillimeter Protostar

< 10 000 yr

Class 0

accretion onto protostar

near-IR



Infrared Protostar

~ 100 000 yr

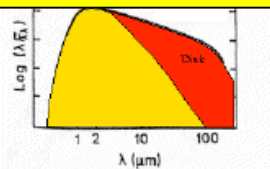
formation of **disk** & **outflow**

Birthline

disk without accretion

optical

+NIR



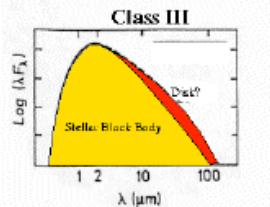
T Tauri (CTTS)

~ 1 000 000 yr

Class II

protoplanetary disk

optical



Evolved T Tauri (WTTS)

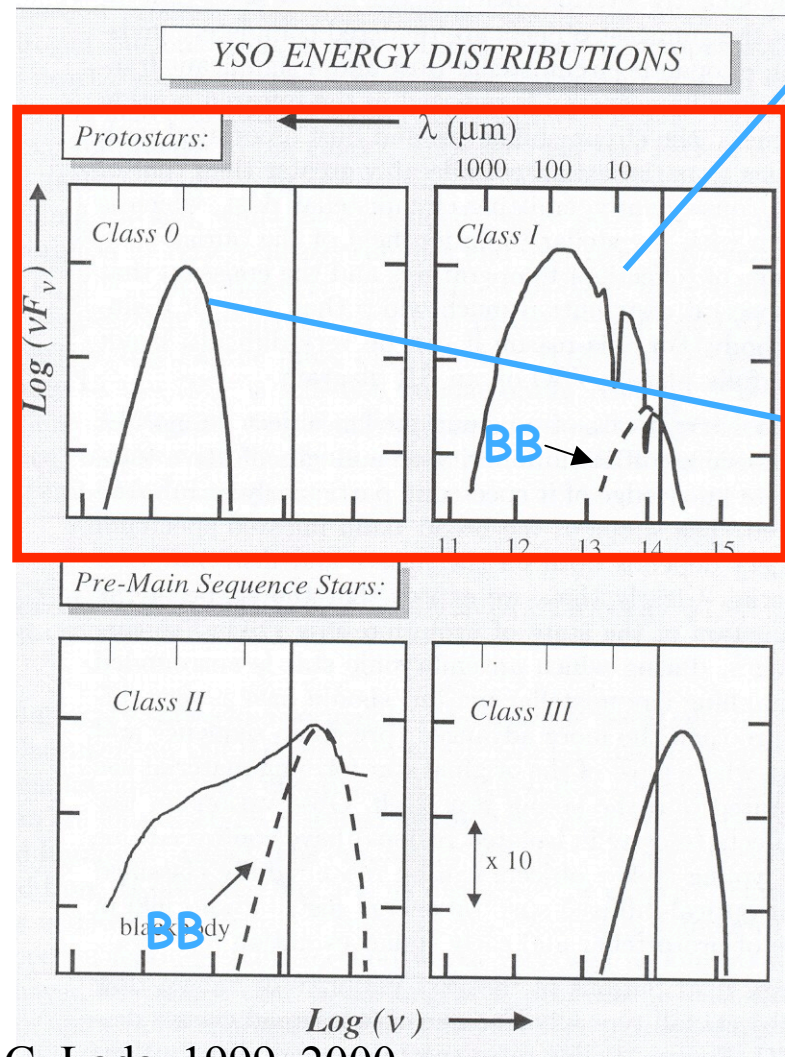
~ 10 000 000 yr

Class III

Revealed phase

Time

Embedded phase: protostars



C. Lada, 1999, 2000

Class I:

- SED broader than single-T BB
- At $\lambda > 2\mu\text{m}$ SED rises with λ :
huge IR-excess
- Deeply embedded; detected in NIR (freq. assoc'd with RNe)
- Often associated with outflows
- $M_{\text{circumst}}(r < 1000\text{AU}) \ll M_*$
- Age ca. $1-5 \times 10^5$ yrs

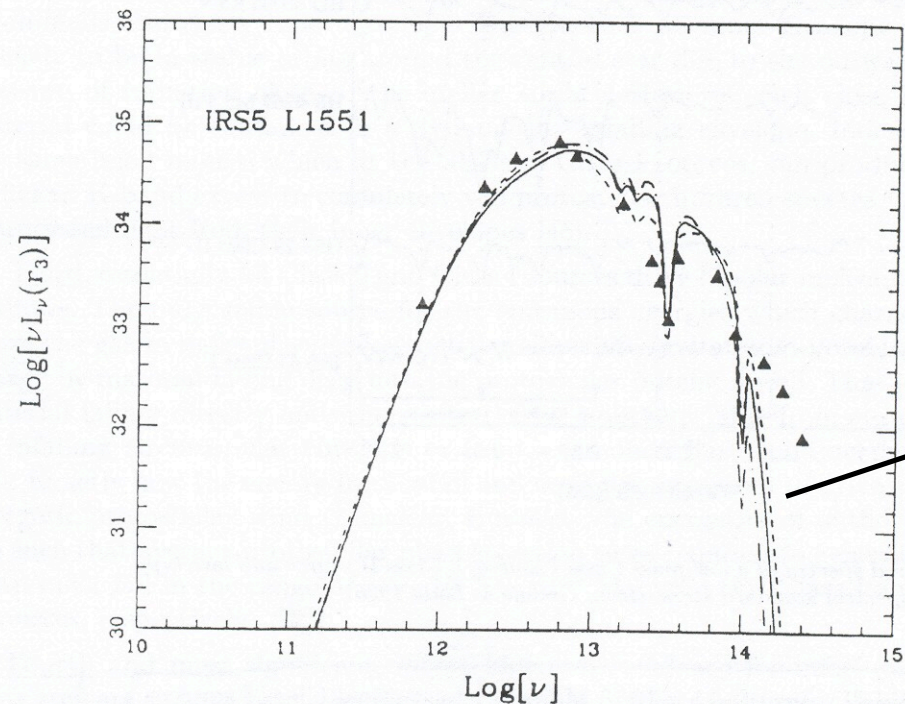
Class 0:

- Much more extincted & embedded;
- SED peak in submm;
not detected at $\lambda < 20\mu\text{m}$
- SED similar to BB at $T = 20-30\text{K}$
- All have energetic, v. highly collimated outflows.
- $M_{\text{circumst}}(r < 1000\text{AU}) \approx M_*$
- Constitute 10% of embedded sources
- Age ca. 10^4 yrs

Protostellar nature embedded YSOs: evidence

Protostar: objects in process of accumulating into star-like configuration the bulk of the material they will contain as ms stars

- 1) SED can be modeled as embryonic stellar core + circumstellar disk + massive gas & dust envelope with density structure as predicted by theory for stellar cloud cores.



fits: rotating-collapsing
isothermal protostellar models
Mass infall rate $\sim 5 \times 10^{-6} M_\odot$ /yr

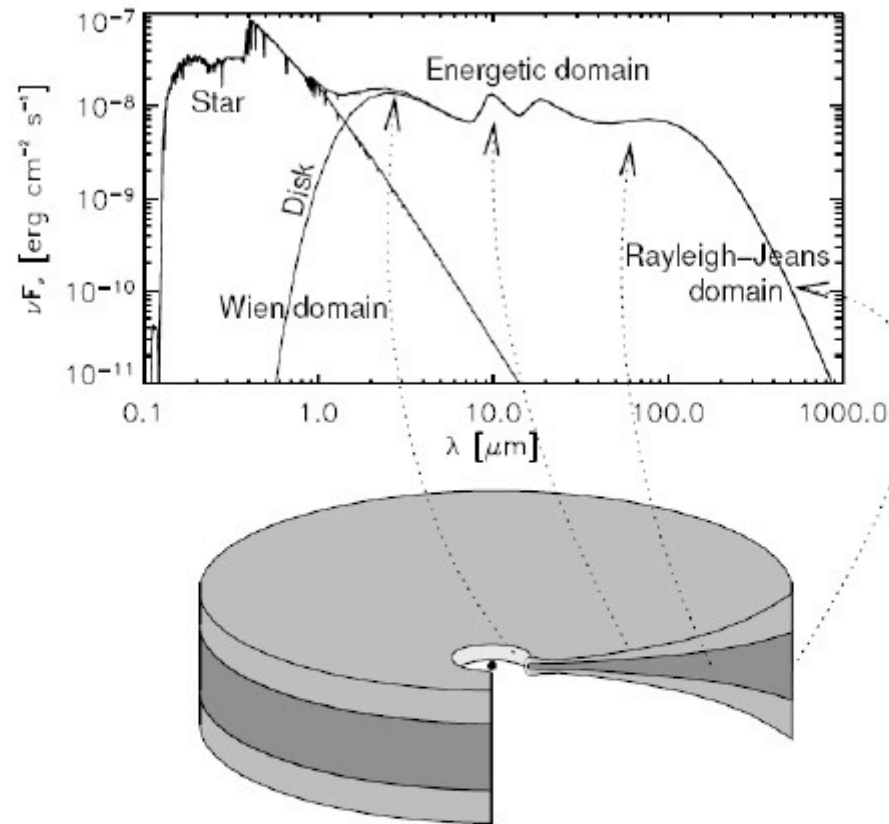


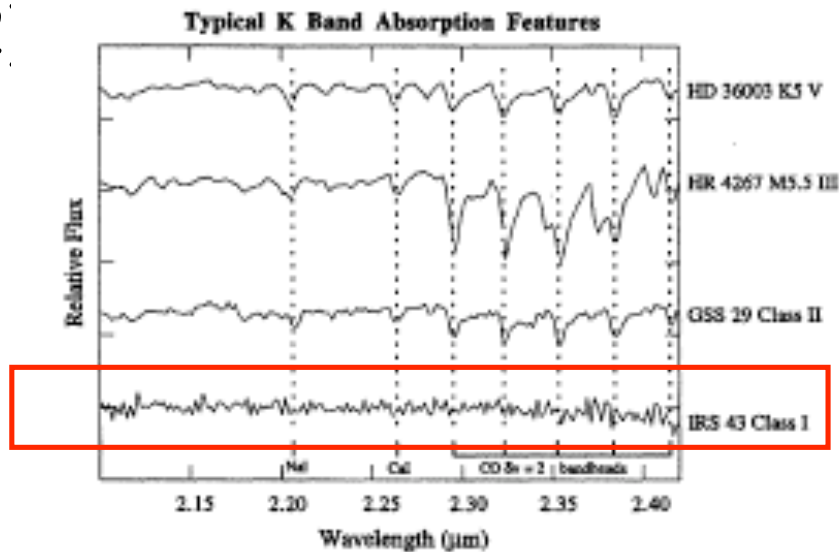
Figure 1.2: From Dullemond et al. (2006). Build-up of the SED of a flaring circumstellar disk and the origin of various components: the near infrared bump is supposed to originate in the puffed-up inner rim, the infrared dust features (as the silicate ones between $10\mu\text{m}$ and $20\mu\text{m}$) from the warm surface layer, and the underlying continuum from the deeper and cooler disk regions. Typically the near and mid-infrared emission comes from small radii, while the far-infrared and the millimeter emission come from the outer disk regions.

Isella 2006: Dullemond et al. 2006

Protostellar nature embedded YSOs: evidence

- 1) SED can be modeled as embryonic stellar core + circumstellar disk + massive gas & dust envelope with density structure as predicted by theory for rotating, infalling protostellar cloud cores.

2



as hot dust at $\ll 1\text{AU}$
due to 'veil' absorption
' that.

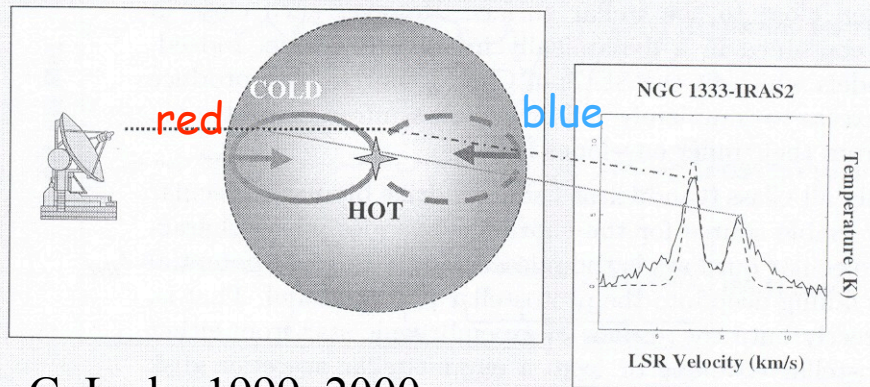
FIG. 1. K-band absorption features. The indicated Na I, Ca I, and CO features are commonly seen in the spectra of late-type stars such as the typical MK standards HD 36003 and HR 4267. Class II (and III) YSOs (such as GSS 29 shown) usually show similar features, but Class I YSOs (such as IRS 43 shown) usually do not show any early- or late-type features. The data shown are enlarged subregions of spectra presented in Appendix, but baseline continuum slopes have been removed.

Greene & Lada, AJ 1996

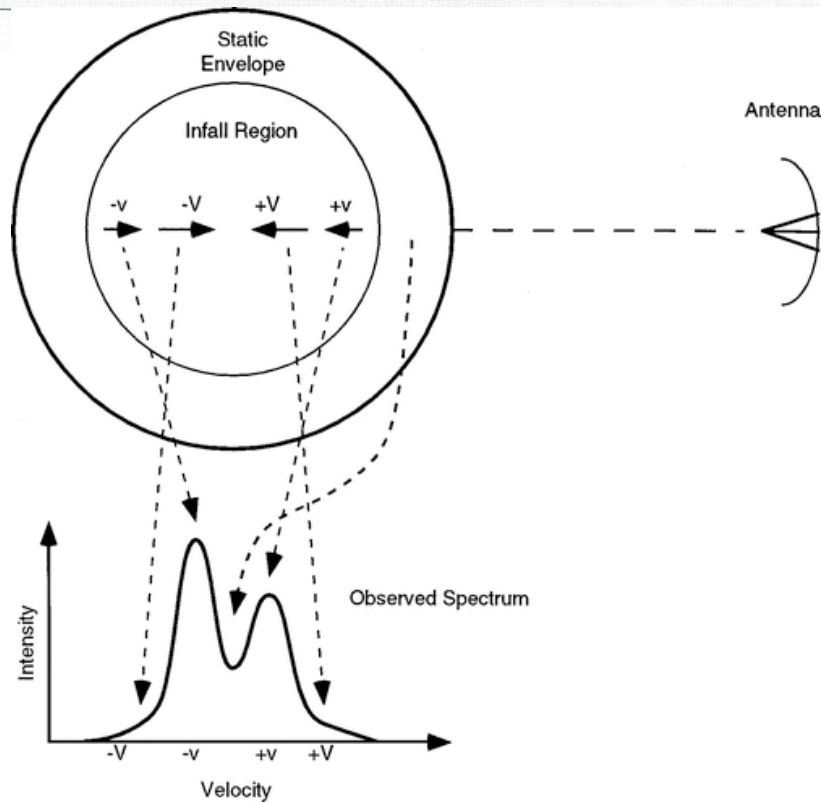
Protostellar nature embedded YSOs: evidence

- 1) SED can be modeled as embryonic stellar core + circumstellar disk + massive gas & dust envelope with density structure as predicted by theory for rotating, infalling protostellar cloud cores.
- 2) Featureless spectrum, requires hot dust at $\ll 1\text{AU}$ to provide additional cont. flux to 'veil' absorption lines. Infall models account for that.
- 3) Only viable source for outflow energy is gravity (from infall).
- 4) Direct kinematic evidence for infall motions found in Class 0 sources!

Kinematic Signature of Protostellar Infall



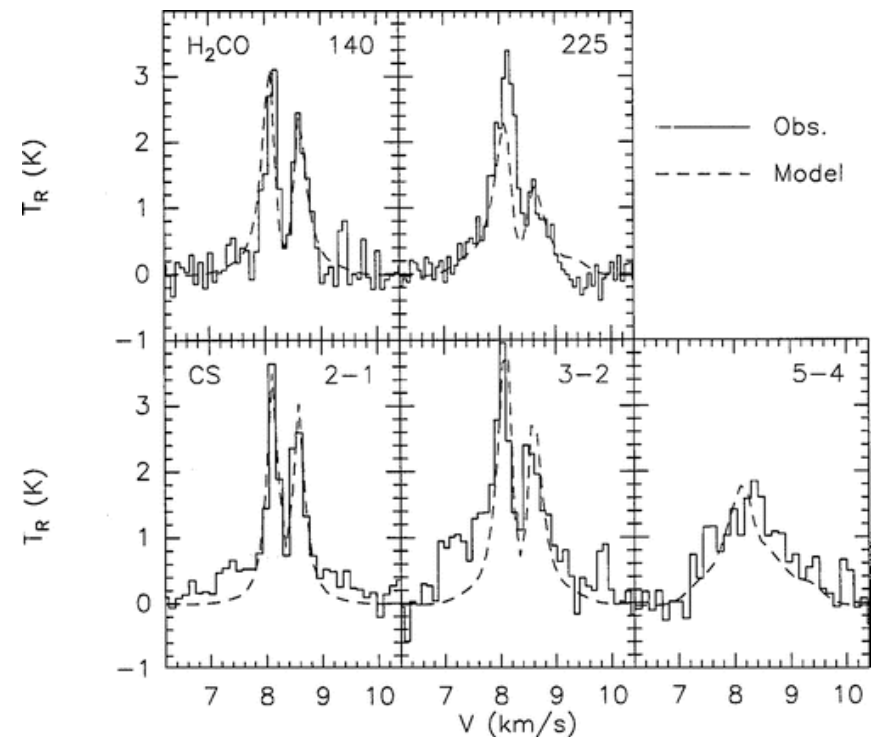
C. Lada, 1999, 2000



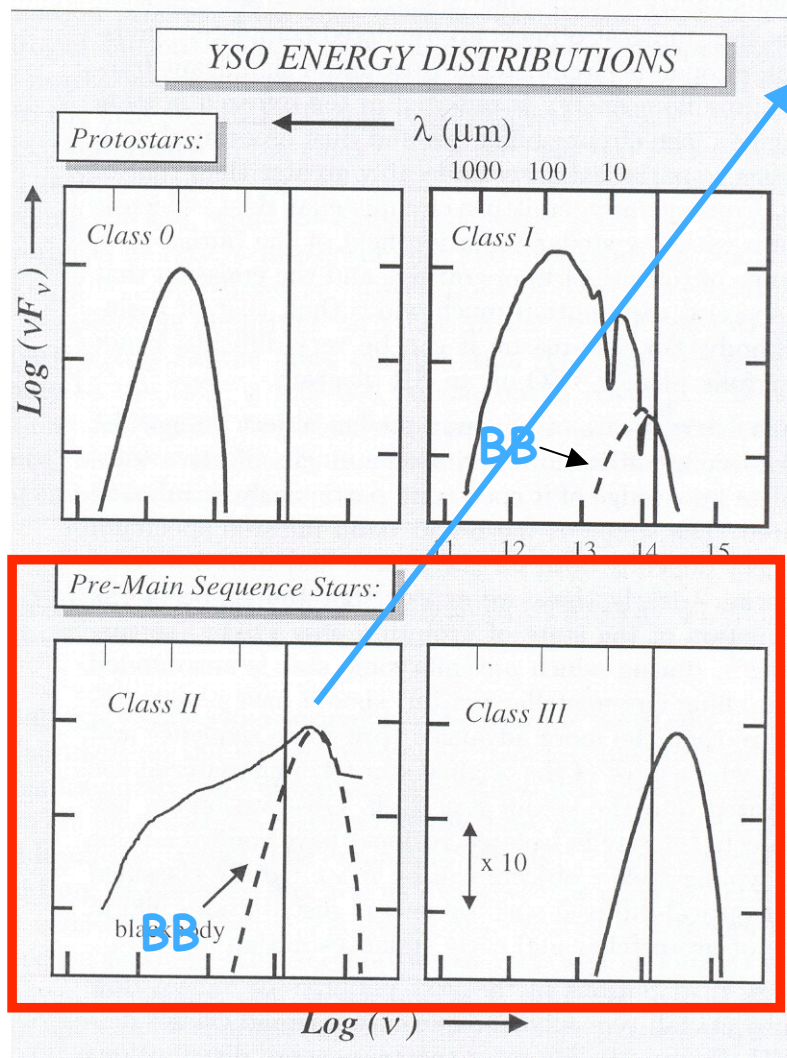
Protostellar infall

Detecting infall from
opt. thick line

B335; Zhou et al. 1993



Revealed phase: Pre-ms stars



Class II:

- SED peaks in visible or NIR
- SED broader than single-T BB
- At $\lambda > 2\mu\text{m}$ SED falls with λ (power-law): **IR-excess, but smaller than Class I**
- Disk, but no massive envelope
- $M_{\text{disk}} \approx 0.01\text{-}0.1 M_{\odot}$
- Accretion rate $\sim 10^{-8} M_{\odot}/\text{yr}$
- in SFRs: 10x more than Class I
- in optical, Class II are CTTS

SED can be fitted with model of disk with T-gradient, reprocessing and reradiating light from central star

ClassII model fit

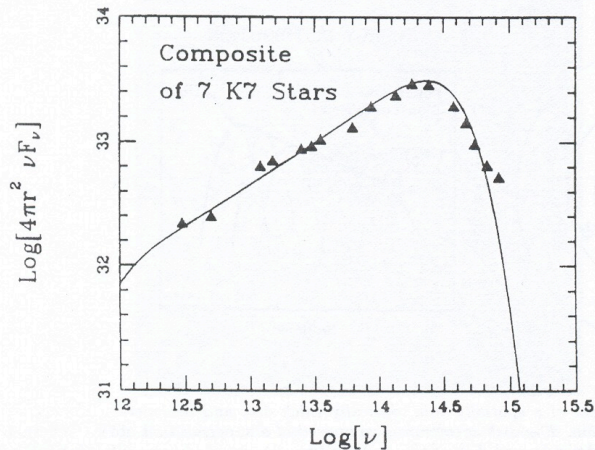


Figure 15. The composite SED of seven Class II stars along with that (solid line) of a model circumstellar disk. (From Adams, Lada and Shu 1988).

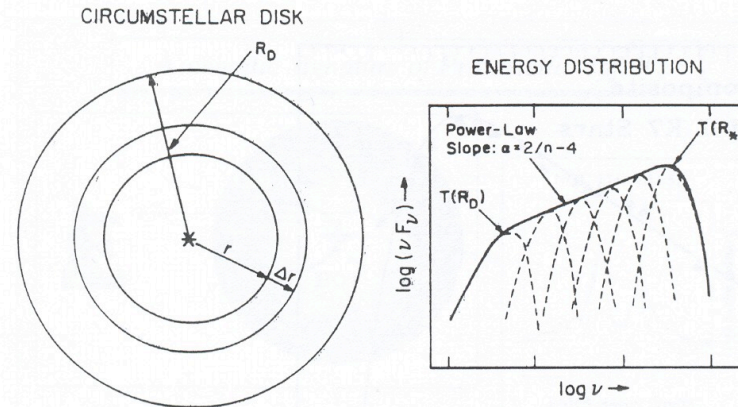


Figure 16. Schematic diagram of a spatially thin, optically thick disk and its emergent spectral energy distribution. The disk spectrum is composed of a superposition of blackbodies of varying temperature.

Disk: each annulus has area $2\pi R\Delta R$ and radiates as BB with $T(R)$

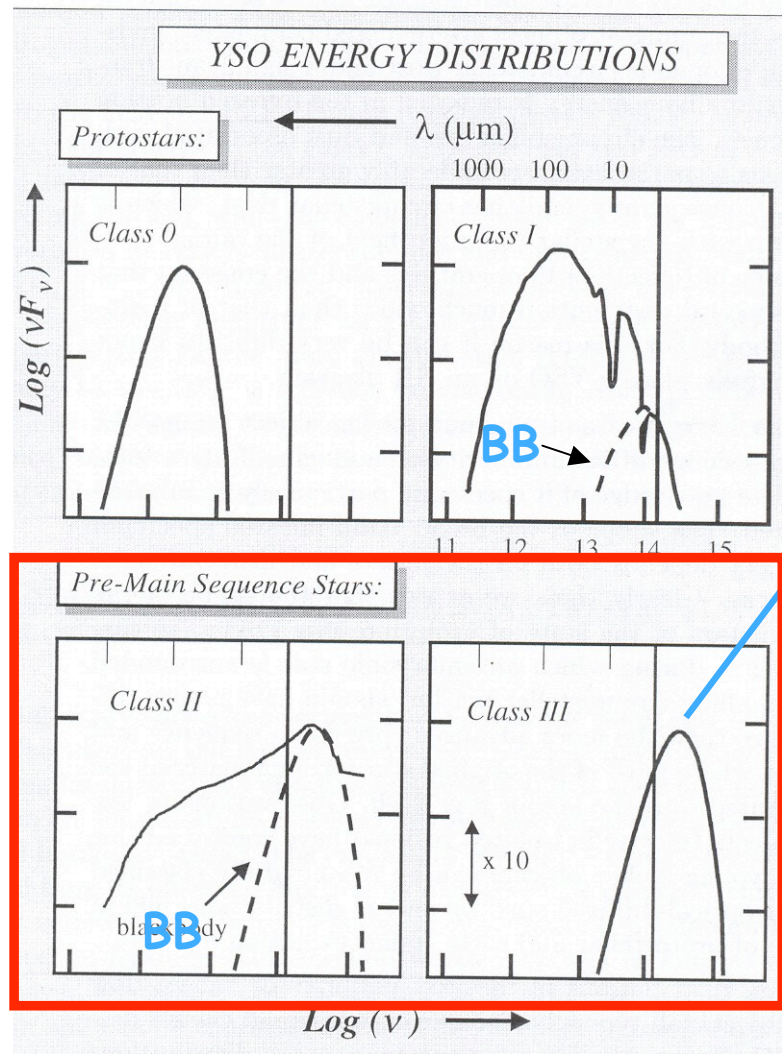
SED is superposition of series of BB-curves

If $T(R) \sim R^{-n}$, then (Wien's law) max. emission at $\nu \sim T(R) \sim R^{-n}$.

Luminosity each annulus: $L_\nu d\nu = 2\pi R\Delta R\sigma T(R)^4 \sim R^{2-3n}d\nu \sim \nu^{3-2/n}$.

For a SED, $\nu L_\nu \sim \nu^{4-2/n}$.

Revealed phase: Pre-ms stars



Class III:

- SED peak in visible/NIR
- SED similar to single-T BB; interpreted as photospheres of young stars with extinction.
- No significant amounts circumstellar gas, dust
- Class III are WTTS
- Age ca. $10^6 - 10^7$ yrs

No IR excess, confused with fore- & background stars in SFRs. But are X-ray sources.

Evolutionary sequence low-mass YSOs

Evolution Class 0 \Rightarrow I \Rightarrow II:

requires removal circumstellar material in infalling envelope

Evolution Class II \Rightarrow III:

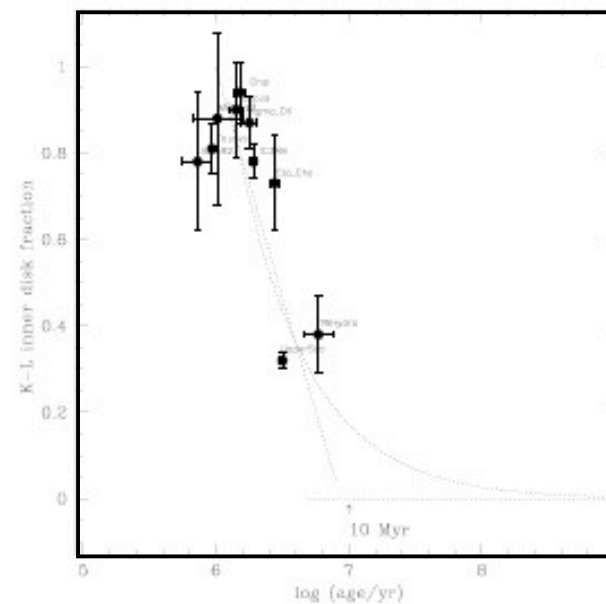
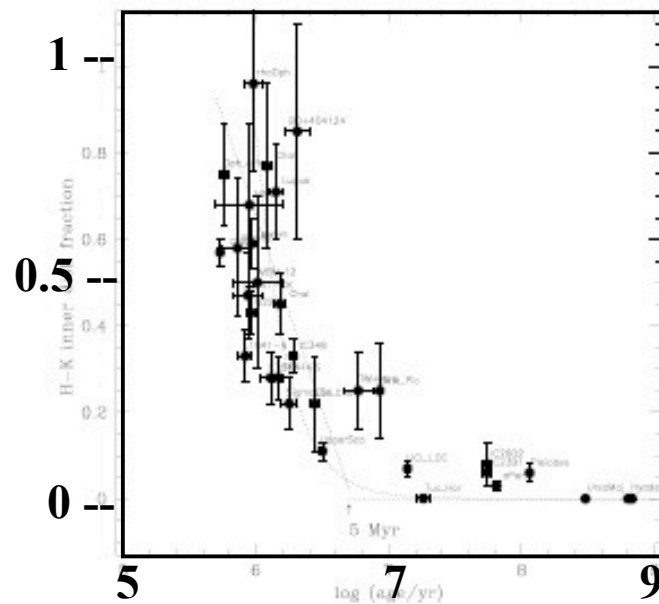
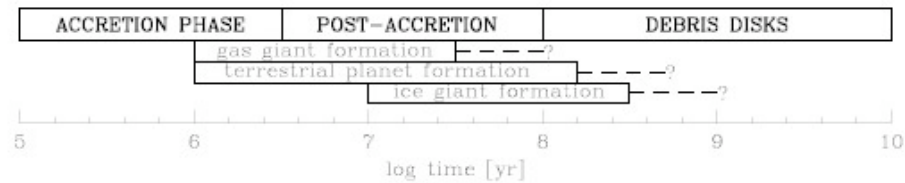
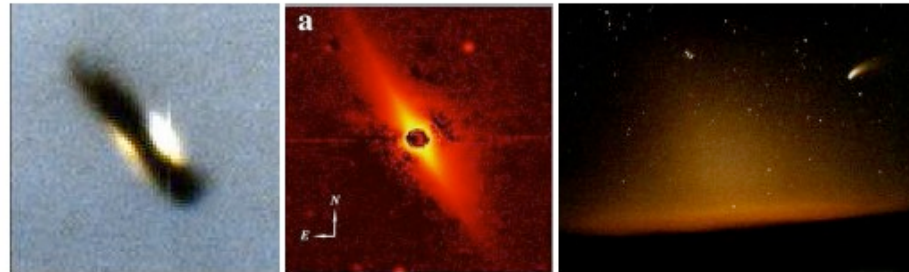
Requires clearing of circumstellar disk

Total accretion: NO - because SFE is very low ($M_{\star} \ll M_{\text{core}}$)

Therefore: very early on cloudy material physically removed
Most likely by bipolar outflows, originating from stellar wind
(virtually all Class 0,I drive molecular outflows).

A protostar can only gain mass if it loses mass at same time

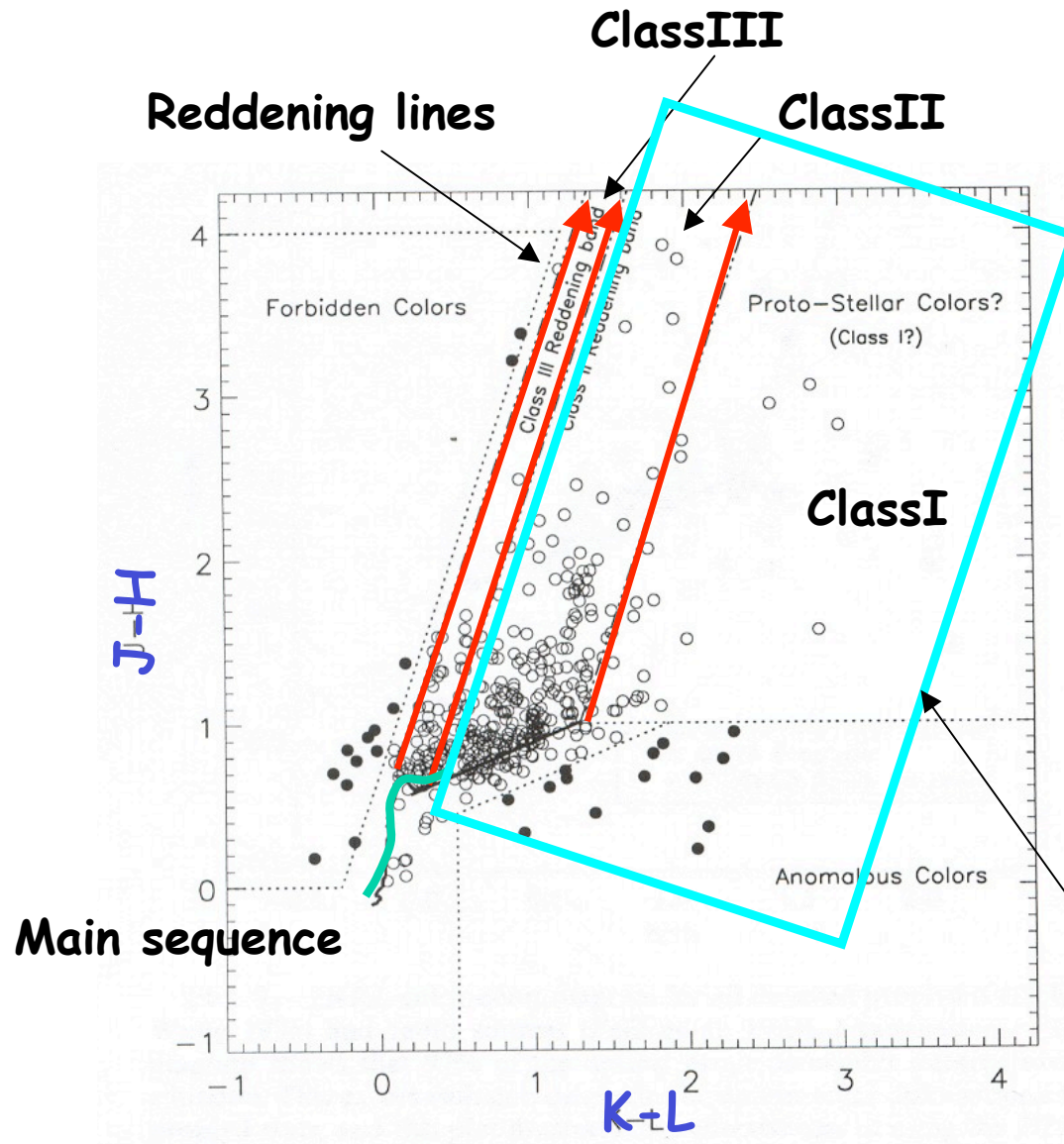
Disk lifetimes



Disk fraction vs. log(cluster age) for ca. 3500 stars, $0.3-1 M_{\odot}$

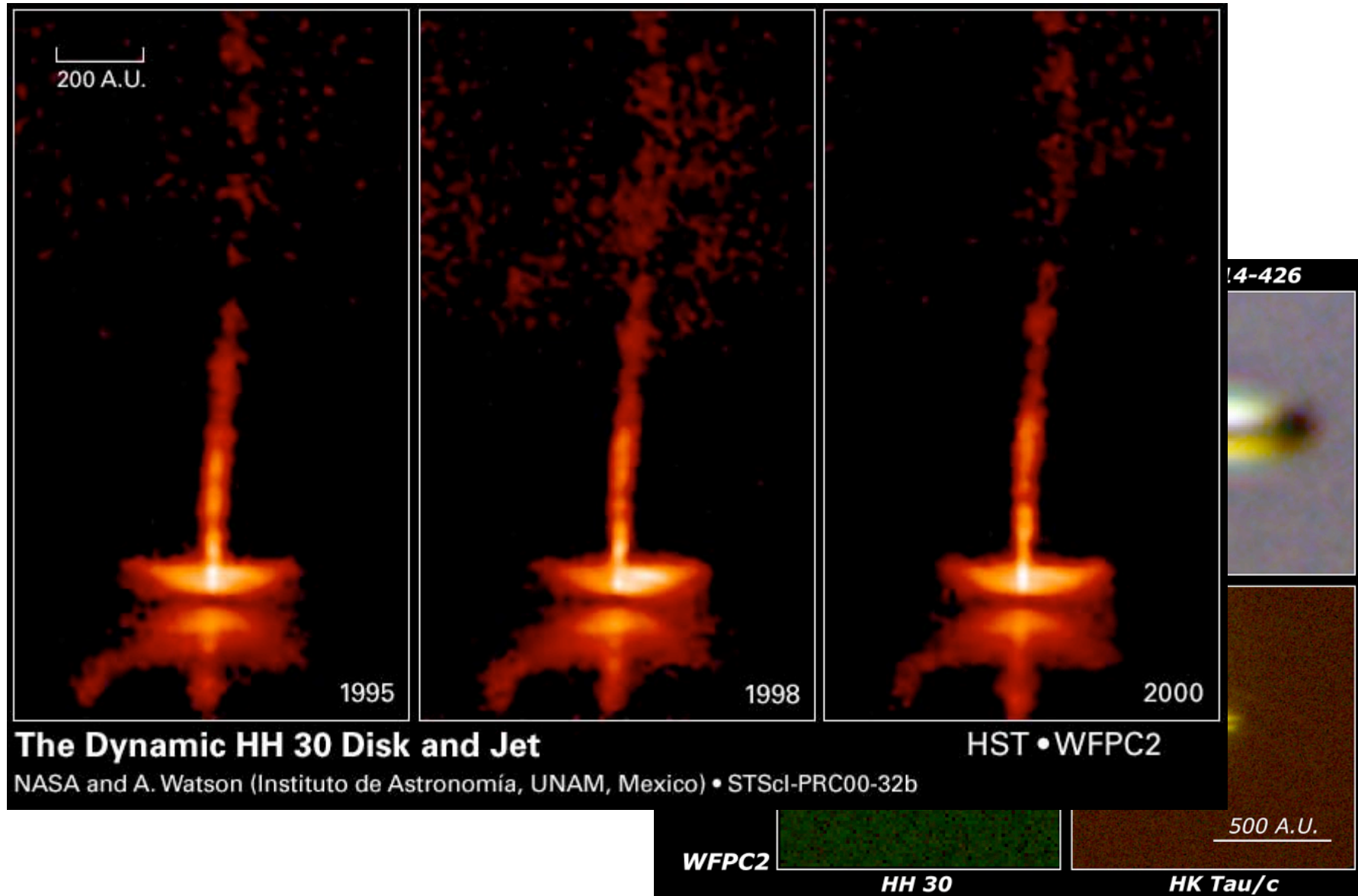
Hillenbrand 2006

YSOs: IR colour-colour diagram

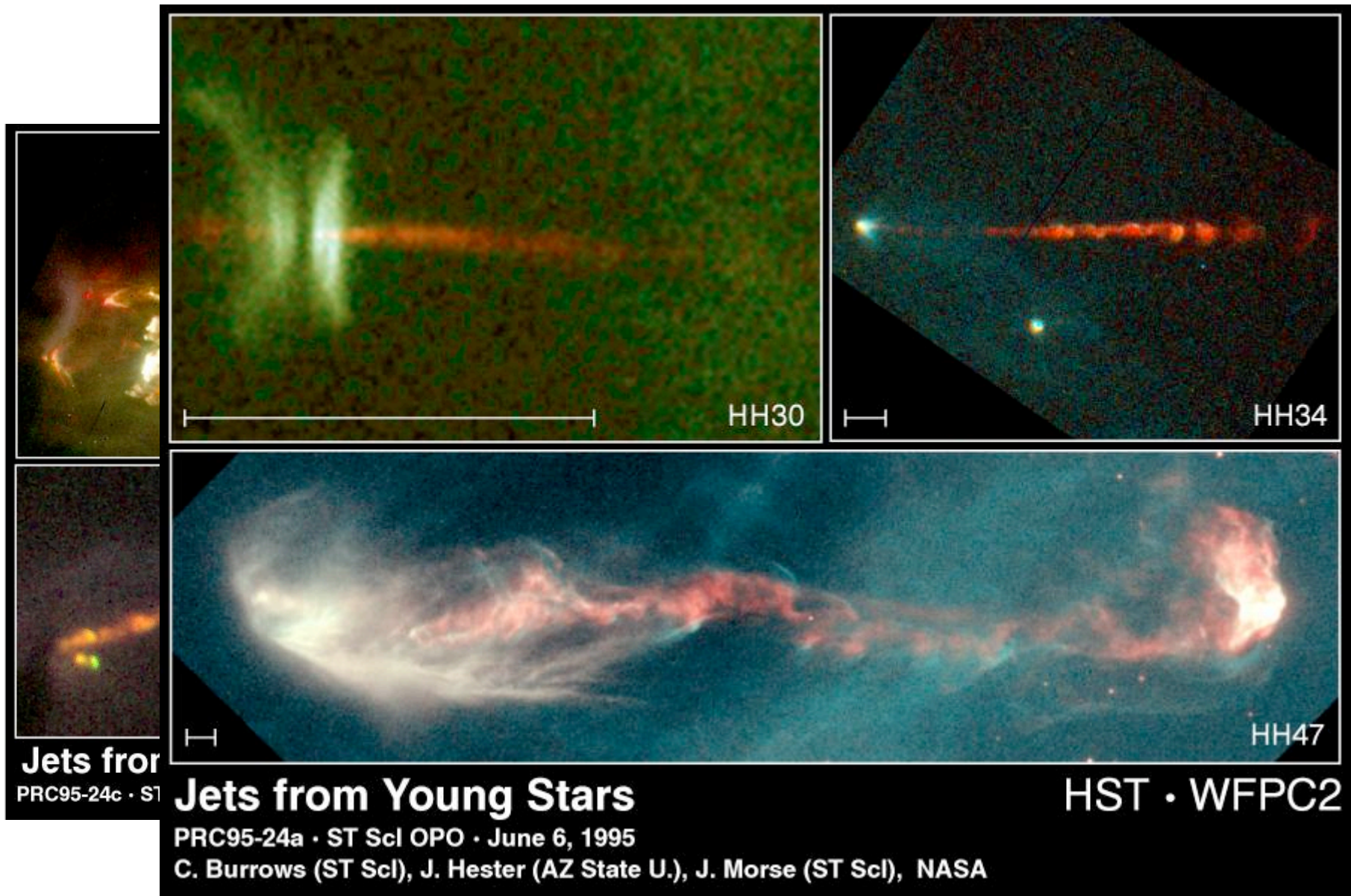


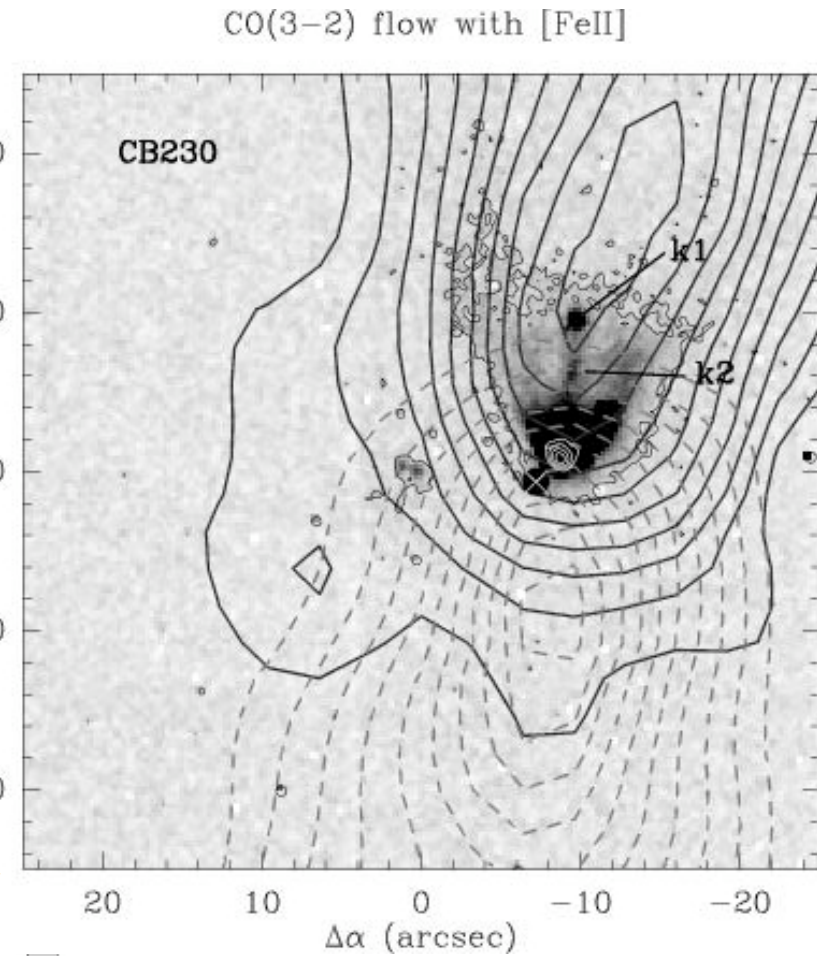
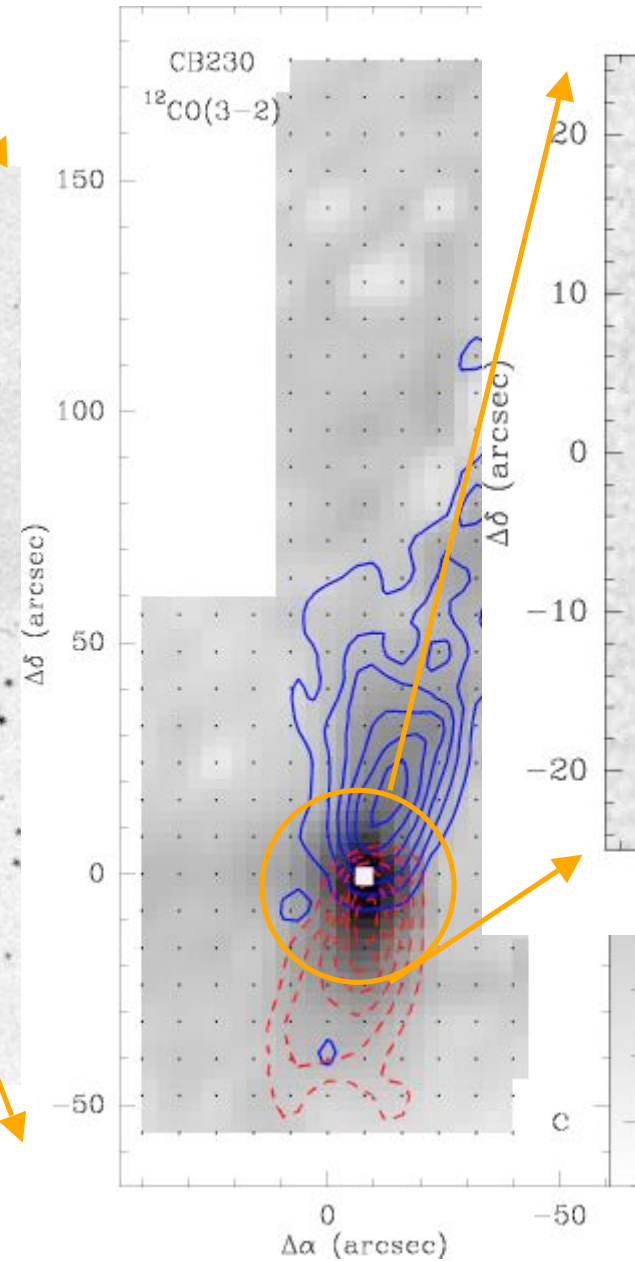
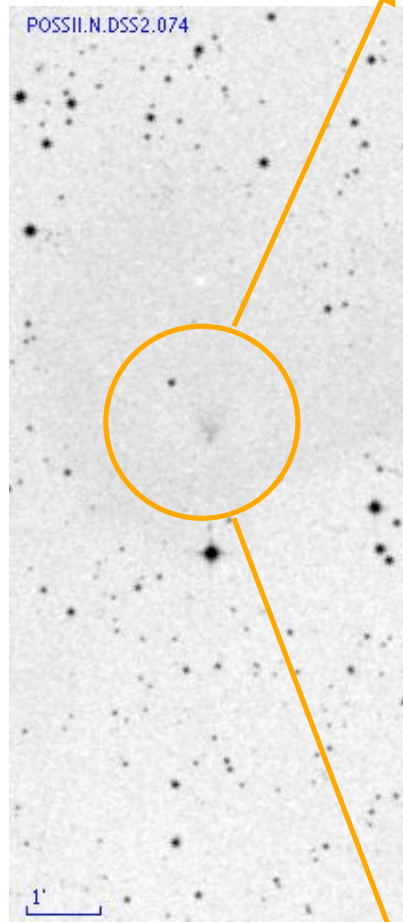
Stars with IR-excess

Disks... with HST (IR)



Disks and jets... with HST (IR)





A jet at
the base
of the
outflow

Brand et al., ApSpSci 313, 2008

Massi et al., A&A 2004, 2008

MASSIVE STAR FORMATION **in the Galaxy**

Literature:

Protostars & Planets I-V: conference proceedings. Reviews.

Tetons Conferences 1-4 (Astron. Soc. Pacific. Conf. Series)

(e.g. Tetons 4 (2001), Galactic Structure, Stars, and the Interstellar Medium)

Crete conf. (Kylafis, Lada, Eds.) “The physics of star form. and early stellar evolution”

<http://www.cfa.harvard.edu/events/1999/crete/>

Ferrière - 2001, Rev. Mod. Phys. 73, 1031 “The interstellar environment of our Galaxy”

Annual Reviews of Astronomy and Astrophysics. A search for ‘molecular clouds’ results in 376 reviews (!) covering all topics, and more, covered here. E.g.:

Evans - 1999, ARAA 37, 311 “Physical conditions in regions of star formation”

Bergin & Tafalla - 2007, ARAA 45, 339 “Cold dark clouds: the initial conditions for SF”

Lada & Lada - 2003, ARAA 51, 57 “Embedded clusters in molecular clouds”

Cox - 2005, ARAA 43, 337 “The three-phase interstellar medium revisited”

Kalberla & Kerp - 2009, ARAA 47, 37 “The HI distribution of the Milky Way”

Herbst & van Dishoeck - 2009, ARAA 47, 437 “Complex organic interstellar molecules”

Next lecture:

MASSIVE STAR FORMATION

Riccardo Cesaroni