



(A highly biased view of) Polarization science with ALMA

Wouter Vlemmings (Nordic ARC/Chalmers/Onsala)



EUROPEAN ARC
ALMA Regional Centre || Nordic

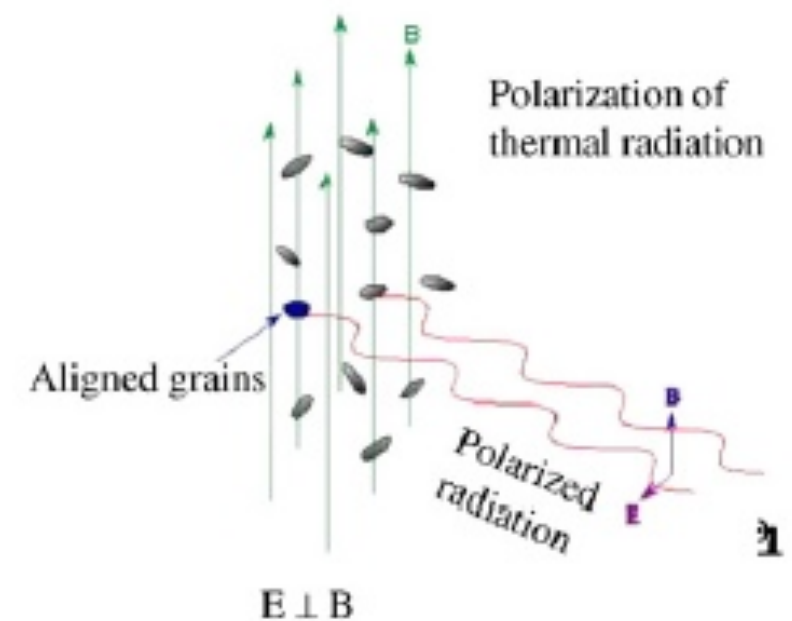
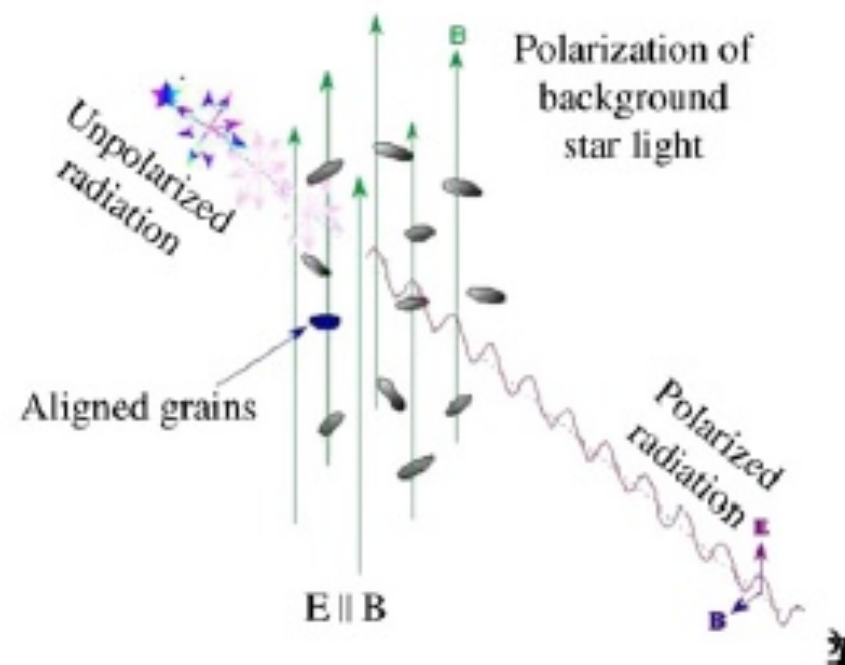
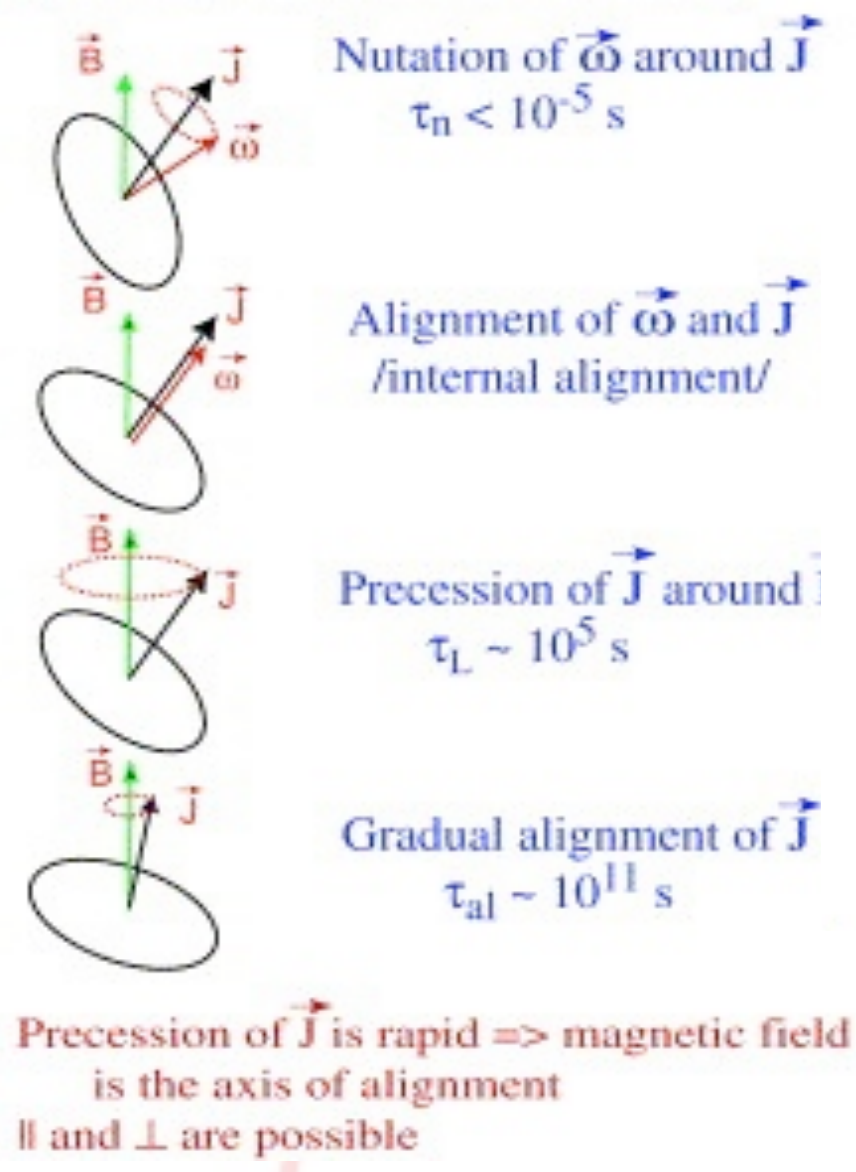


Outline

- (some) Sources of polarization
 - Continuum
 - Dust grain alignment
 - Synchrotron emission
 - Molecular lines
 - Zeeman splitting
 - Goldreich-Kylafis effect
 - Anisotropic radiation effects
- Science Targets
 - Galactic
 - Star Formation
 - Evolved Stars
 - Compact objects / Galactic Centre
 - Extra-galactic
 - Galaxies
 - GRBs
 - AGN / jets / BHs
 - Conclusions

Continuum polarization: Dust grain alignment

- Torques align grain minor axis with B-field
 - P_l from net emission parallel to major axis

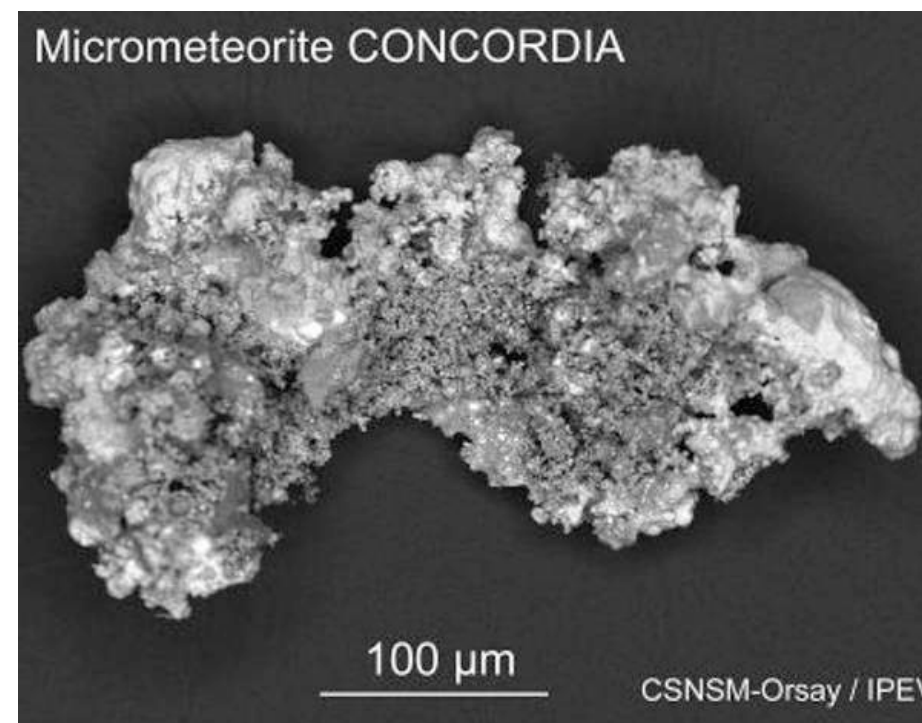


details & figures from Lazarian (2007),
JQSRT 106, 225
Slide from J. Greaves

Continuum polarization: Dust grain alignment

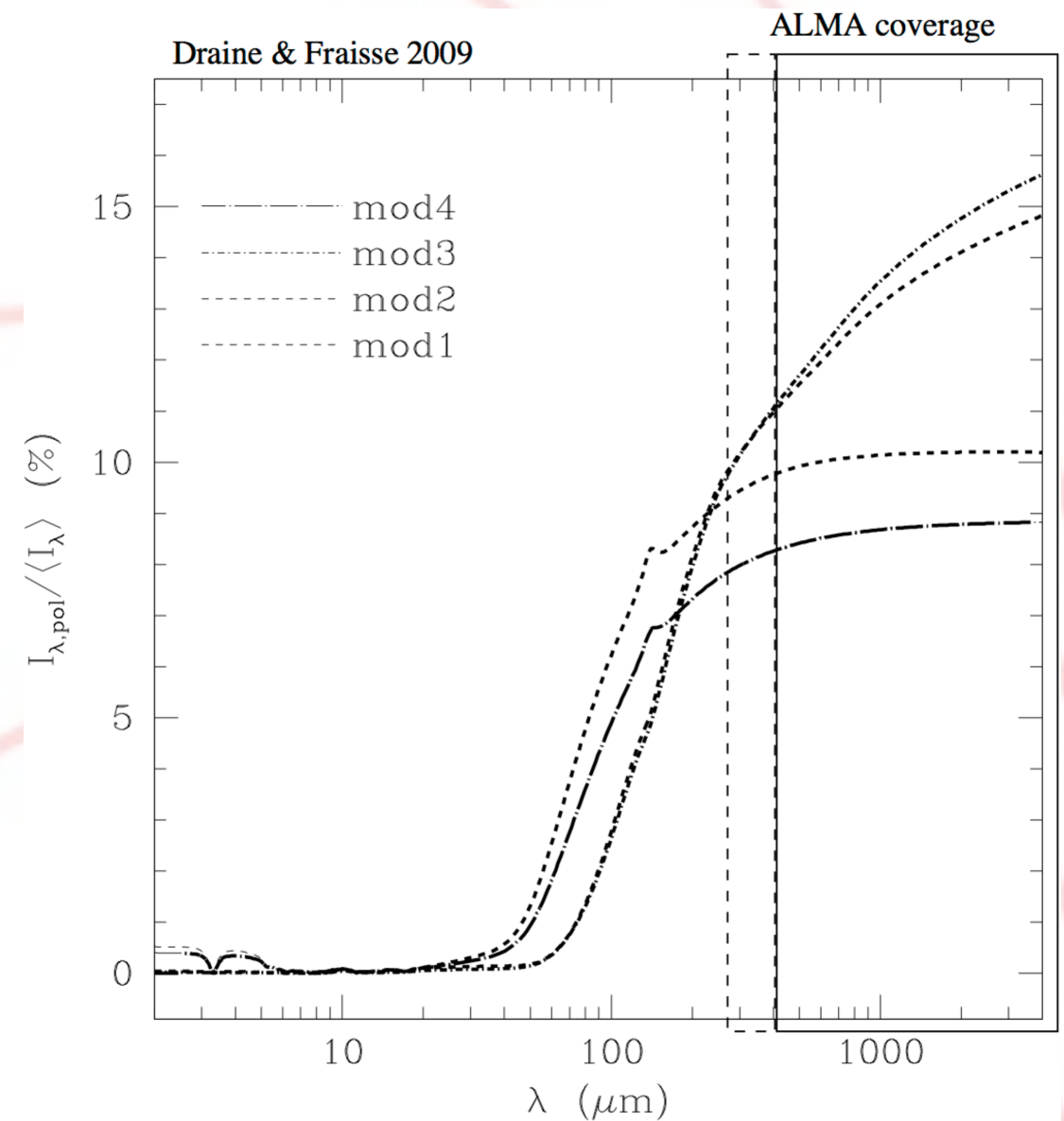
- Torques align grain minor axis with B-field
 - P_l from net emission parallel to major axis
- Idealized approximation of dust grains
 - realistic grains will have different grain alignment efficiencies

➔ P_l obs. potential probe of grain properties



Continuum polarization: Dust grain alignment

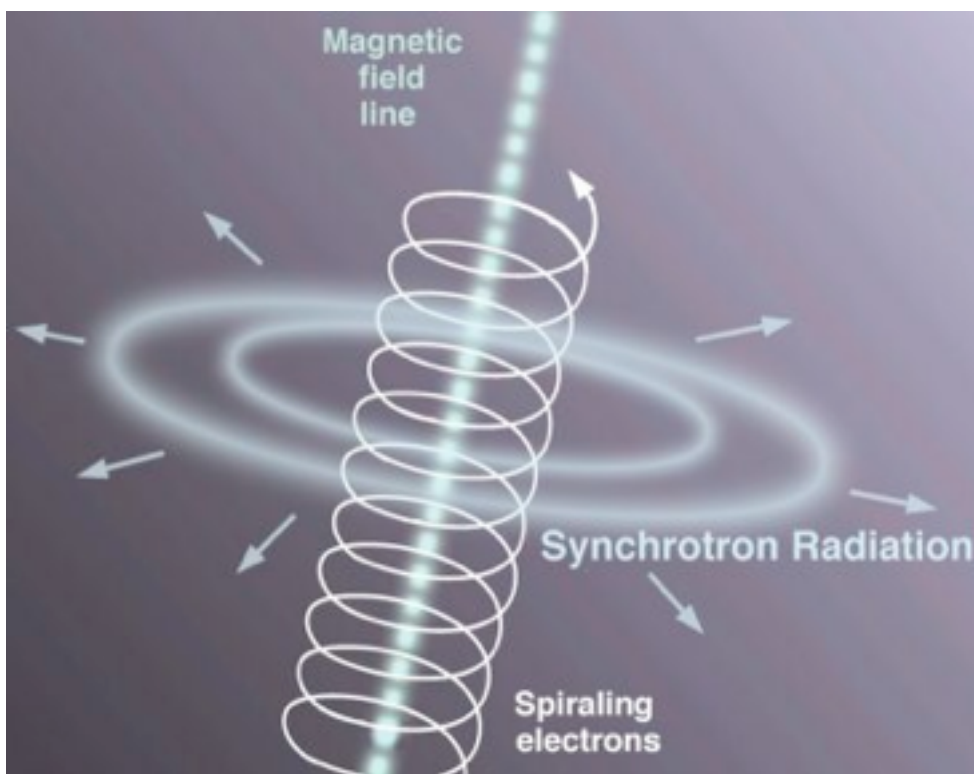
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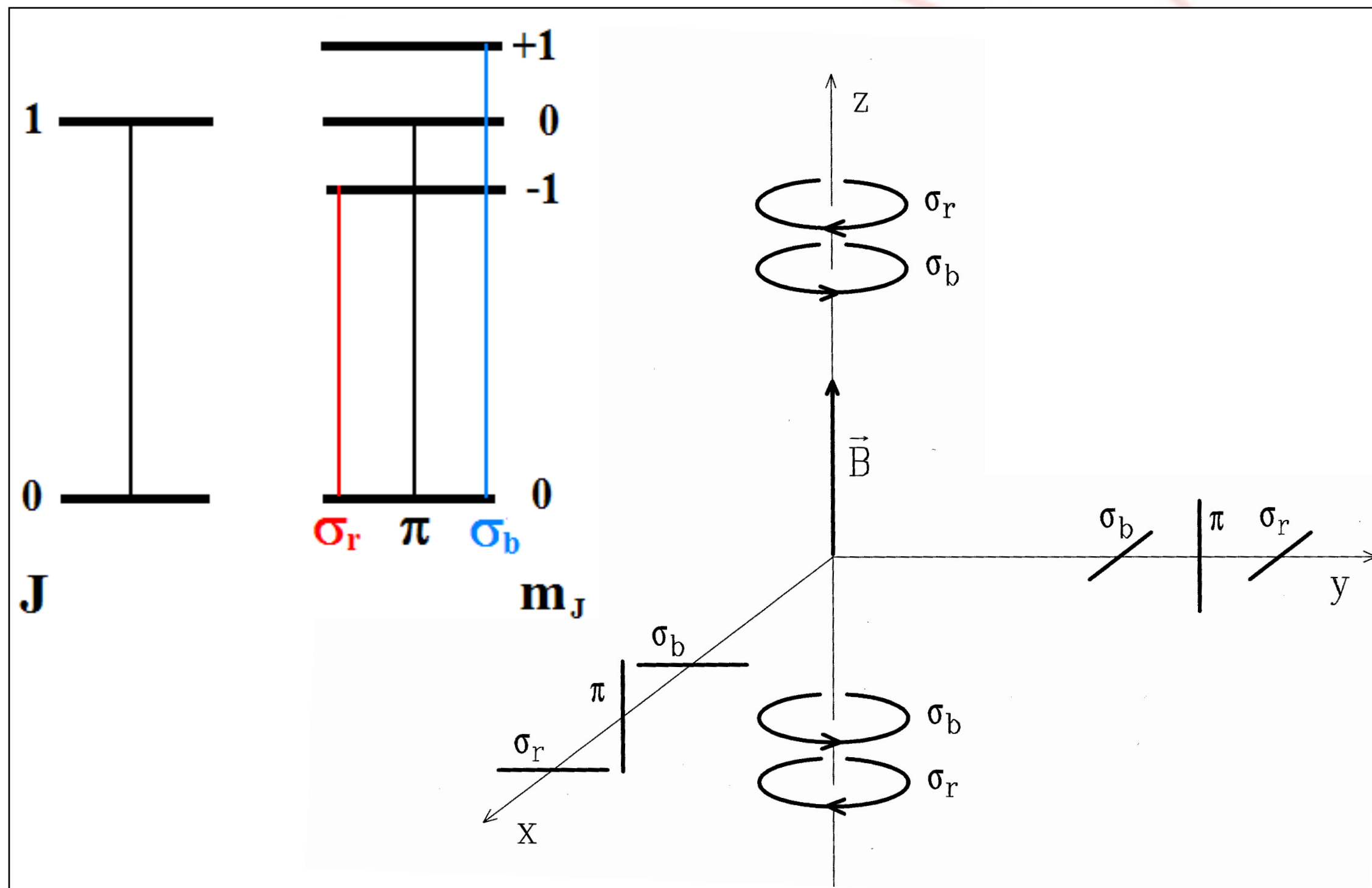
Continuum polarization: Synchrotron radiation

- Magnetic field acceleration of charged particles by the Lorentz force
- radio synchrotron emission with typical spectrum of $F_\nu \propto \nu^{-0.75}$ ($p=2\alpha+1=2.5$)
- Strong polarization

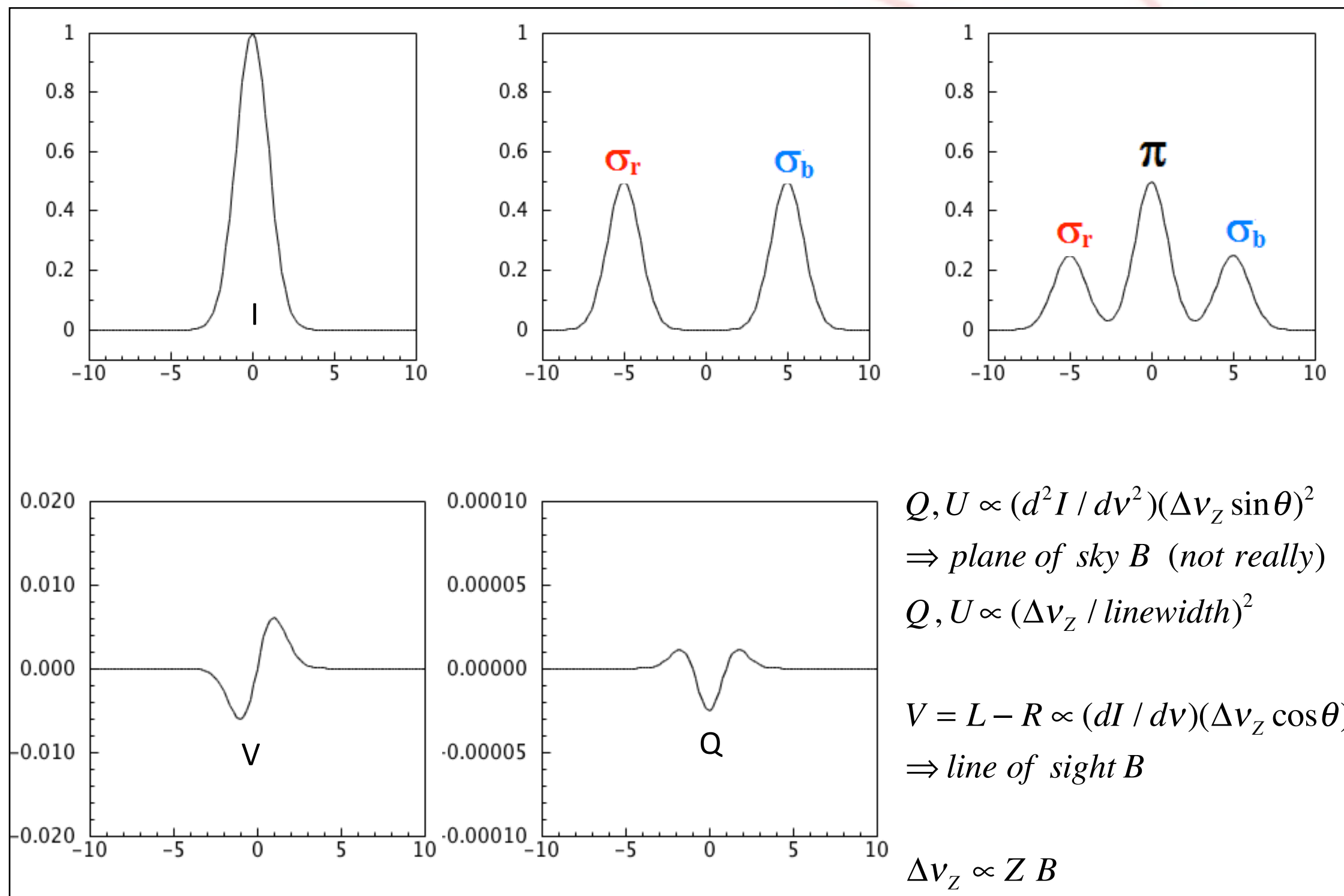
$$\frac{P}{I} = \frac{p+1}{p+7/3}$$



Line polarization: Zeeman Effect



Line polarization: Zeeman Effect



Possible Zeeman lines

Species	Transition	ν (GHz)	Z (Hz/ μ G)	n_H (cm ⁻³)
H I	$F = 1 \rightarrow 0$	1.4	2.8	$10^1 - 10^2$
OH	Λ -doublet	1.7	~ 3	$10^3 - 10^4$
CN	$N, J = 1, 3/2 \rightarrow 0, 1/2$	113.5	2.2	$10^5 - 10^6$
CN	$N, J = 2, 3/2 \rightarrow 1, 3/2$	226.3	~ 2	$\sim 10^6$
CH	$J = 3/2, F = 1 \rightarrow 0$	0.7	~ 3	$\sim 10^5(?)$
CCH	$N, J = 1, 1/2 \rightarrow 0, 1/2$	87.4	~ 2	
SO	$N, J = 2, 3 \rightarrow 1, 2$	99.3	1.0	
SO	$N, J = 3, 4 \rightarrow 2, 3$	138.2	0.8	
SO	$N, J = 4, 3 \rightarrow 3, 2$	159.0	1.0	
SO	$N, J = 5, 6 \rightarrow 4, 5$	220.0	0.5	
SO	$N, J = 2, 1 \rightarrow 1, 2$	236.5	1.7	
CO, CS, HCN, ...	various	various	(few) $\times 10^{-4}$	

+ maser lines!

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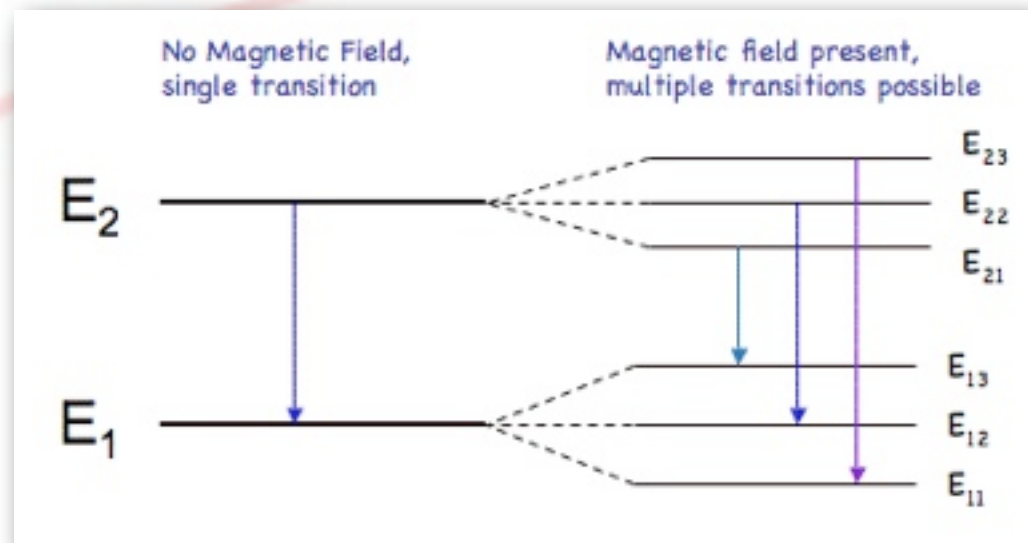
Example:

CN@113.5 for 1 mG has a splitting of 5.8 m/s or about 10^{-3} of its intrinsic linewidth leading to a circular polarization of $\sim 0.1\%$

+ maser lines!

SO	$N, J = 5, 6 \rightarrow 4, 5$	220.0	0.5 Band 6	
SO	$N, J = 2, 1 \rightarrow 1, 2$	236.5	1.7 Band 6	
CO, CS, HCN, ...	various	various	(few) $\times 10^{-4}$	

Goldreich-Kylafis effect I

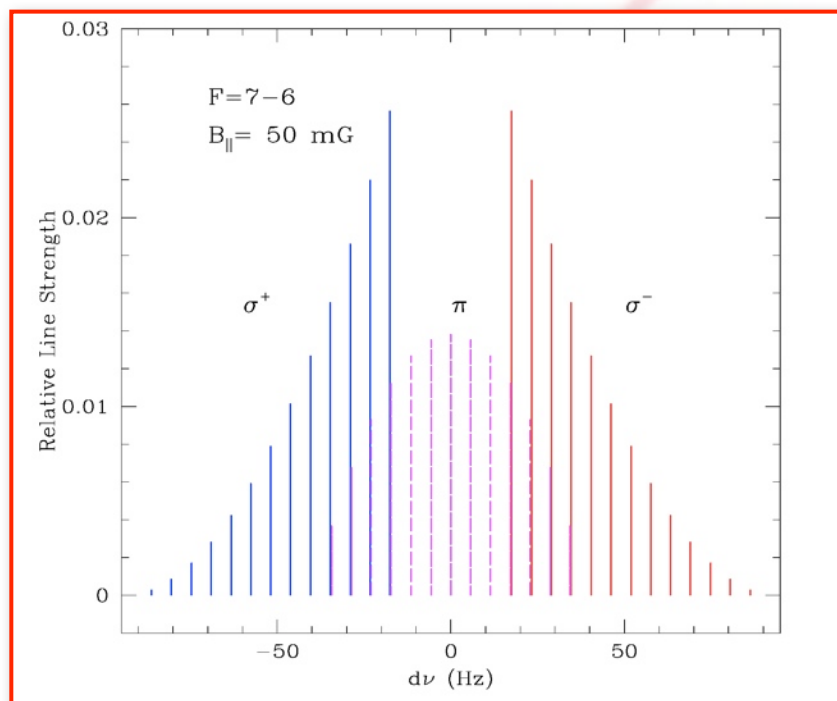


$$\frac{dI_{JJ'}^{\perp}}{ds} = -\kappa_{JJ'}^{\perp} (I_{JJ'}^{\perp} - S_{JJ'}^{\perp})$$

$$\frac{dI_{JJ'}^{\parallel}}{ds} = -\kappa_{JJ'}^{\parallel} (I_{JJ'}^{\parallel} - S_{JJ'}^{\parallel})$$

$\Delta m_F = \pm 1$; $\sigma^{\pm}$ – circularly polarized $\perp B$

$\Delta m_F = 0$; π – linearly polarized along B



$$\kappa_{JJ'}^{\perp} = \frac{1}{2} \phi(\nu - \nu_{JJ'}) \sum_{\Delta M=1} \kappa_{JM J' M'}$$

Opacity

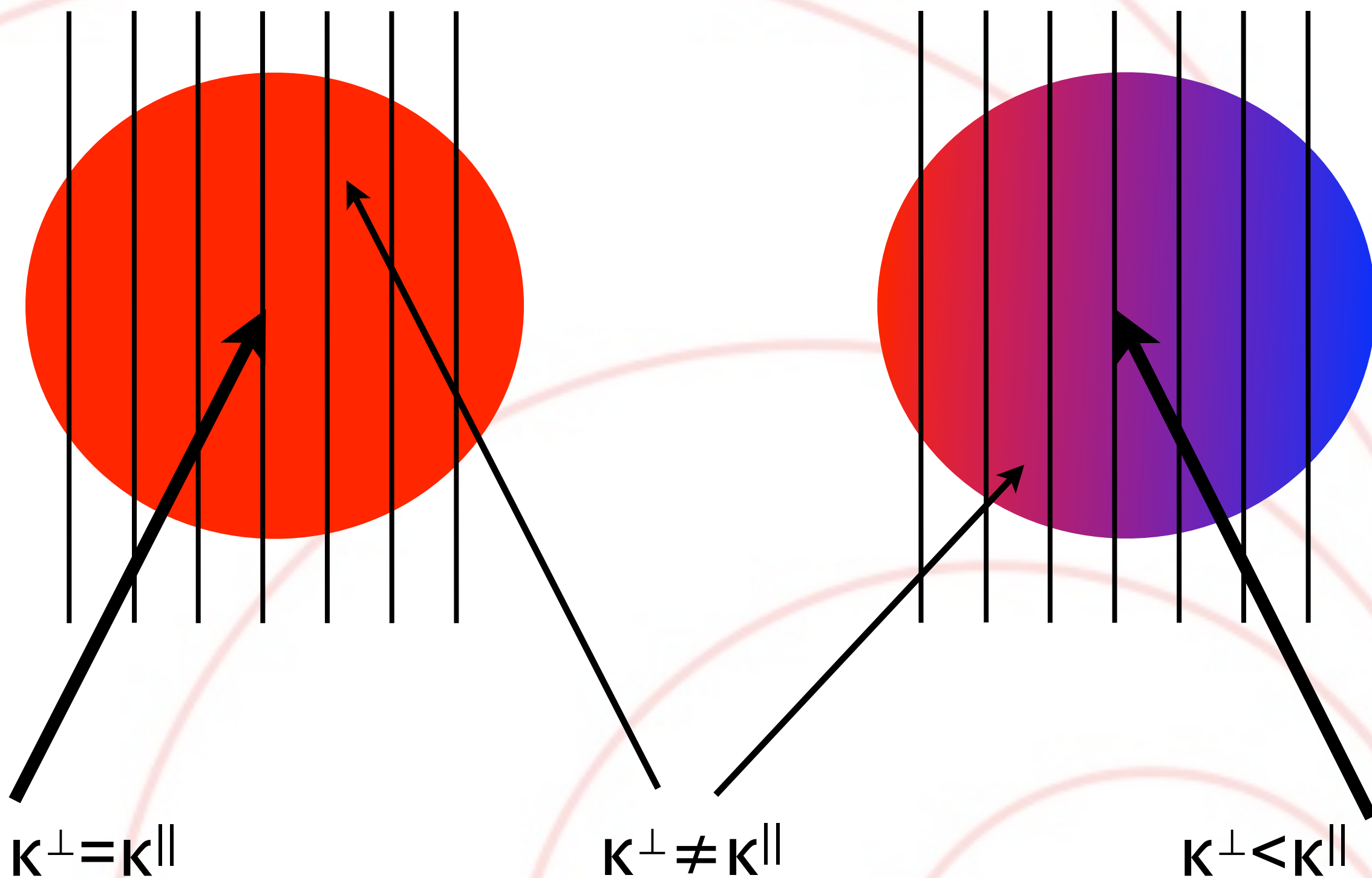
$$S_{JJ'}^{\perp} = \frac{\sum_{\Delta M=1} \kappa_{JM J' M'} S_{JM J' M'}}{\sum_{\Delta M=1} \kappa_{JM J' M'}}$$

Source term

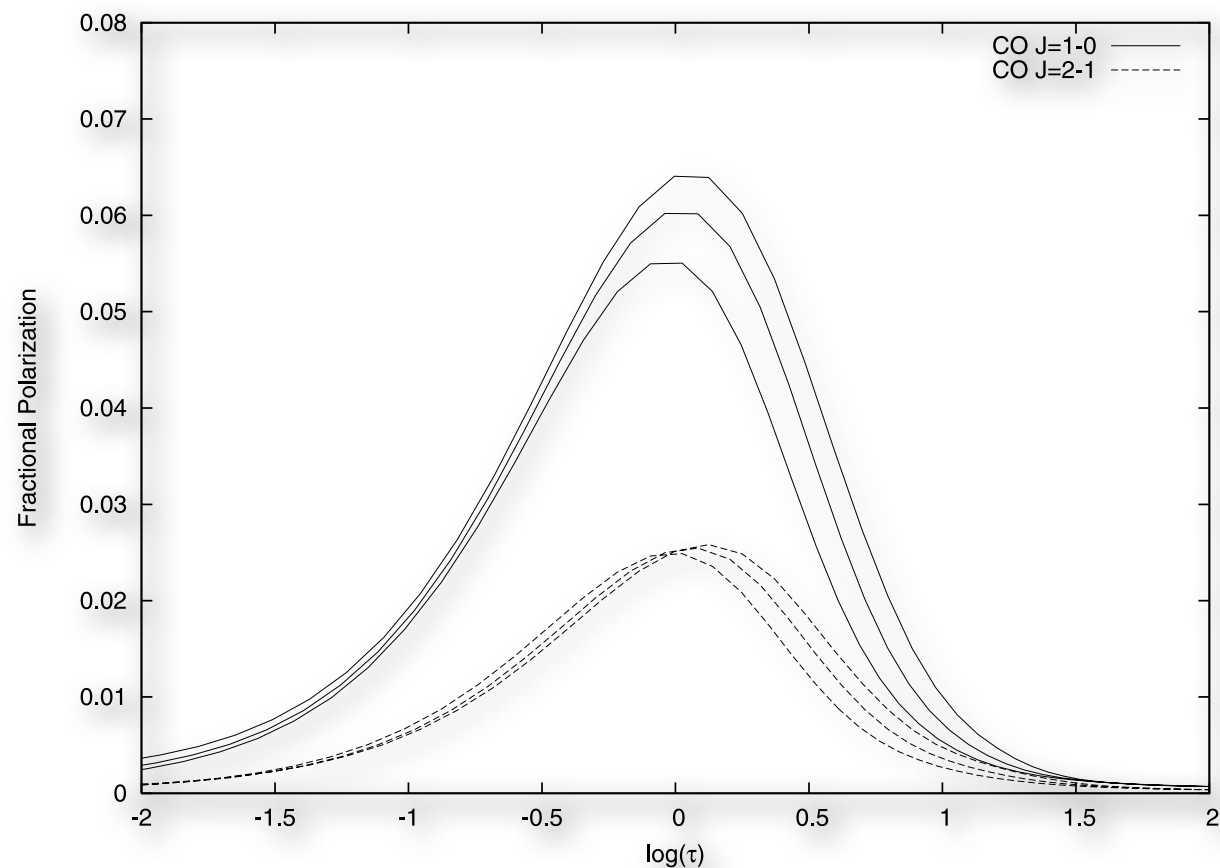
$$\kappa_{JJ'}^{\parallel} = \phi(\nu - \nu_{JJ'}) \left(\sin^2 \theta \sum_{\Delta M=0} \kappa_{JM J' M'} + \frac{1}{2} \cos^2 \theta \sum_{\Delta M=1} \kappa_{JM J' M'} \right)$$

$$S_{JJ'}^{\parallel} = \left(\sin^2 \theta \sum_{\Delta M=0} \kappa_{JM J' M'} S_{JM J' M'} + \frac{1}{2} \cos^2 \theta \sum_{\Delta M=1} \kappa_{JM J' M'} S_{JM J' M'} \right) \times \left(\sin^2 \theta \sum_{\Delta M=0} \kappa_{JM J' M'} + \frac{1}{2} \cos^2 \theta \sum_{\Delta M=1} \kappa_{JM J' M'} \right)^{-1}$$

Goldreich-Kylafis effect II

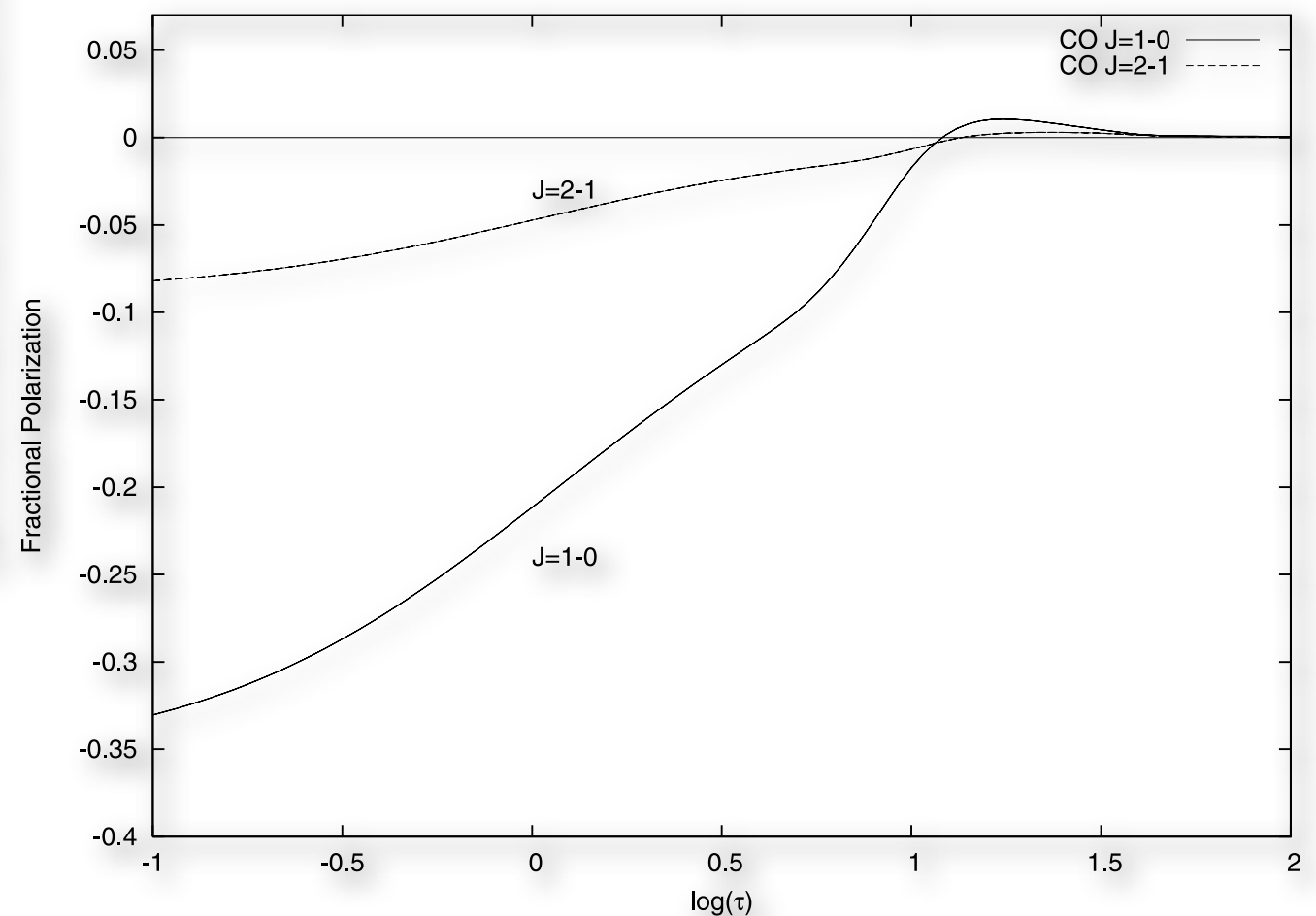


Goldreich-Kylafis effect III



Velocity anisotropy
perpendicular to B

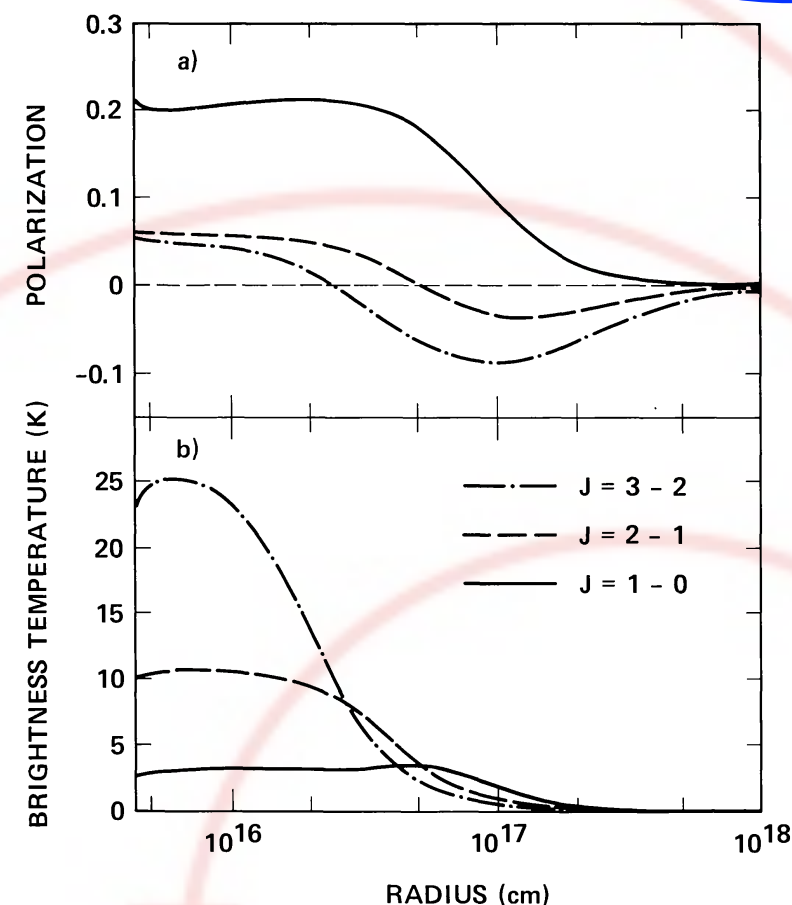
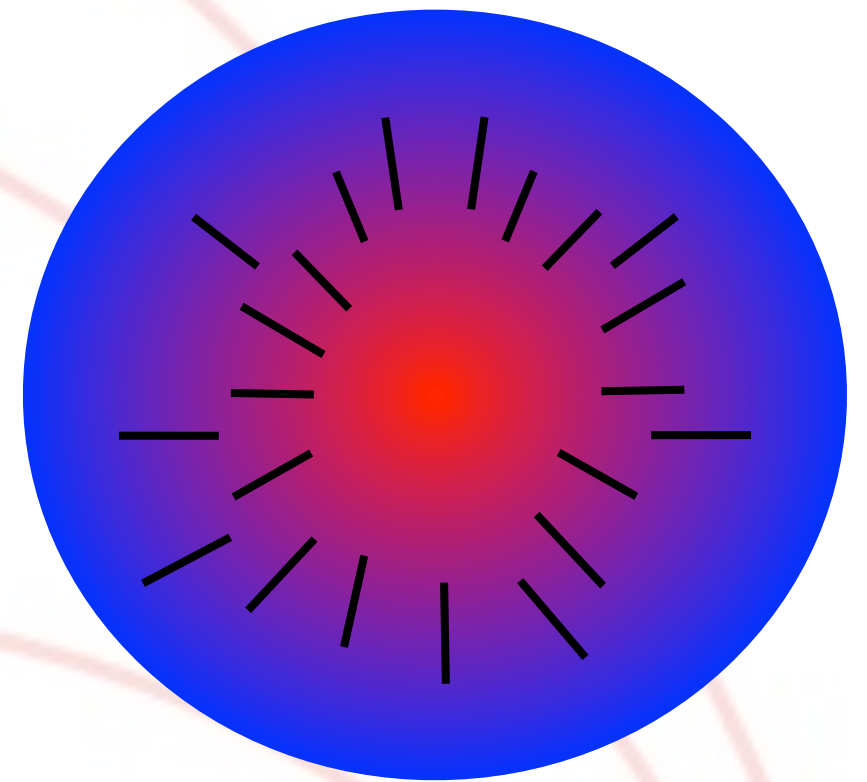
Radiation anisotropy



Cortes et al. 2005

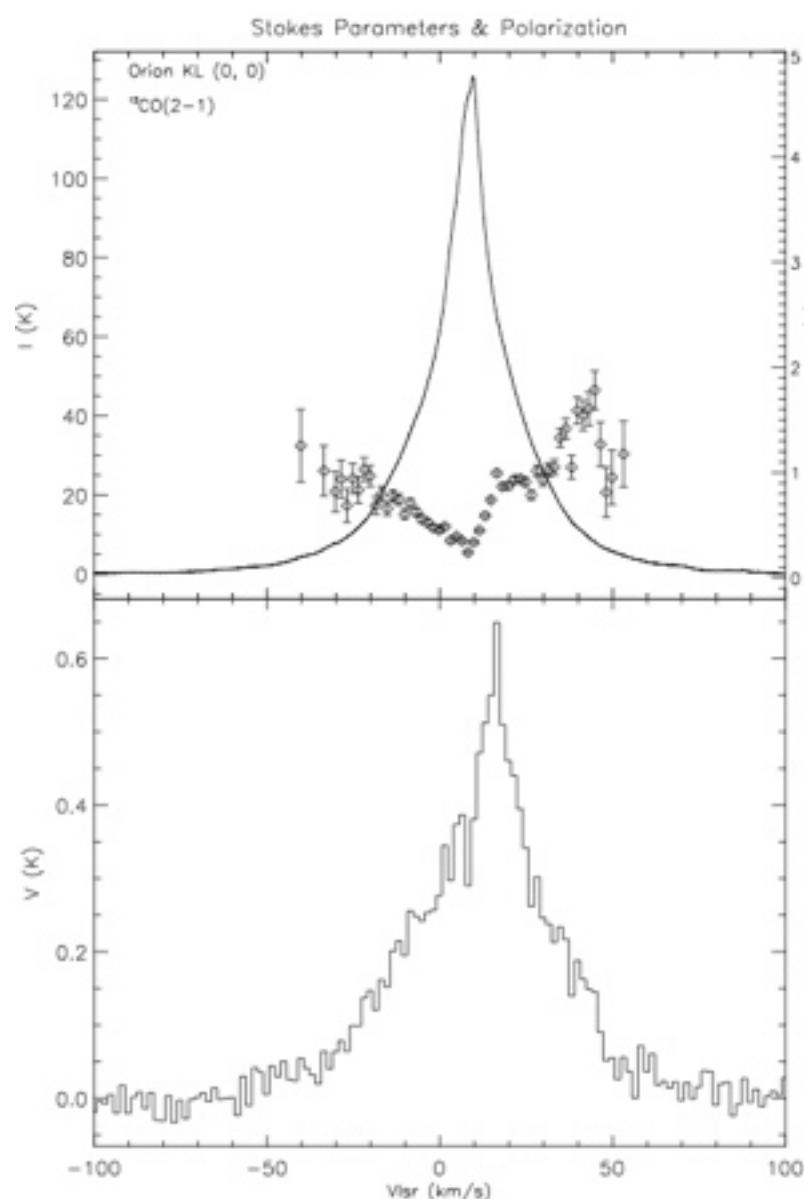
GK related Caveats....

- Molecular alignment by radiative (infrared) pumping (Morris et al. 1985)
 - Linear polarization becomes radial or tangential to IR radiation source (i.e. central star)
- Multi-level excitation



non-Zeeman circular

- Linear to circular polarization conversion through anisotropic resonant scattering



$$|\psi_0\rangle = \alpha_0 |n_{\parallel}\rangle + \beta_0 |n_{\perp}\rangle$$

$$|\psi'\rangle = \alpha_0 e^{i\phi} |n_{\parallel}\rangle + \beta_0 |n_{\perp}\rangle$$

$$q = \alpha_0^2 - \beta_0^2$$

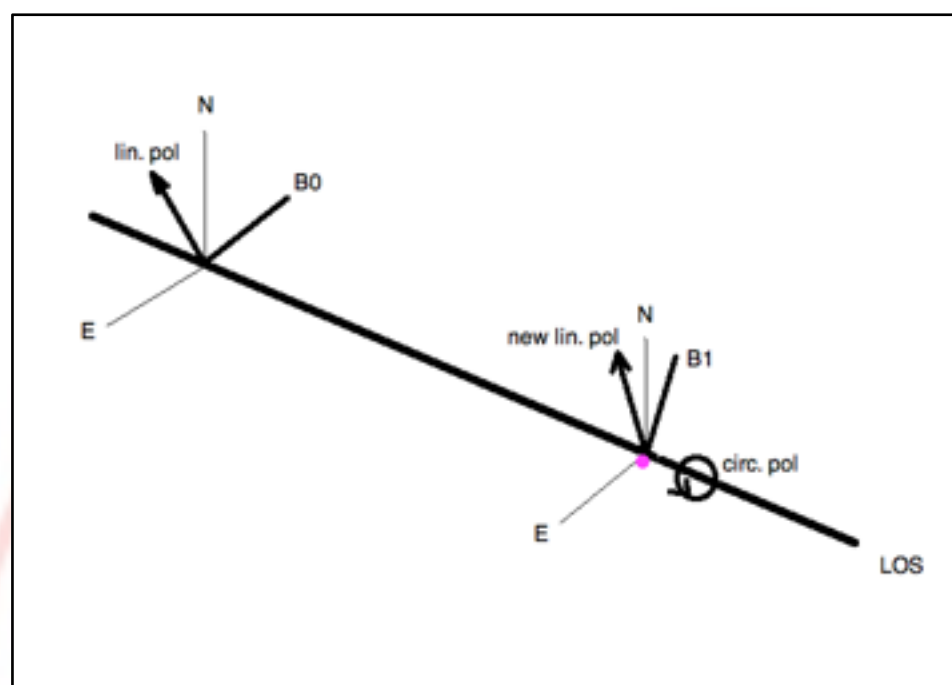
$$u = 2\alpha_0\beta_0 \cos(\phi)$$

$$v = -2\alpha_0\beta_0 \sin(\phi)$$

Incident background radiation
scattered radiation

Stokes parameters in the frame of
foreground magnetic field

Increase of $\phi \Rightarrow$ decrease of u
increase of v



(Houde et al. 2013, slides from
T. Hezareh)

Anisotropic scattering - phase shift

$$\phi(\omega) \cong -\omega_z^2 \sin^2(\iota) l^4 \frac{n_{CO} 3\pi c^2 A_{ba}}{4\hbar \omega_0^3 \omega^2} \sqrt{u(\omega)u'(\omega)I(\omega)}$$

ω_z : the Zeeman splitting

ι : inclination angle of the magnetic field

ω : the frequency of scattered photon

ω_0 : frequency of transition

n_{CO} : density of CO molecules in lower state

l : the size of interaction region

A_{ba} : the spontaneous emission coefficient ($\sim 10^{-6} \text{ s}^{-1}$)

$u(u')$: the incident (scattered) linear polarization energy density

$I(\omega)$: resonant scattering integral over incident linear polarization profile

Remember, CO Zeeman splitting
would be <0.01%

Masers

Many masers, several will be highly polarized

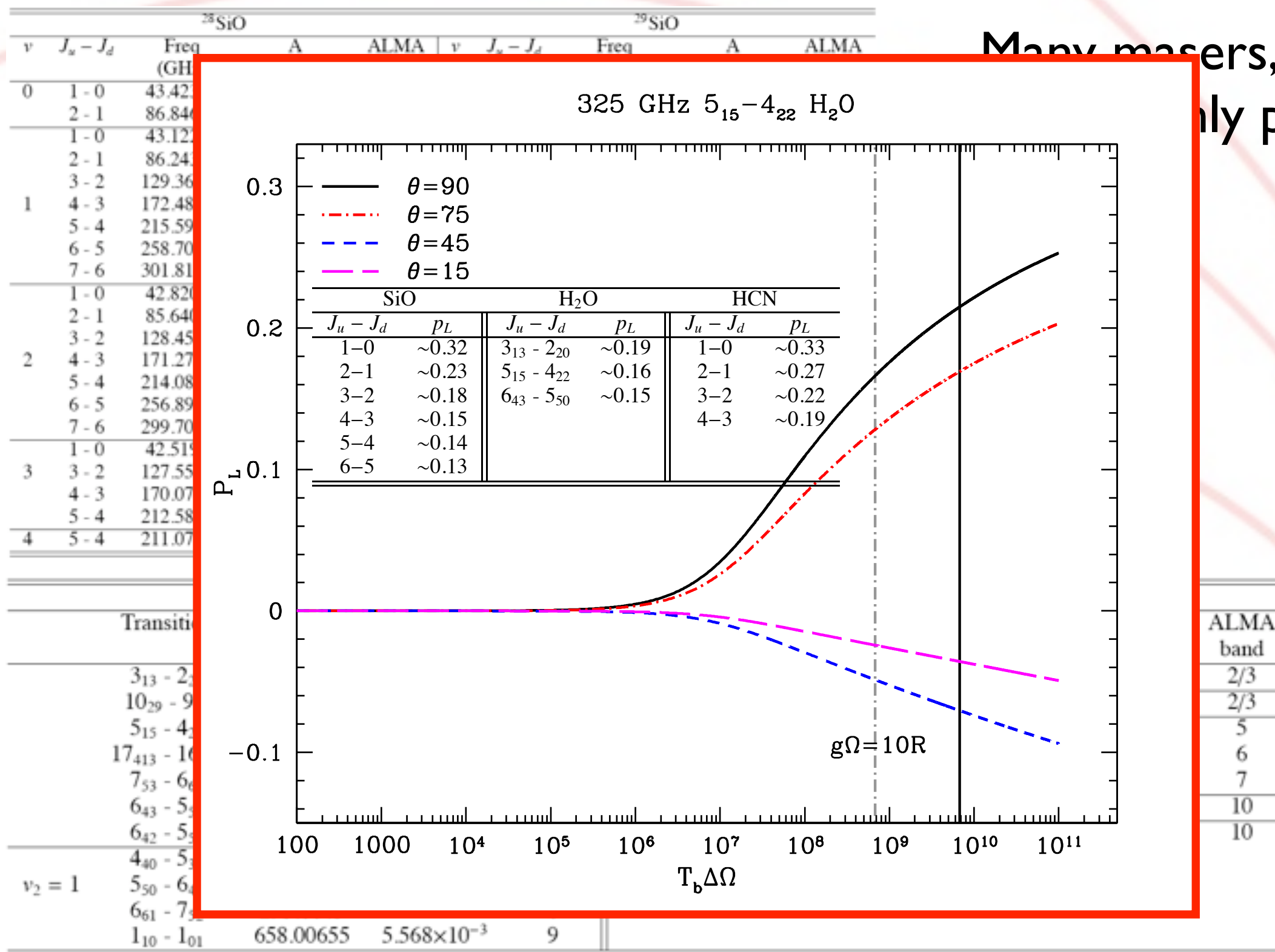
²⁸ SiO					²⁹ SiO				
ν	$J_u - J_d$	Freq (GHz)	A (s ⁻¹)	ALMA band	ν	$J_u - J_d$	Freq (GHz)	A (s ⁻¹)	ALMA band
0	1 - 0	43.42386	3.036×10 ⁻⁶	1	0	1 - 0	42.87992	2.114×10 ⁻⁸	1
	2 - 1	86.84699	2.915×10 ⁻⁵	2		2 - 1	85.75906	2.460×10 ⁻⁷	2
1	1 - 0	43.12208	3.011×10 ⁻⁶	1	0	3 - 2	128.63685	9.696×10 ⁻⁷	4
	2 - 1	86.24344	2.891×10 ⁻⁵	2		4 - 3	171.51255	2.532×10 ⁻⁶	5
	3 - 2	129.36326	1.045×10 ⁻⁴	4		5 - 4	214.38548	5.334×10 ⁻⁶	6
	4 - 3	172.48102	2.569×10 ⁻⁴	5		6 - 5	257.25493	9.869×10 ⁻⁶	6
	5 - 4	215.59592	5.131×10 ⁻⁴	6		3 - 2	127.74849	3.350×10 ⁻⁴	4
	6 - 5	258.70725	9.003×10 ⁻⁴	6	1	4 - 3	170.32807	8.745×10 ⁻⁴	5
	7 - 6	301.81430	1.445×10 ⁻³	7		6 - 5	255.47849	3.407×10 ⁻³	6
2	1 - 0	42.82059	2.986×10 ⁻⁶	1	2	6 - 5	253.70317	1.11139	6
	2 - 1	85.64046	2.866×10 ⁻⁵	3	³⁰ SiO				
	3 - 2	128.45881	1.036×10 ⁻⁴	4	0	1 - 0	42.373426	2.016×10 ⁻⁸	1
	4 - 3	171.27507	2.547×10 ⁻⁴	5		2 - 1	84.746170	2.346×10 ⁻⁷	2
	5 - 4	214.08848	5.088×10 ⁻⁴	6	1	5 - 4	211.853473	5.081×10 ⁻⁶	6
	6 - 5	256.89831	8.927×10 ⁻⁴	6		4 - 3	168.323352	8.054×10 ⁻⁴	5
	7 - 6	299.70386	1.433×10 ⁻³	7	2	4 - 3	167.160563	2.542×10 ⁻¹	5
3	1 - 0	42.51938	2.951×10 ⁻⁶	1					
	3 - 2	127.55521	1.027×10 ⁻⁴	4					
	4 - 3	170.07057	2.525×10 ⁻⁴	5					
	5 - 4	212.58248	5.044×10 ⁻⁴	6					
4	5 - 4	211.07784	4.986×10 ⁻⁴	6					

H ₂ O				HCN				
Transition	Freq (GHz)	A (s ⁻¹)	ALMA band	Transition	Freq (GHz)	A (s ⁻¹)	ALMA band	
3 ₁₃ - 2 ₂₀	183.31012	3.629×10 ⁻⁶	5	1 - 0	88.631602	1.771×10 ⁻⁷	2/3	
10 ₂₉ - 9 ₃₆	321.22564	6.348×10 ⁻⁶	7	$\nu_2 = 2^0$ 1 - 0	89.0877	1.483×10 ⁻⁴	2/3	
5 ₁₅ - 4 ₂₂	325.15292	1.166×10 ⁻⁵	7	$\nu_2 = 1^{1c}$ 2 - 1	177.2387	4.578×10 ⁻⁵	5	
17 ₄₁₃ - 16 ₇₁₀	354.8089	1.096×10 ⁻⁵	7		3 - 2	267.1993	2.262×10 ⁻⁴	6
7 ₅₃ - 6 ₆₀	437.34667	2.212×10 ⁻⁵	8		4 - 3	354.4605	6.122×10 ⁻⁴	7
6 ₄₃ - 5 ₅₀	439.15081	2.857×10 ⁻⁵	8	$\nu_2 = 4$ 9 - 8	804.7509	- ^a	10	
6 ₄₂ - 5 ₅₁	470.88895	3.534×10 ⁻⁵	8	$\nu_1 = 1^1 \rightarrow \nu_2 = 4^0$ 10 - 9	890.761	- ^a	10	
$\nu_2 = 1$	4 ₄₀ - 5 ₃₃	96.26116	4.719×10 ⁻⁷					
	5 ₅₀ - 6 ₄₃	232.68670	4.770×10 ⁻⁶					
	6 ₆₁ - 7 ₅₂	293.6645	- ^a					
	1 ₁₀ - 1 ₀₁	658.00655	5.568×10 ⁻³					

Pérez Sánchez et al. 2013

Masers

Many masers, several
only polarized



Pérez Sánchez et al. 2013

Recap

- Various linear and circular polarization mechanisms
 - most probe line-of-sight or plane-of-the-sky magnetic field
 - most have (sub)-percent polarization fractions
 - except synchrotron and masers
 - Several fairly unique to the (sub-)mm regime
 - Goldreich-Kylafis of e.g. CO
 - Zeeman of e.g. CN/SO and various masers
 - aligned dust (submm dust peak)
 - Resonant scattering?

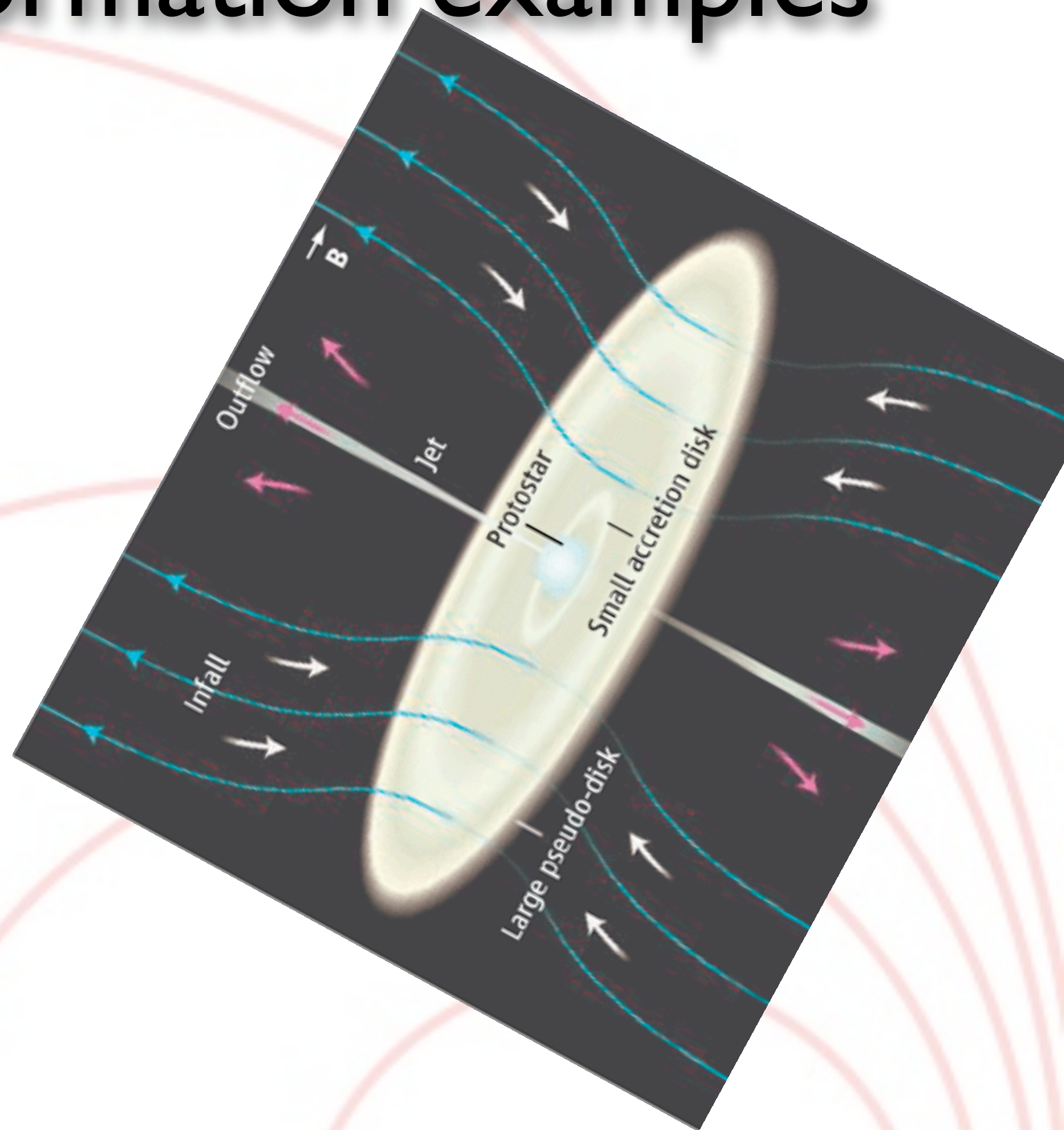
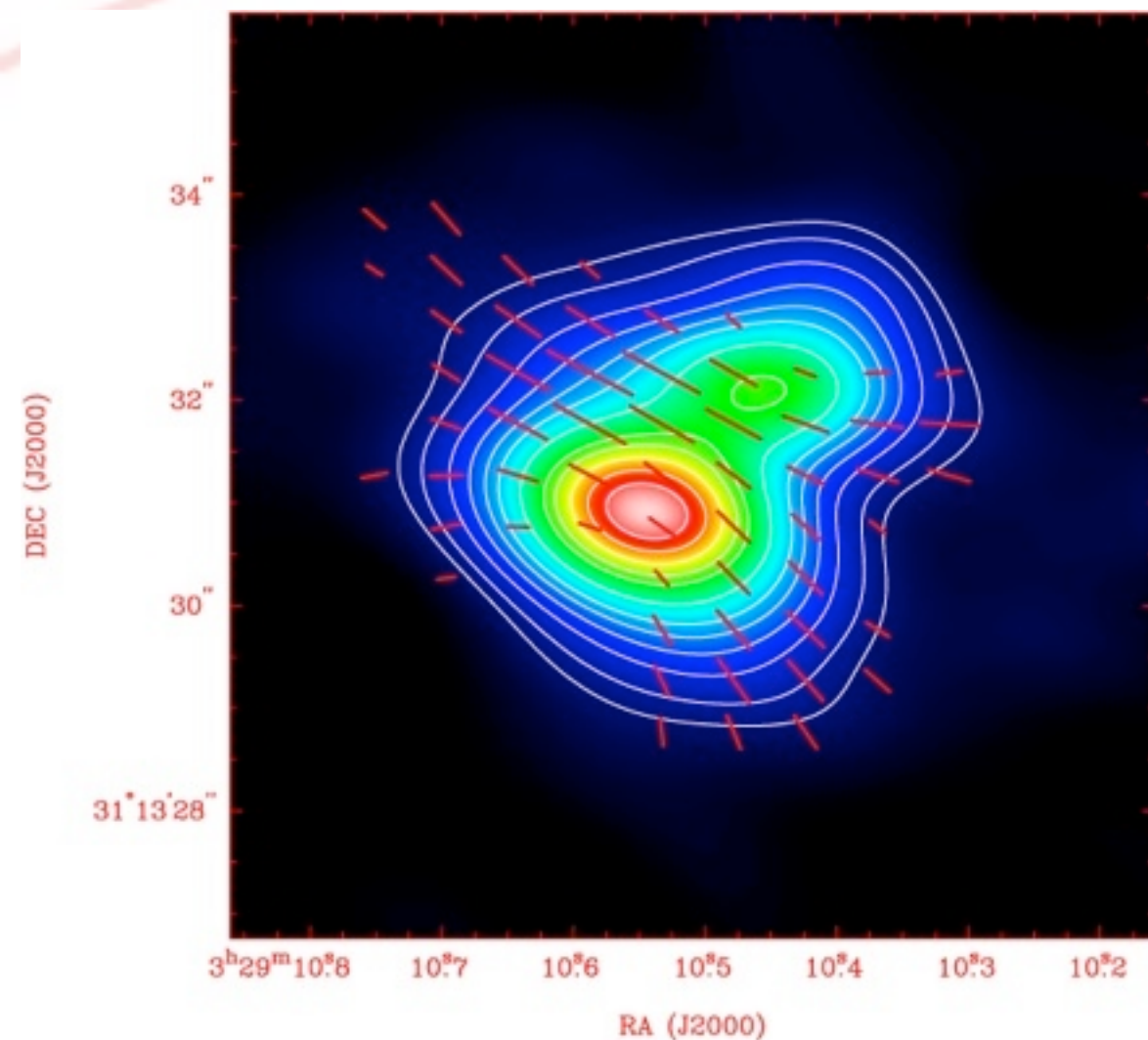


Some Science Examples:
Galactic Science

Star Formation

- What is the role/influence of magnetic fields during low-mass and massive star formation
 - magnetic disk braking (catastrophe?)
 - aligned/misaligned fields?
 - outflow launching (requires magnetic field)
 - disk winds/X-winds?
 - suppression of fragmentation?
 - setting threshold for SF to occur?
 - connection between seed field and protostellar field?

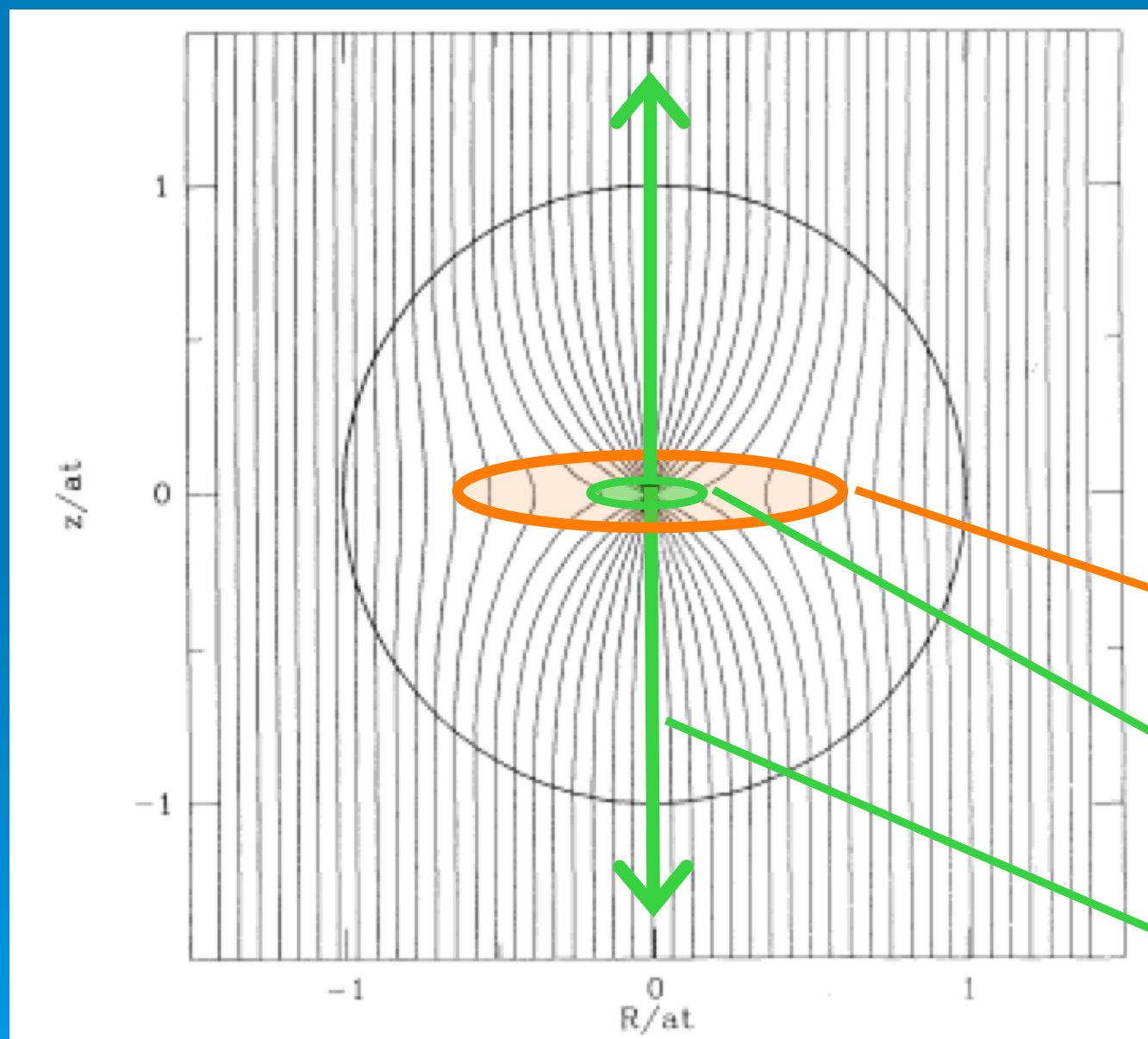
Star Formation examples



Girart et al. (2006)
Ambipolar diffusion?

Star Formation examples

Testing Magnetized Collapse Models usually applied to formation of a single low-mass star



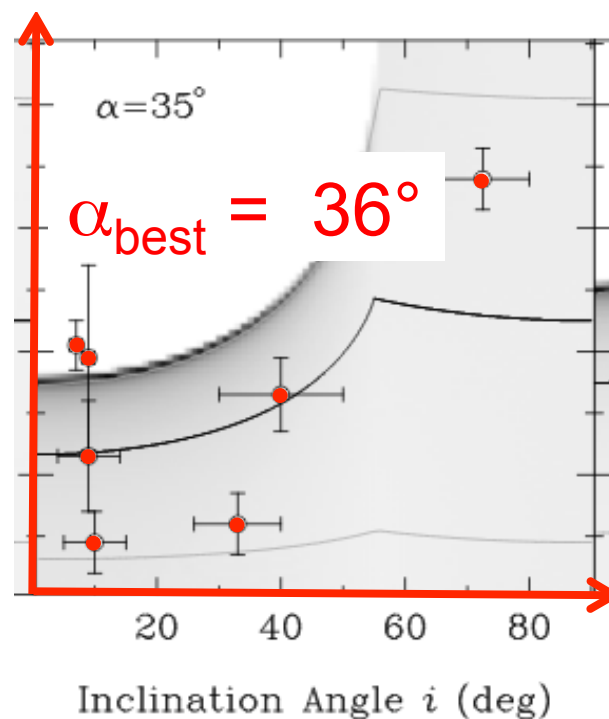
B-field from model of
Galli & Shu '93
(see also Fiedler Mouschovias
'93, Allen, Li, & Shu '03,
Machida, Inutsuka, &
Matsumoto '07, Joos,
Hennebelle, & Ciardi '12)

- B-field uniform outside infall radius
- pseudo-disk: a dynamic structure (few $\times 1000$ AU)
- Keplerian disk: rotationally supported (few $\times 100$ AU)
- jets/outflows originate inside Keplerian disk

Slide courtesy Giles Novak

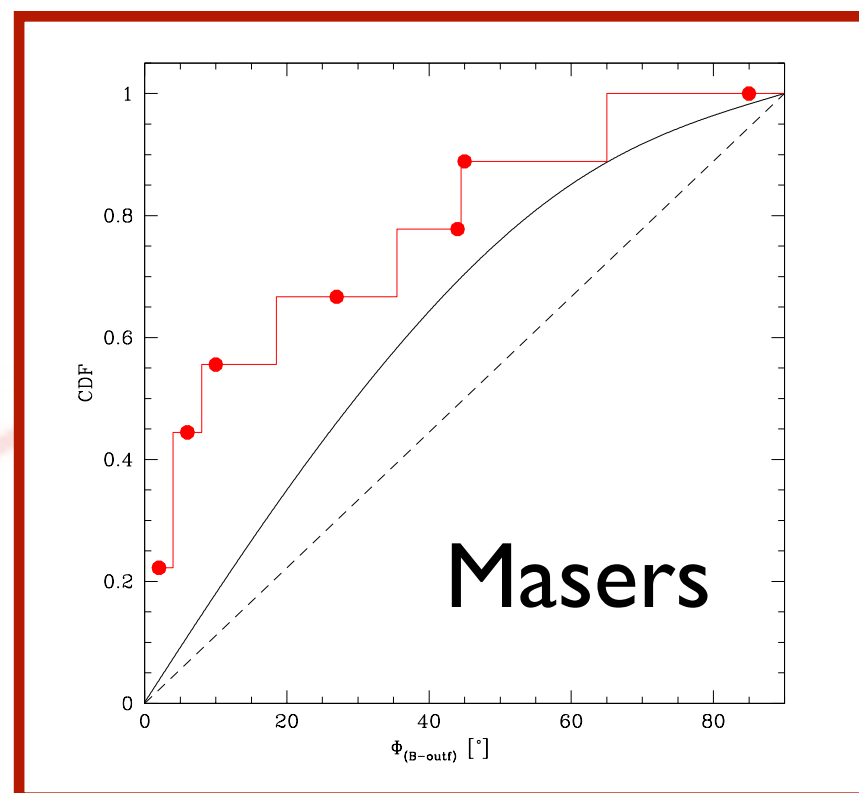
Star Formation examples

- Looking for relation between outflow/disk orientation and envelope magnetic field

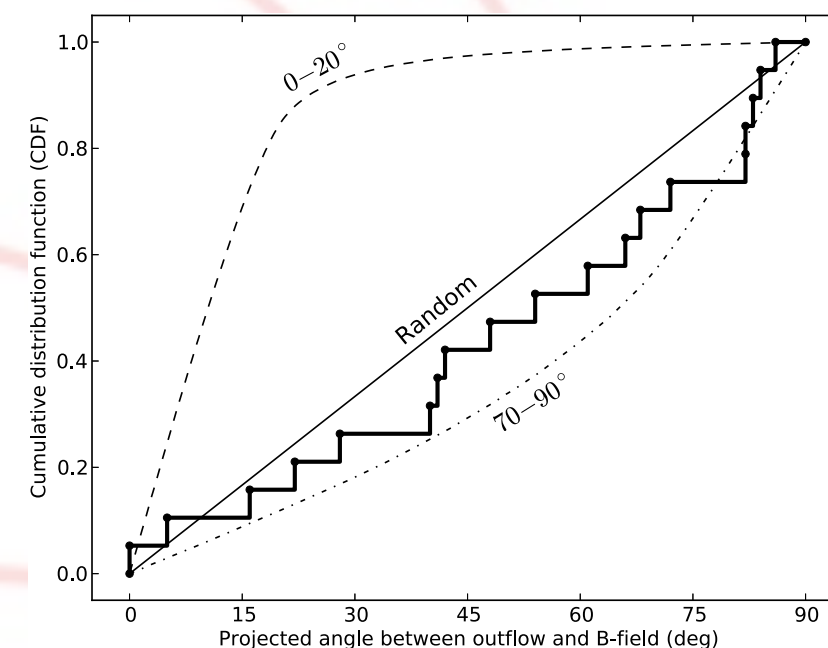


Novak et al. 2013

both ~ 35 degree or less misalignment
marginally significant non-random



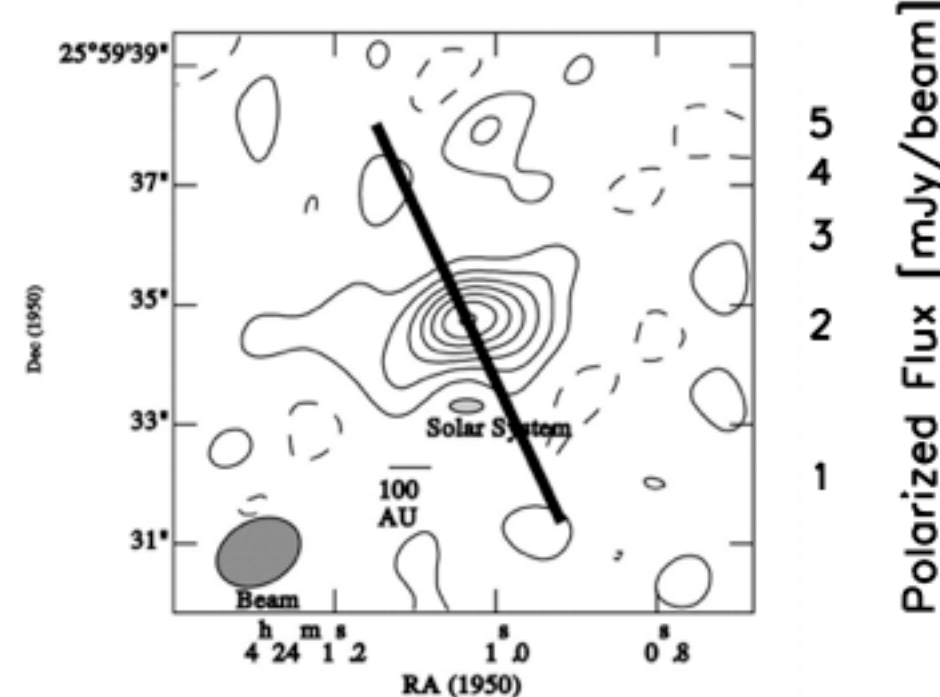
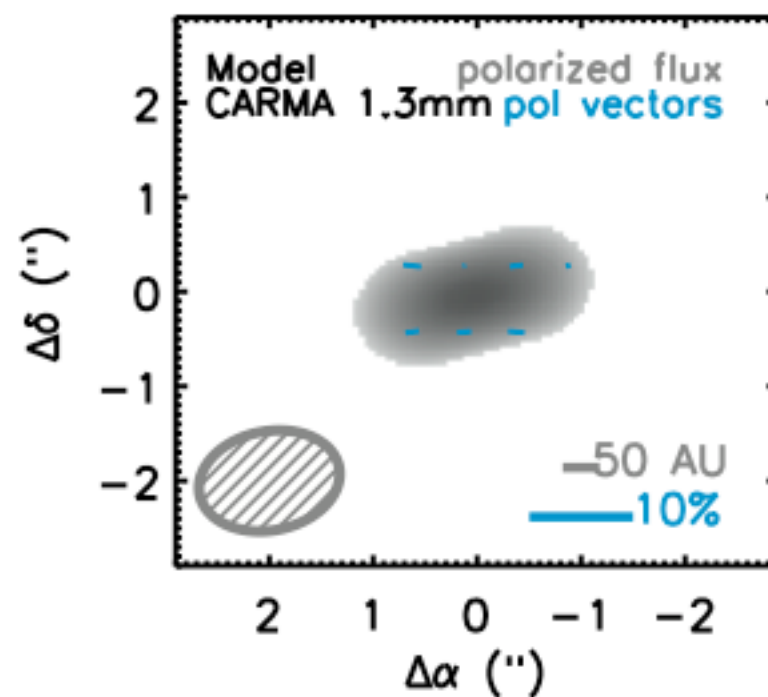
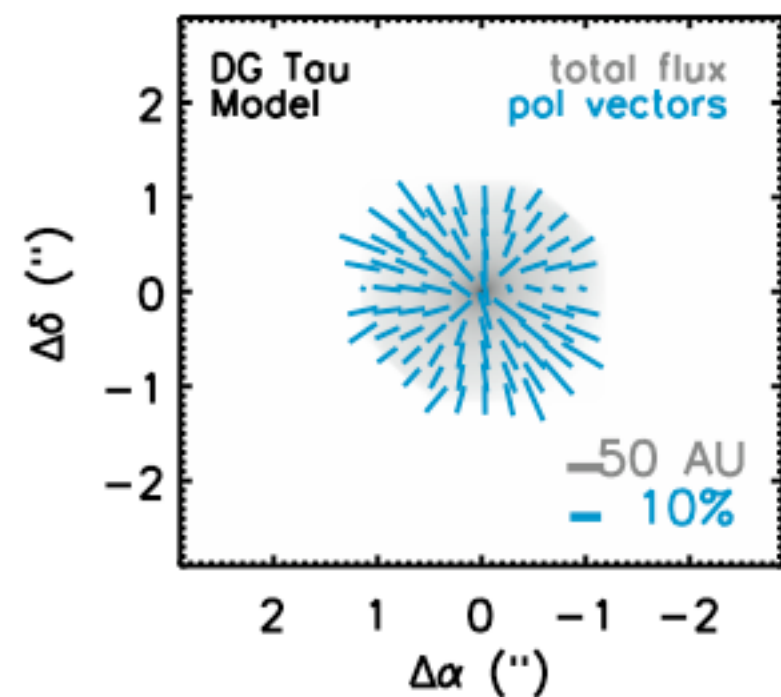
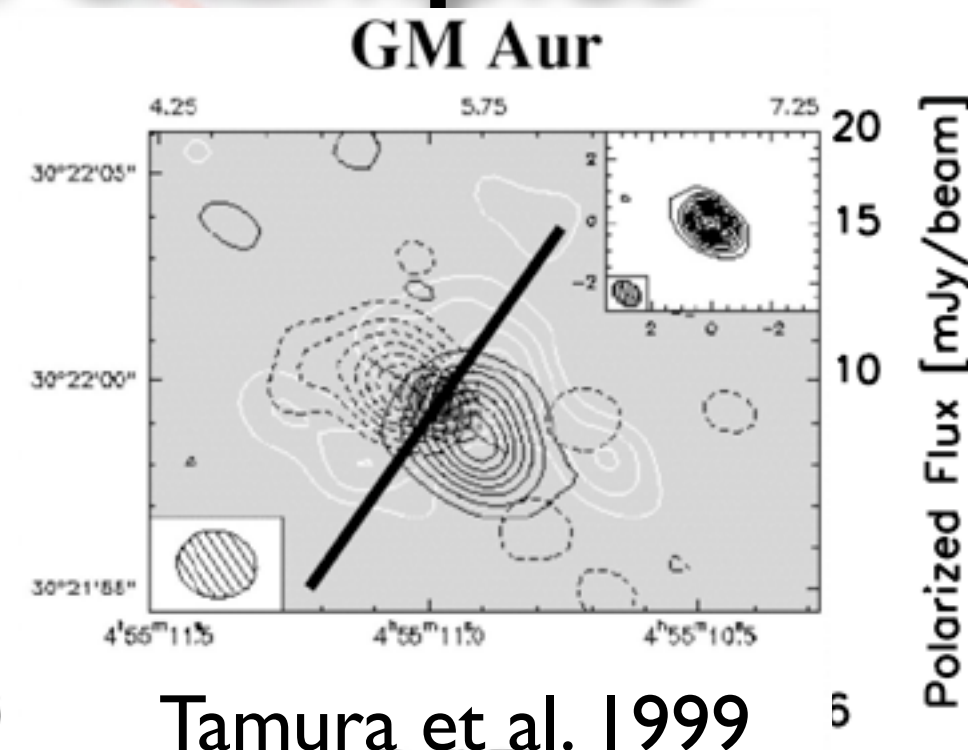
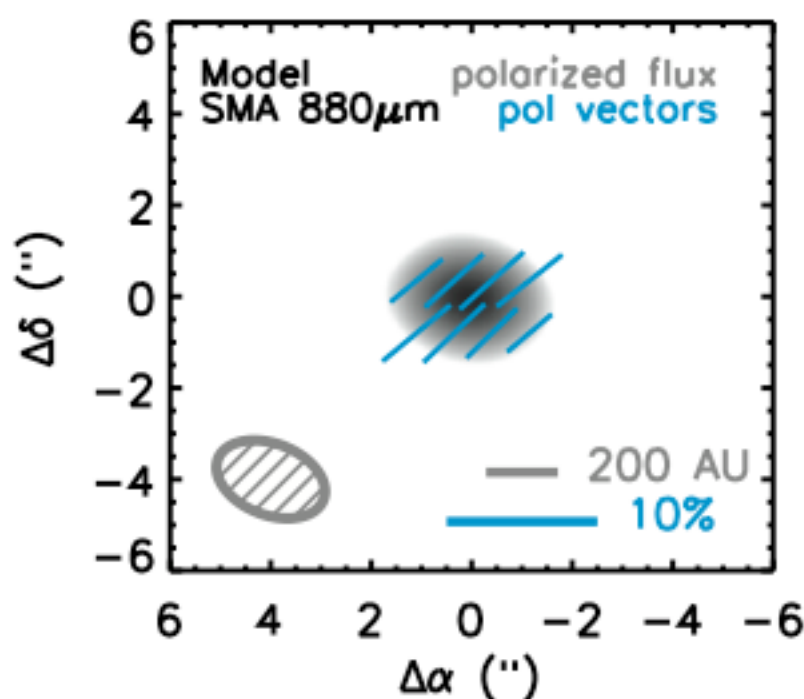
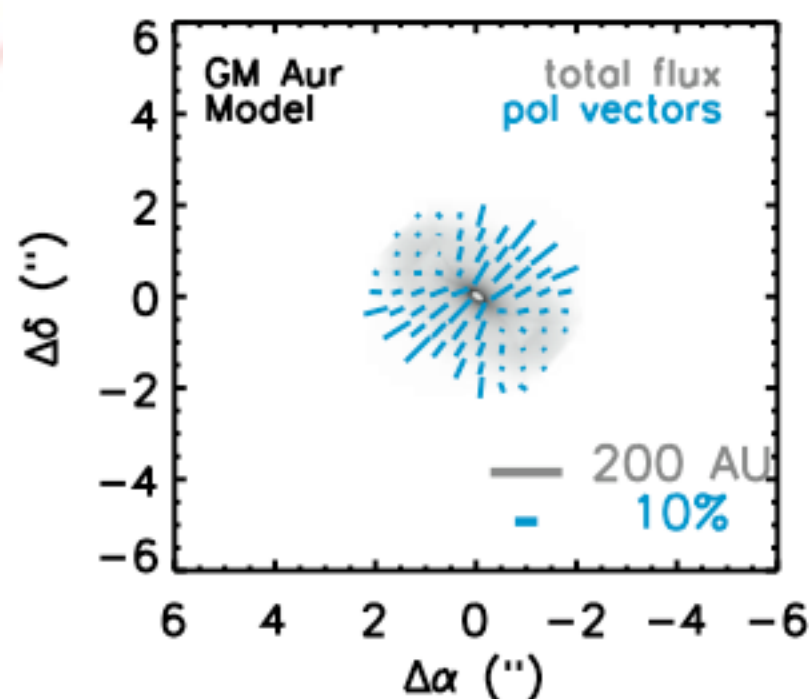
Surcis et al. 2013



Hull et al. 2013

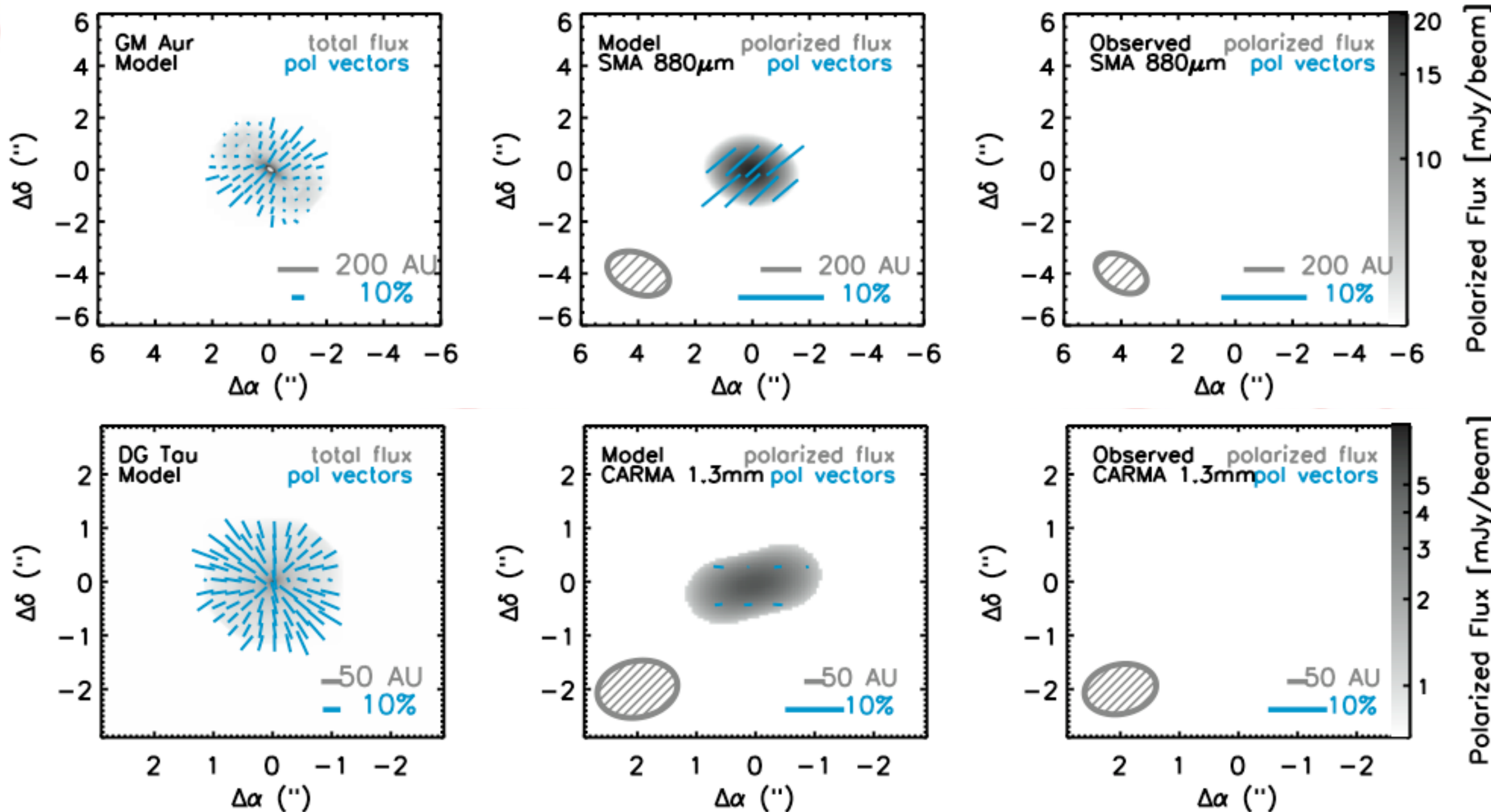
- Different answers
 - multiple sources / observing scales / statistics?

Star Formation examples



T Tauri accretion disks: Hughes et al. 2009, 2013

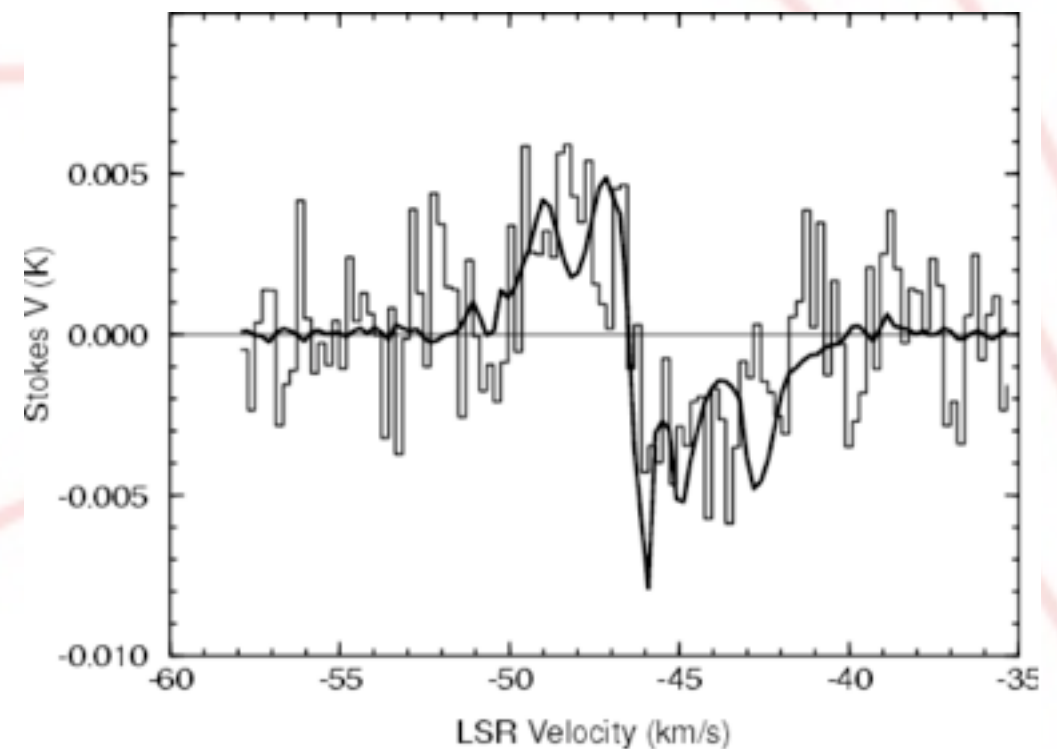
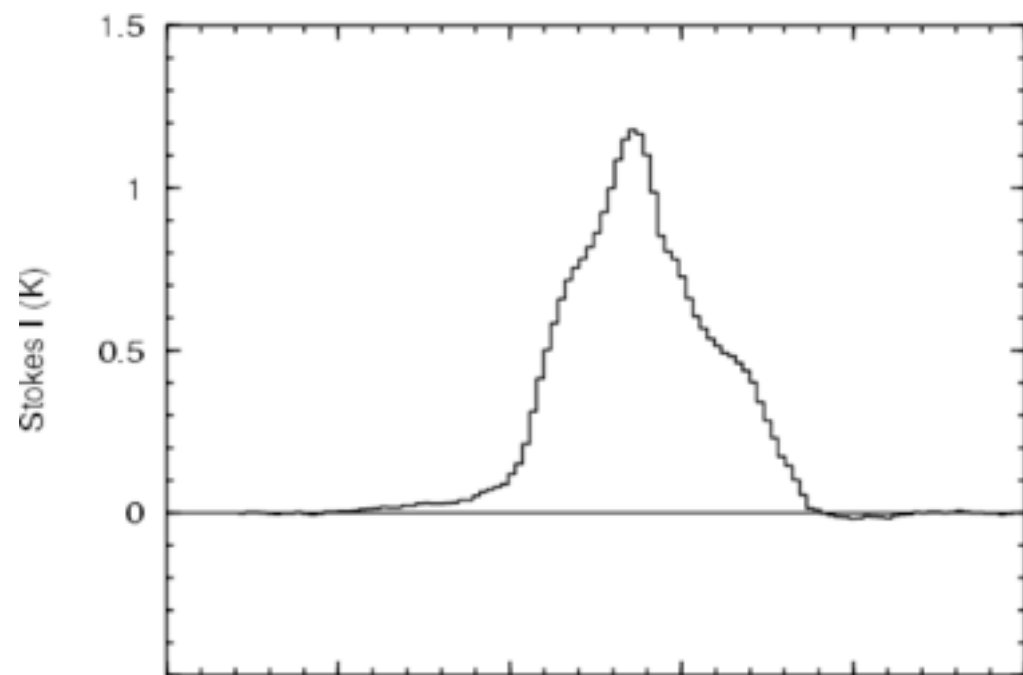
Star Formation examples



T Tauri accretion disks: Hughes et al. 2009, 2013

Star Formation examples

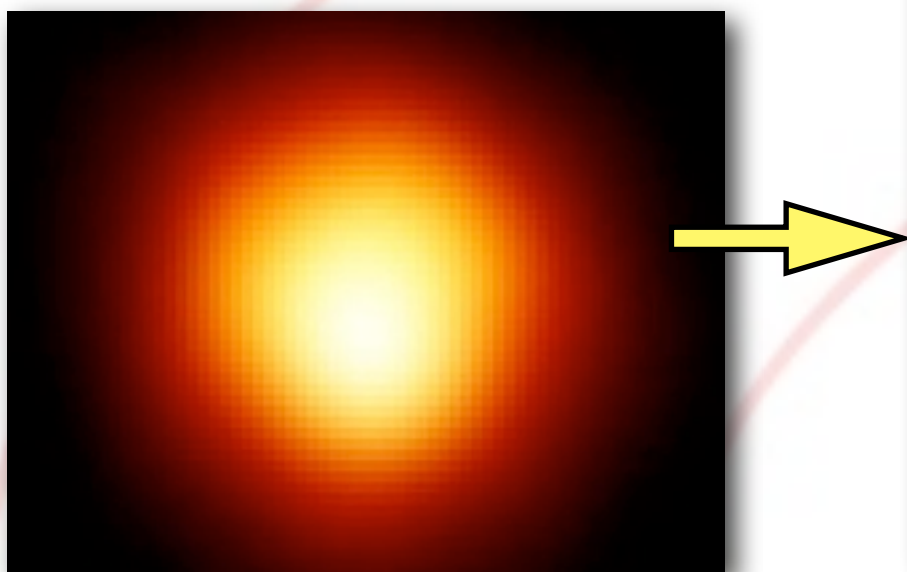
- Goldreich-Kylafis effect of CO
- Zeeman splitting of masers or e.g. CN/SO



CN, Falgarone et al. 2008

Evolved Stars

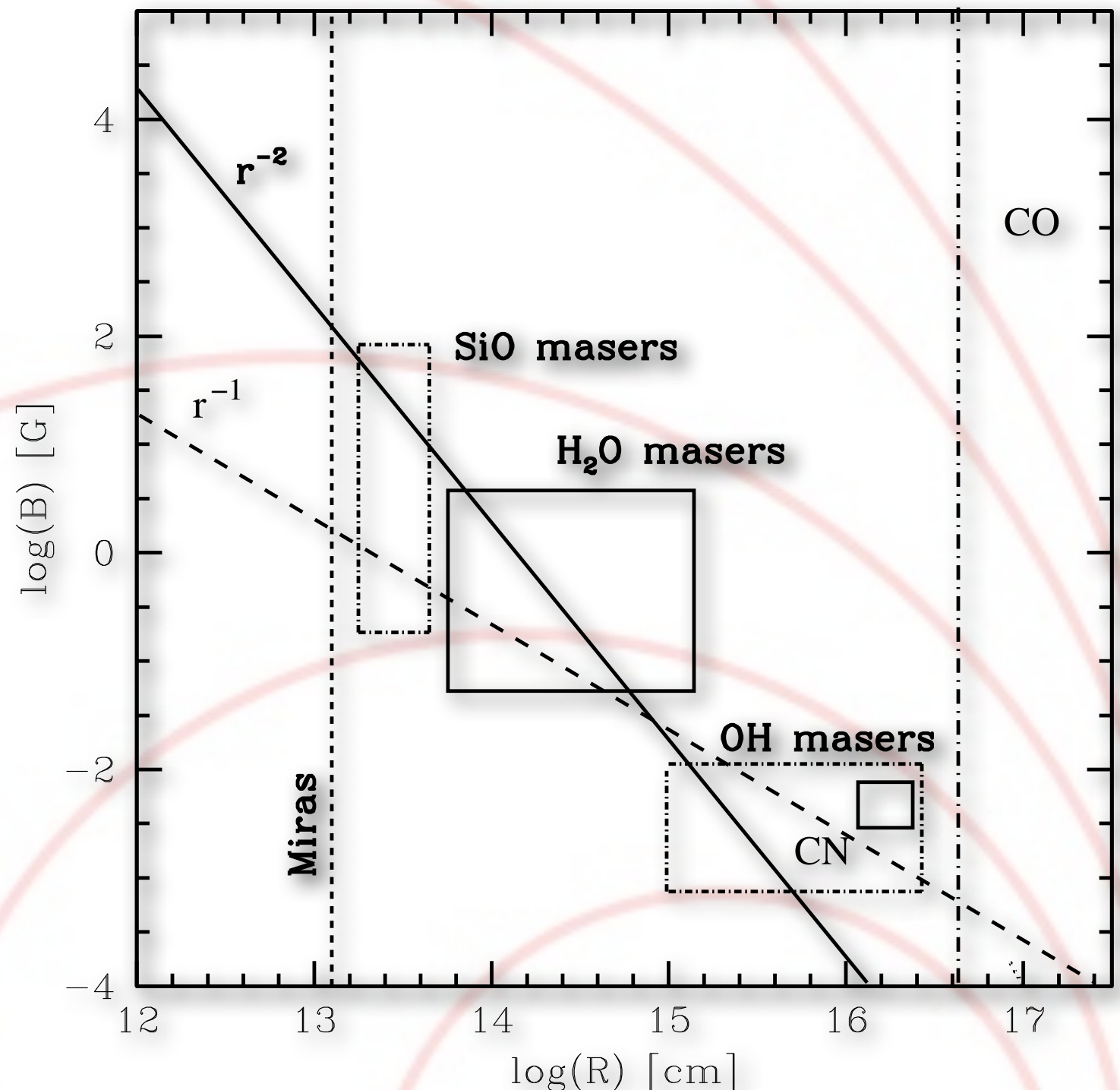
- Magnetic shaping of Planetary Nebulae?
 - origin of the magnetic field (binaries?)
- Magnetic component to AGB mass-loss?



Evolved Stars: AGB

Zeeman studies

- Oxygen rich:
 - SiO at $2 R_*$
 - $B \sim 3.5$ (up to 10s) G
 - H₂O at $\sim 5-80$ AU
 - $B \sim 0.1-2$ G
 - OH at $\sim 100-10,000$ AU
 - $B \sim 1-10$ mG
- Carbon rich:
 - CN at ~ 2500 AU
 - $B \sim 7-10$ mG



Vlemmings et al. 2002, 2005

Kemball et al. 1997, 2009

Herpin et al. 2006, 2009

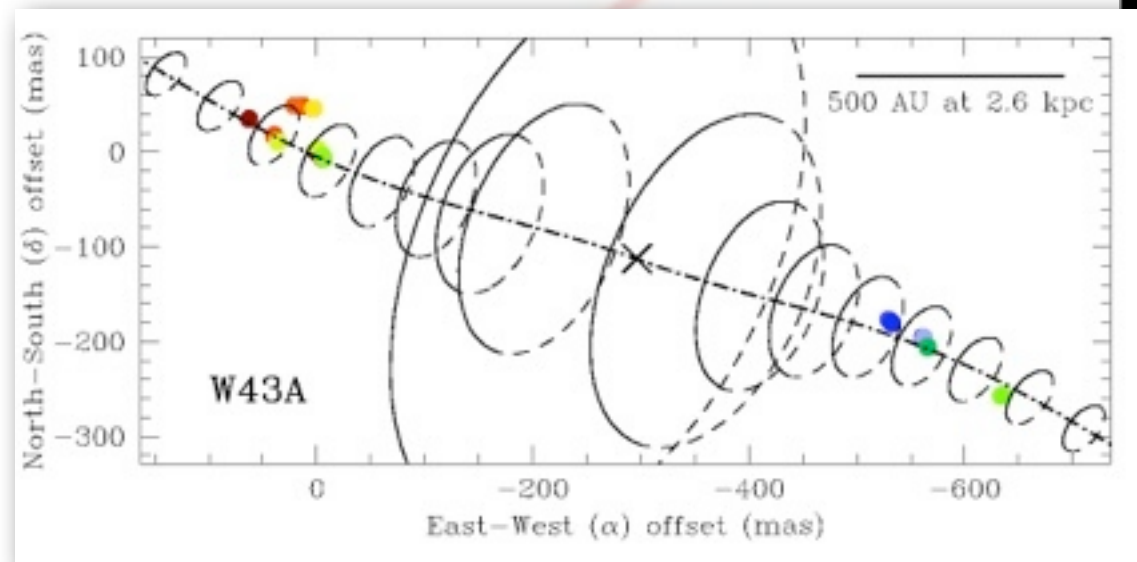
Etoka et al. 2004

Reid et al. 1976

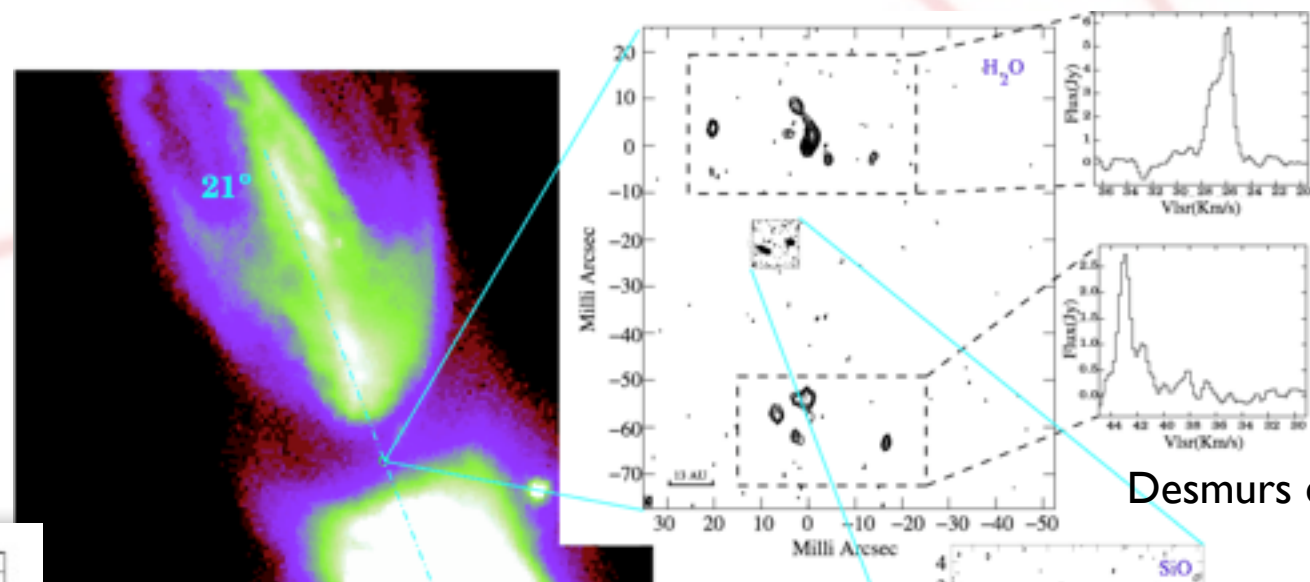
Amiri et al. 2012

Evolved Stars: post-AGB

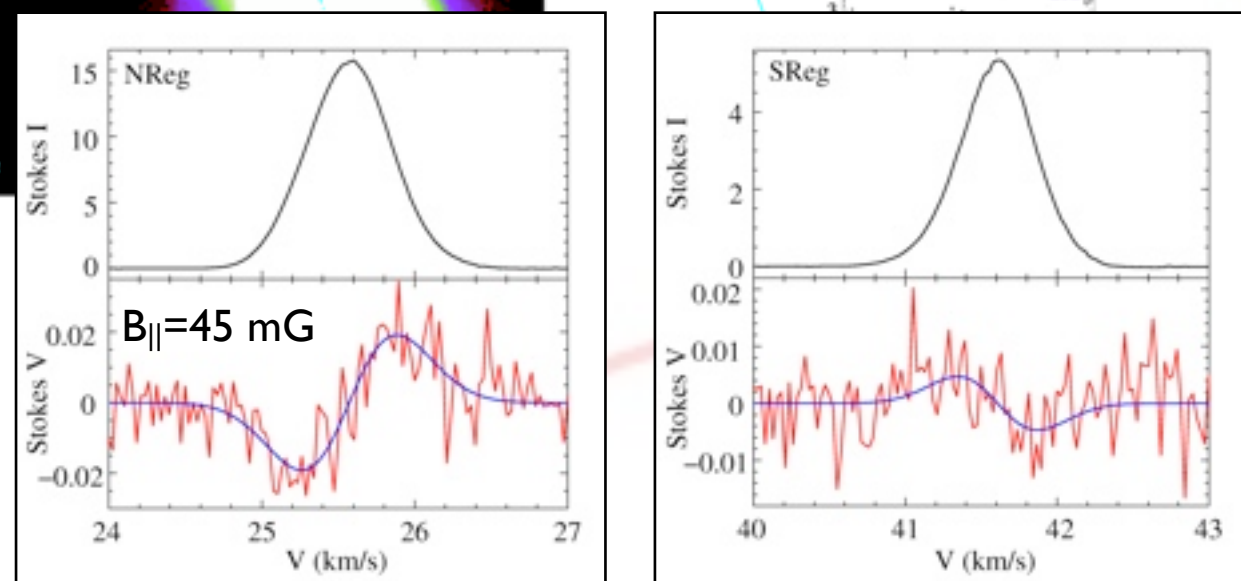
- W43A, post-AGB water-fountain
- Toroidal, collimating magnetic field:
 $B_\phi = 80 \text{ mG}$
- Enhanced in the H_2O masers
 - Around the jet $B = 100 \text{ } \mu\text{G}$ from OH masers
 - GBT confirmed strength in H_2O jet and shows expected reversal.
 - Extrapolated ($B_\phi \propto r^{-1}$) surface magnetic field of $B \sim 2 \text{ G}$.
- Rotten Egg Nebula
- H_2O masers magnetic field measurement
 - Extrapolated ($B_\phi \propto r^{-1}$) surface magnetic field of $B \sim 3 \text{ G}$



Vlemmings et al. (2006); Amiri et al. (2010)

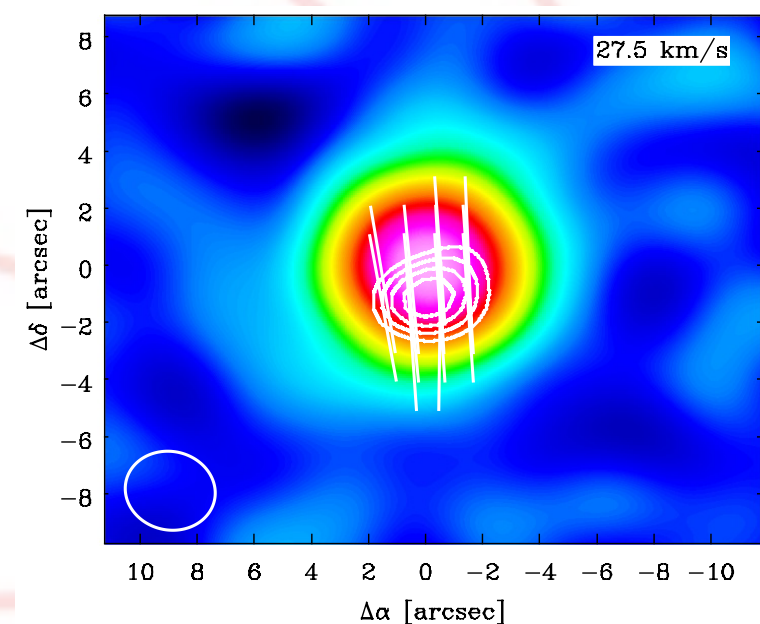
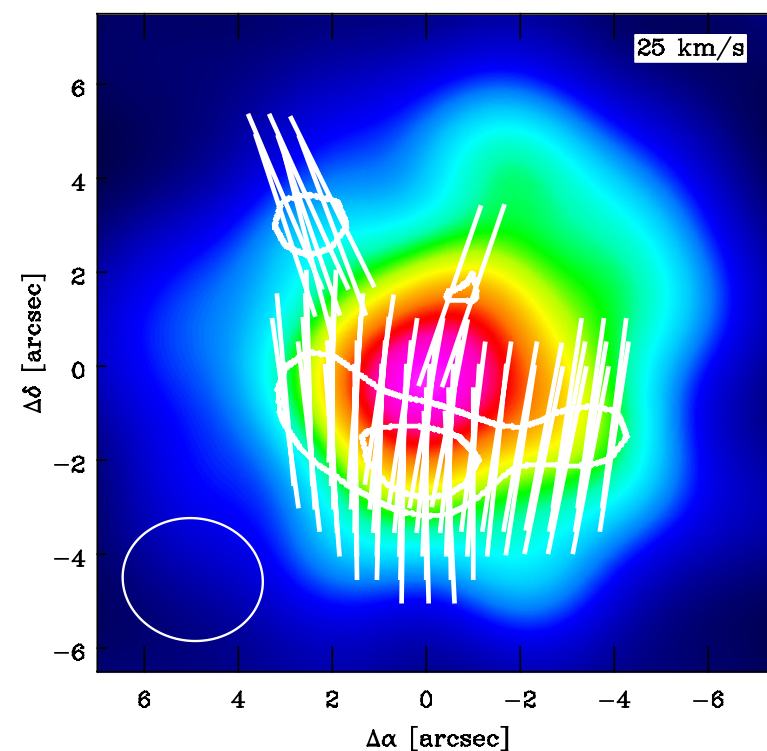
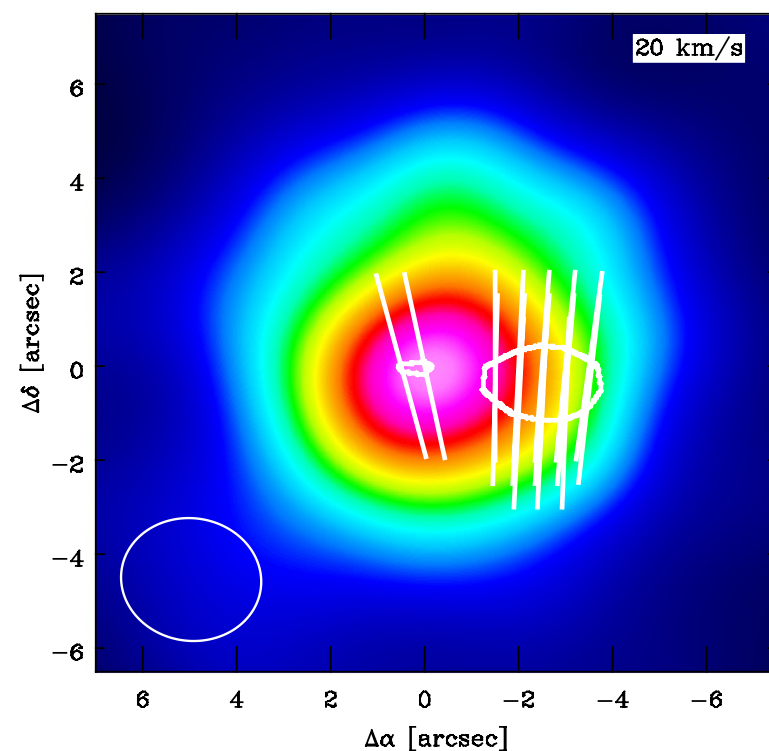


Desmurs et al. (2007)

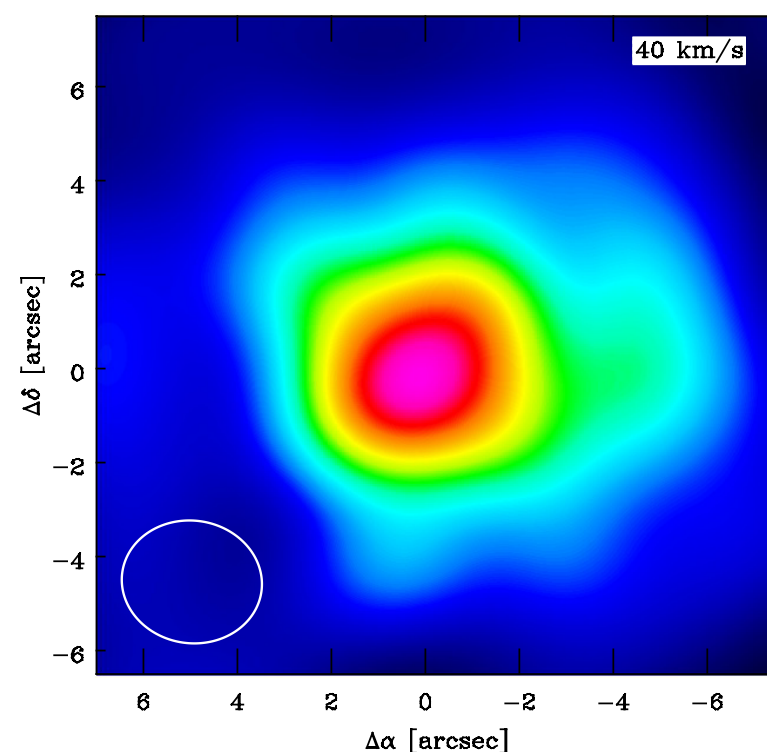
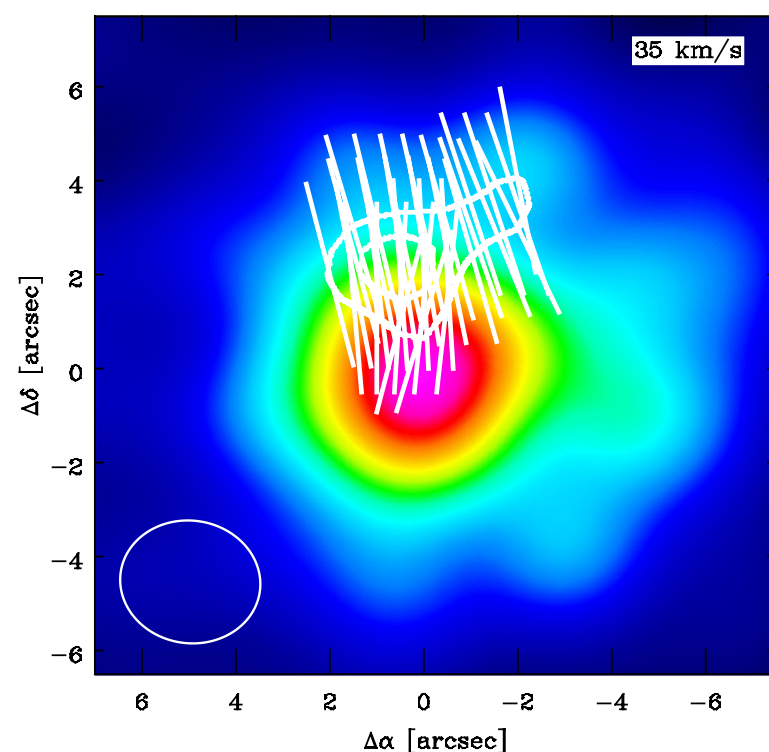


Leal Ferreira et al. (2012)

Evolved Stars examples



SiO(5-4) - up to 8%



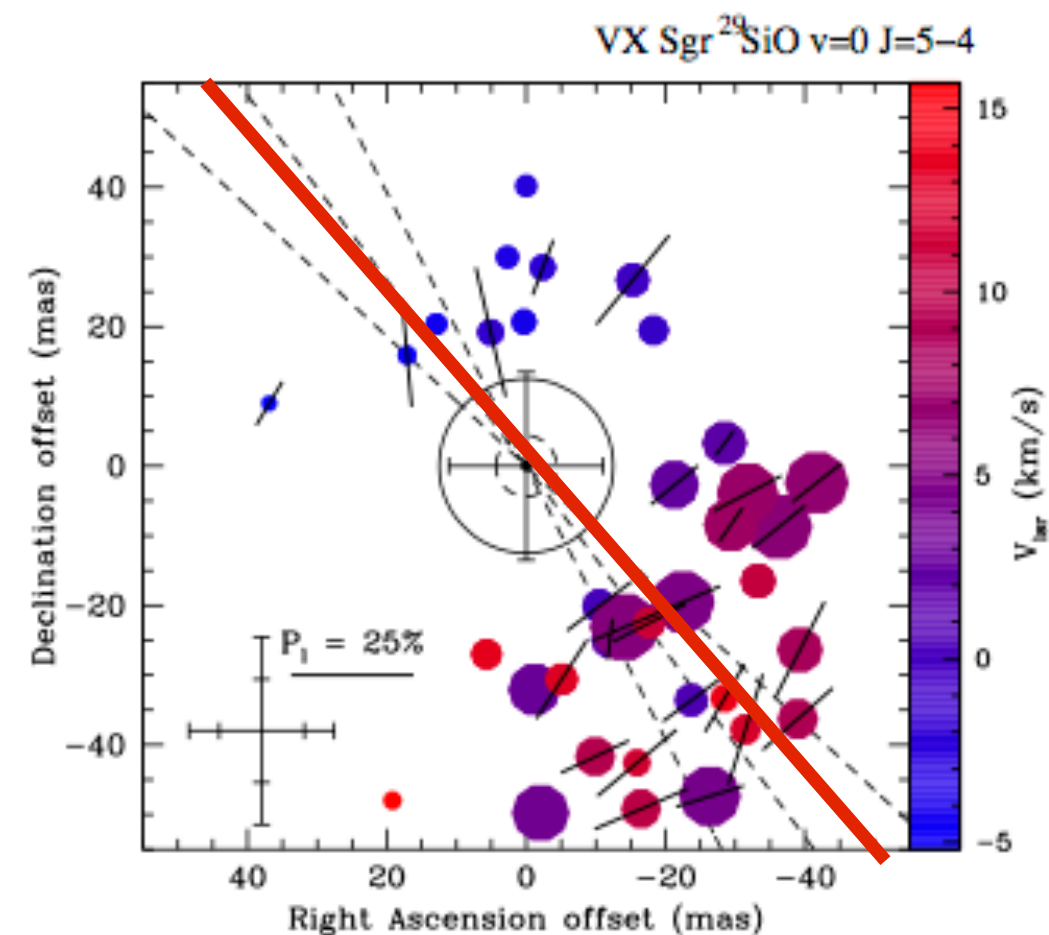
CO(2-1) - up to 13%

- non-radial
- indicative of large scale B-field

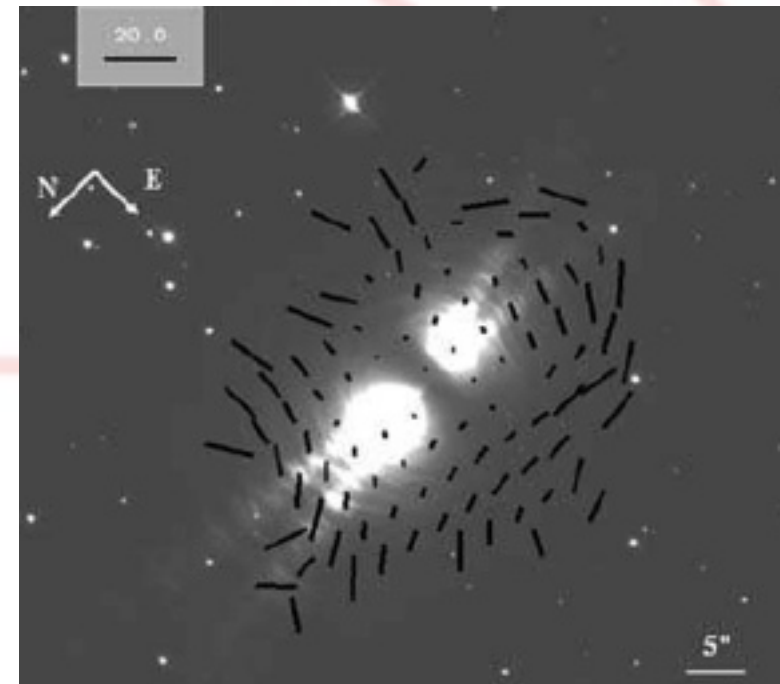
Vlemmings et al. 2012, A&A in press

Evolved Stars examples

Maser linear polarization of various lines (SiO, water, HCN)



215 GHz SiO (Vlemmings et al. 2011)

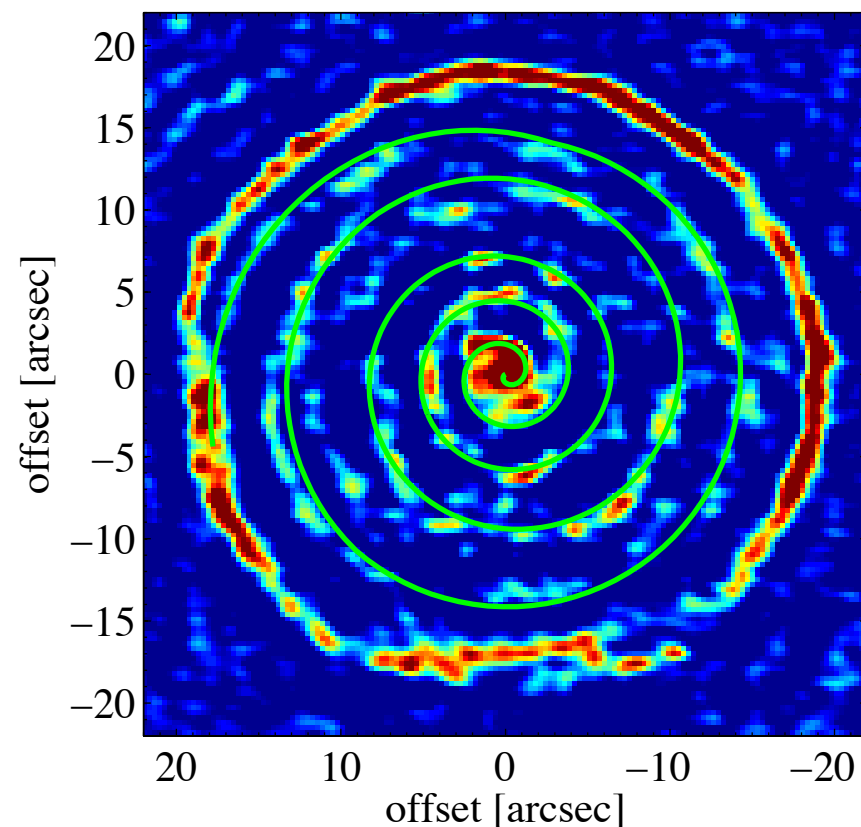


Sabin et al. 2002;
B-vectors for CRL 2688 (Egg Nebula)

Dust polarization of PNe

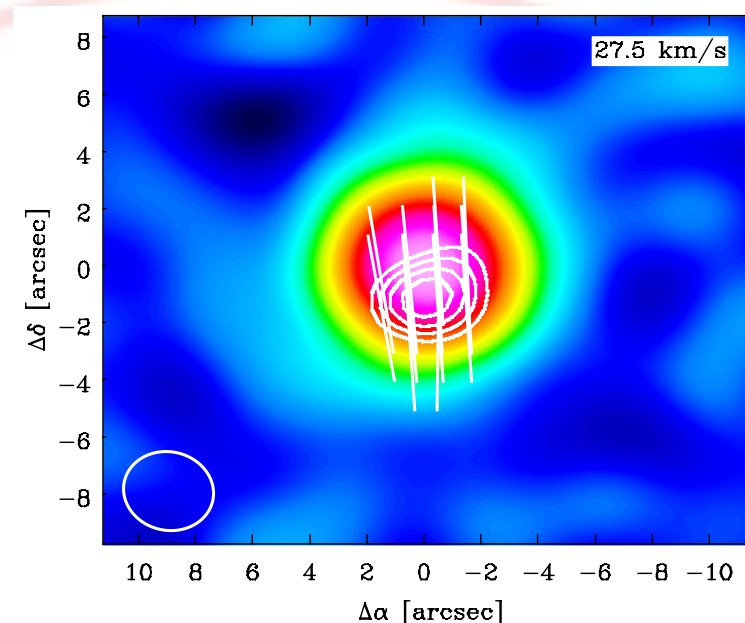
Evolved Stars examples

- Dust grain composition (of the large dust grain component) of P-PNe
- Compare CO morphology with magnetic field (GK-effect)

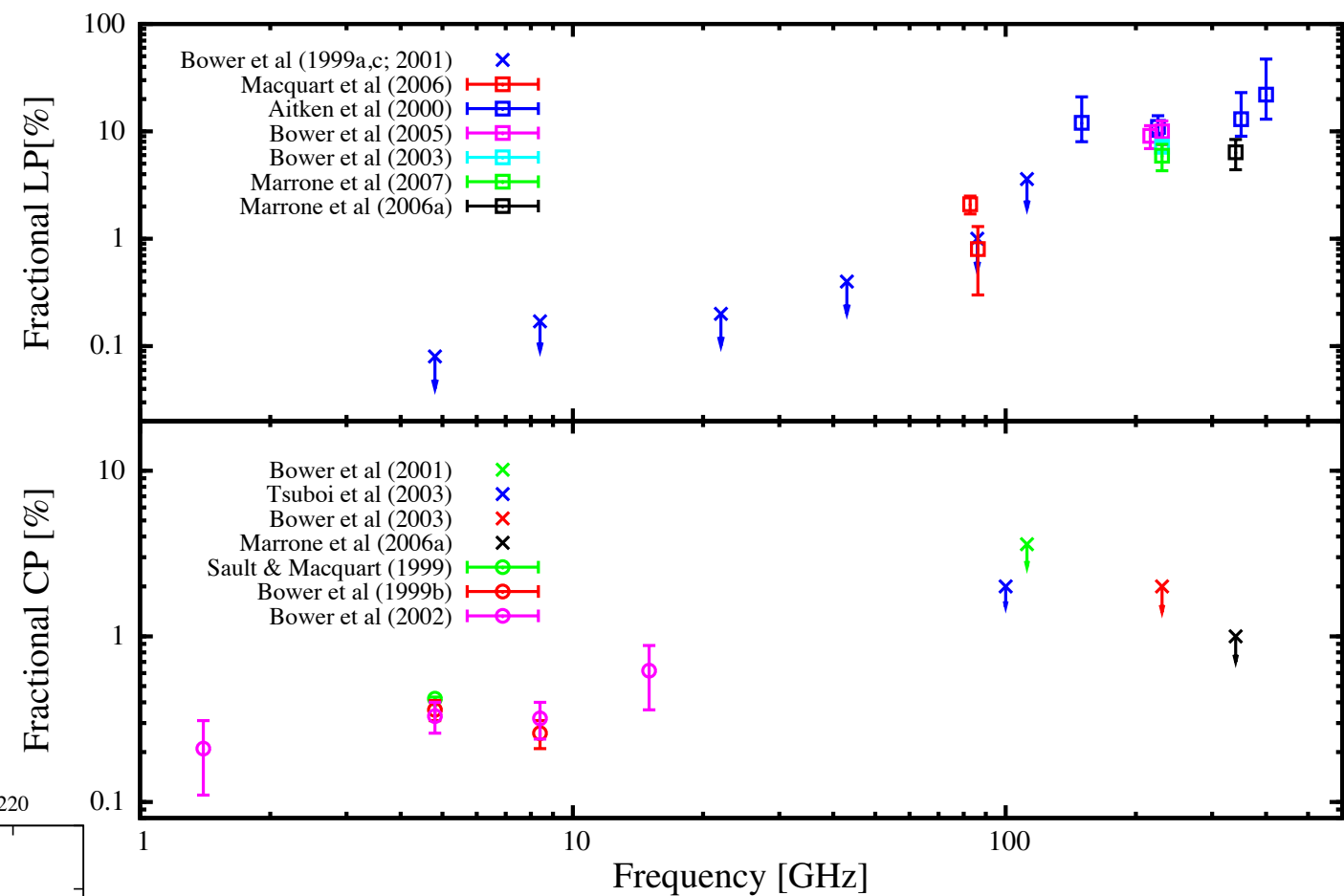
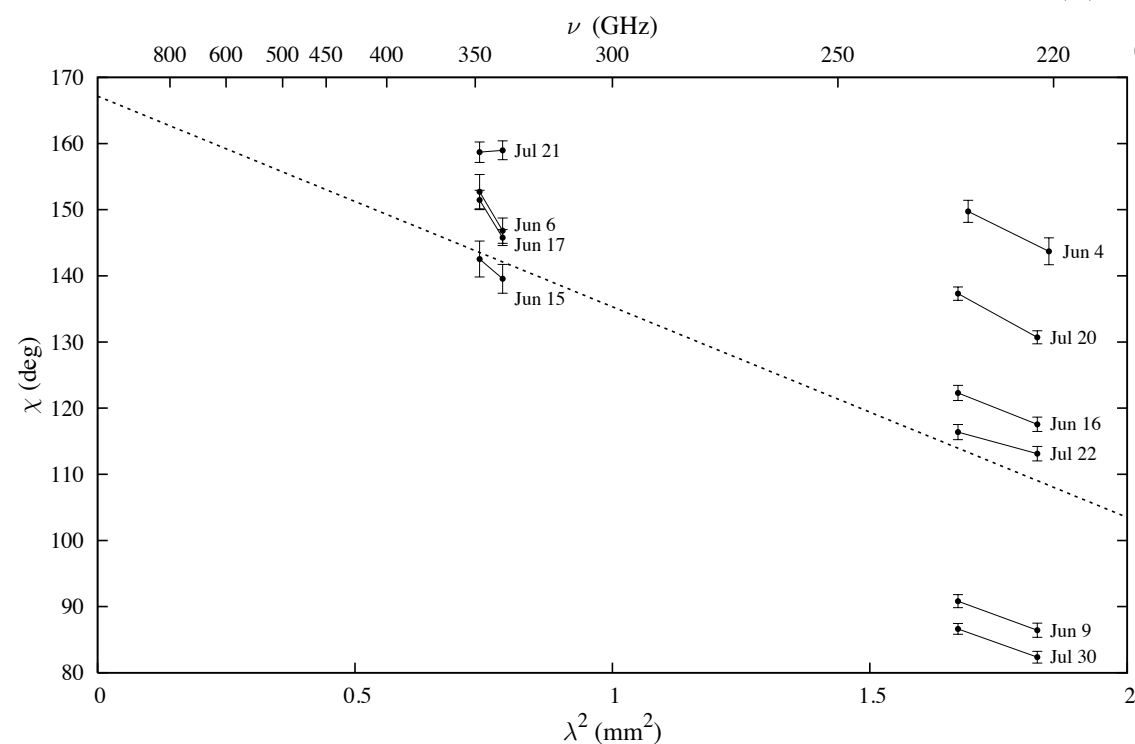


R Scl (Maercker et al. 2012)

SMA full track results can be done with ALMA in a matter of minutes



Galactic Centre

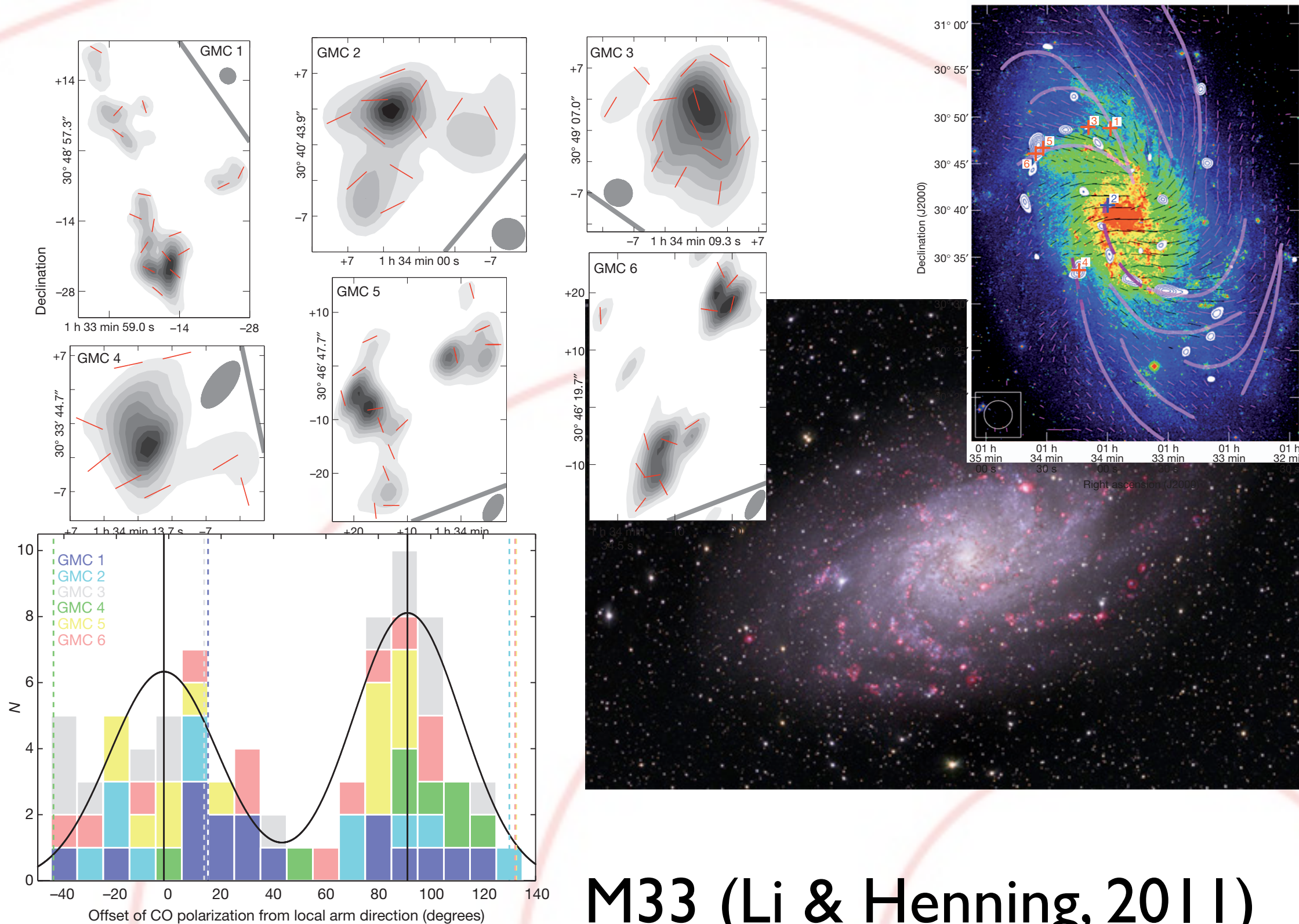


Faraday rotation:
Marrone et al. 2009

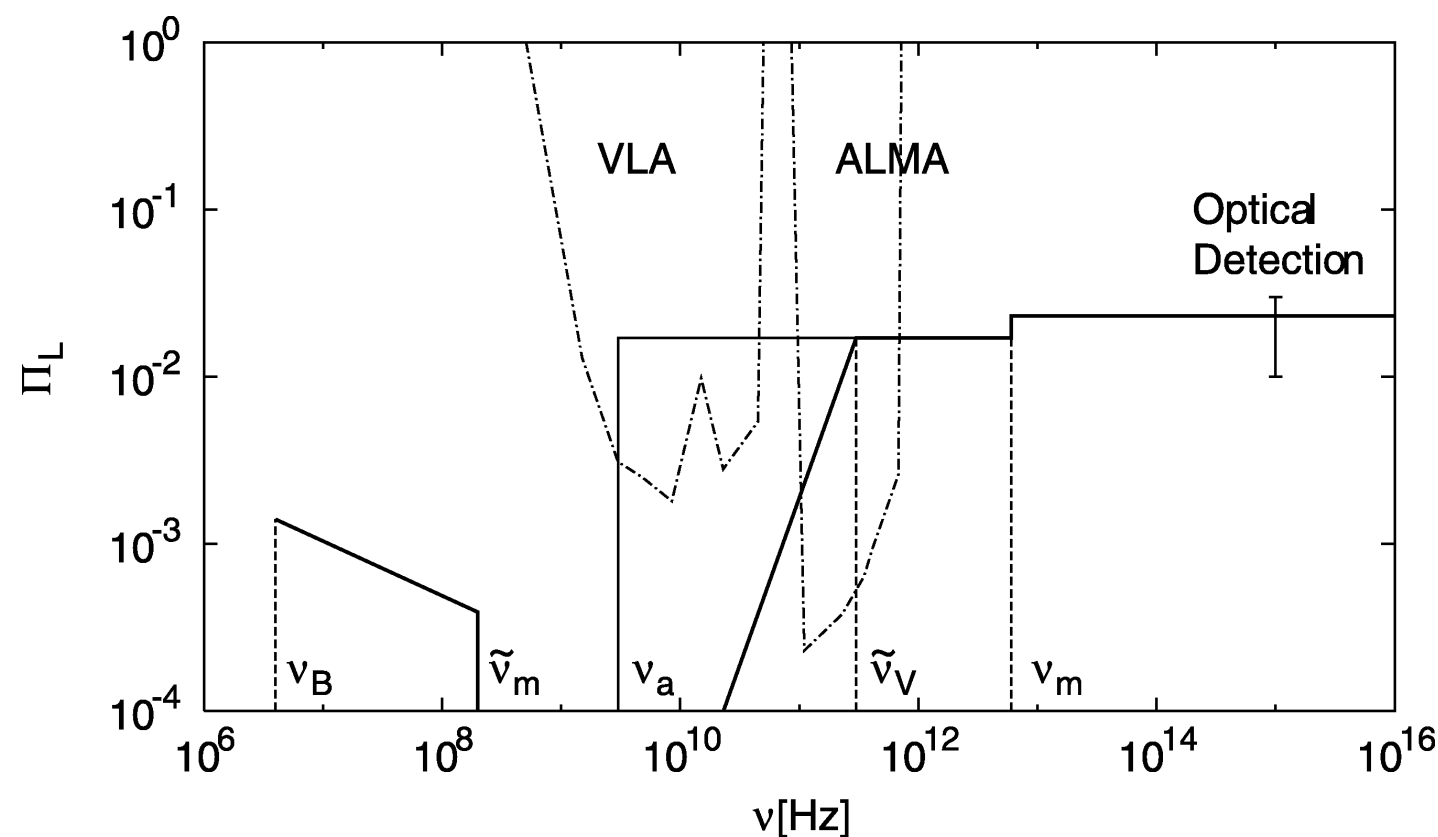


(Very few) Science Examples:
Extra-Galactic Science

Galaxies - Molecular Clouds



M33 (Li & Henning, 2011)



Faraday rotation effect with ALMA

(Toma et al. 2009)

If ν_a is determined by the observation of a bright burst and the linear polarization is not detected at $\nu \gtrsim \nu_a$ with VLA and detected at $\nu \gg \nu_a$ with ALMA, it becomes clear that a number of the thermal electrons exist and the magnetic field is ordered on large scales. If we determine $\tilde{\nu}_V$, the electron-proton coupling parameter f can be constrained by equation (7).

AGN (jets)

- See Massardi/Laing talks



Some modeling options



ARTIST

Adaptive Radiative Transfer Innovations for Submillimeter Telescopes

on behalf of the ARTIST team:

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Padovani³, Rolf Kuiper^{5,6}, Reinhold Schaaf⁵, Pau Frau³

Centre for Star and Planet Formation and Niels Bohr Institutet, Copenhagen

Sterrewacht Leiden, Leiden

Institut de Ciències de l'Espai, Barcelona

Onsala Space Observatory, Onsala

Argelander Institute for Astronomy, Bonn

MPIA, Heidelberg

The ARTIST components

- 1) An innovative radiative transfer code using adaptive gridding that allows simulations of sources with arbitrary (3D) structures, ensuring rapid convergence - even for molecules with a complex level structure, e.g., H₂O
- 2) Tools for modeling the polarization of line and dust emission, information that will come with standard ALMA observations
- 3) A Python-based comprehensive interface with Graphical User Interface connecting these packages and providing links to external codes
- 4) A library of pre-coded common models (e.g., Shu collapse model) for the user to browse.

Theoretical input models

E.g., analytical collapse, magnetic field, chemical network



Dust radiative transfer

Self-consistent (dust) temperature distribution



Line excitation

Chemistry: abundances
Dynamics: velocity field

Continuum polarization

Grain alignment efficiency dependent on
density/temperature



Line polarization

magnetic field model
Zeeman splitting



Raytracer

Images in molecular lines, continuum and polarization



Integration of images into data analysis software, e.g. CASA

Constraints on density, temperature, velocity field, magnetic field, chemistry

Theoretical input models

E.g., analytical collapse, magnetic field, chemical network

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User interface

User interface

Theoretical input models

E.g., analytical collapse, magnetic field, chemical network

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ARTIST

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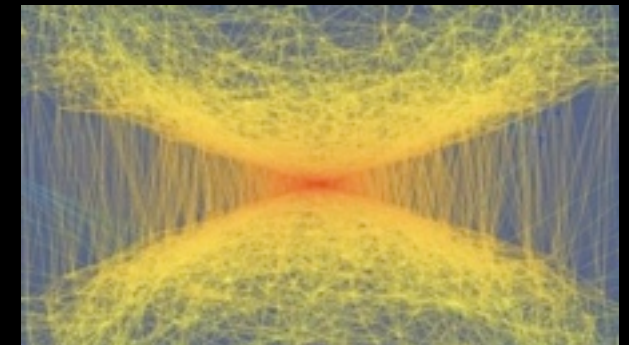
User interface

User interface

Components: Line excitation / Raytracing

LIME

Brinch & Hogerheijde, 2010



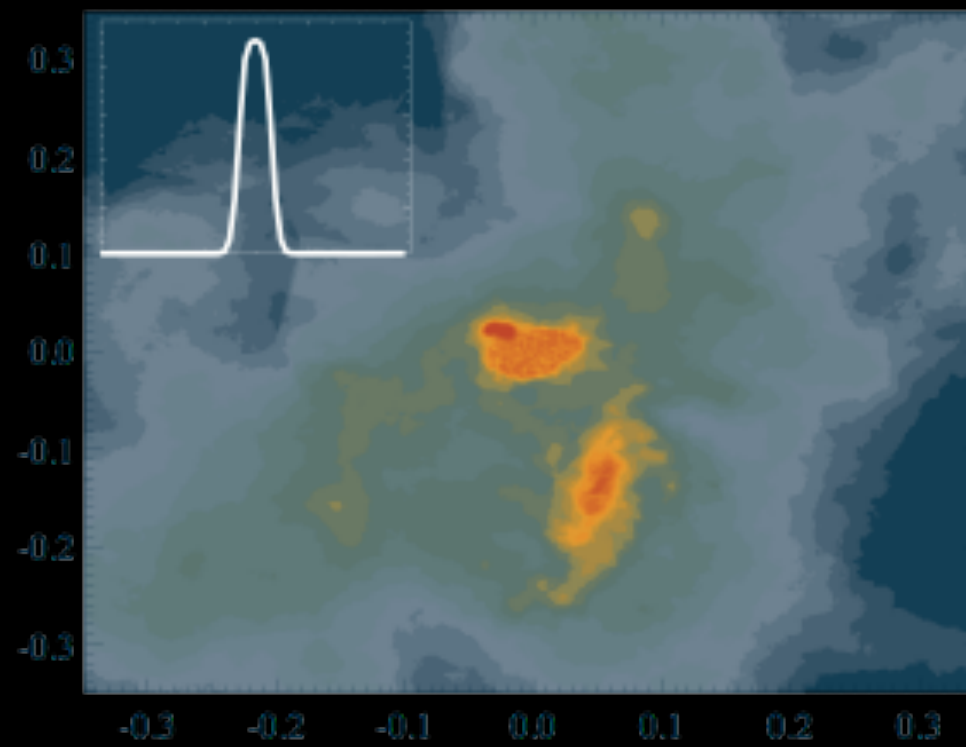
LIME is a new and innovative non-LTE spectral line radiation transfer code for 3D models in arbitrary geometries.

Instead of a 2D regular mesh (e.g. nested AMR) Lime transports photons along the edges of a 3D unstructured Delaunay-grid (Ritzerveld & Icke 2006)

Grid points are placed semi-randomly but grid point distribution is well controlled
=> grid is very flexible

Visualization with VTK

Image data are written in FITS format that can be used in directly in CASA (simdata).



Components: Continuum polarization

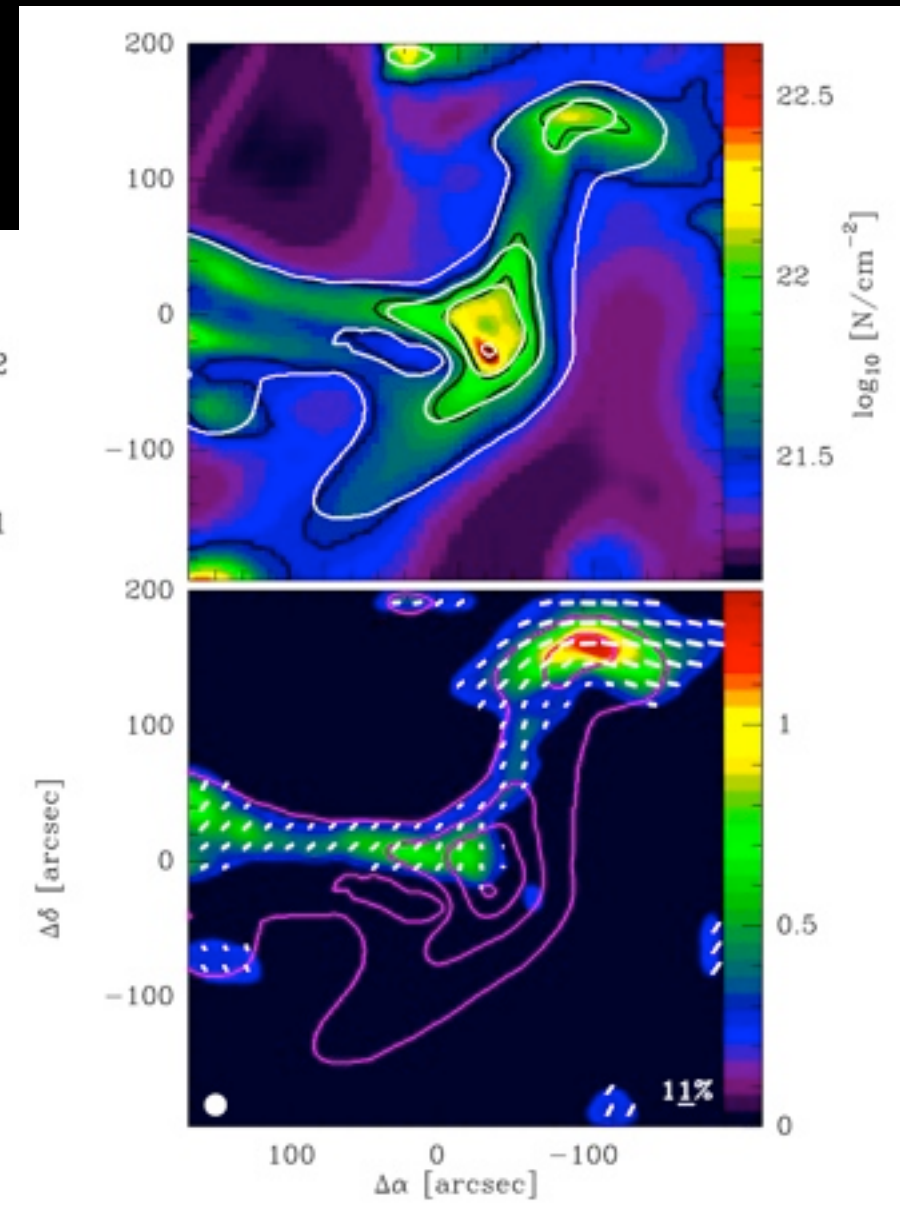
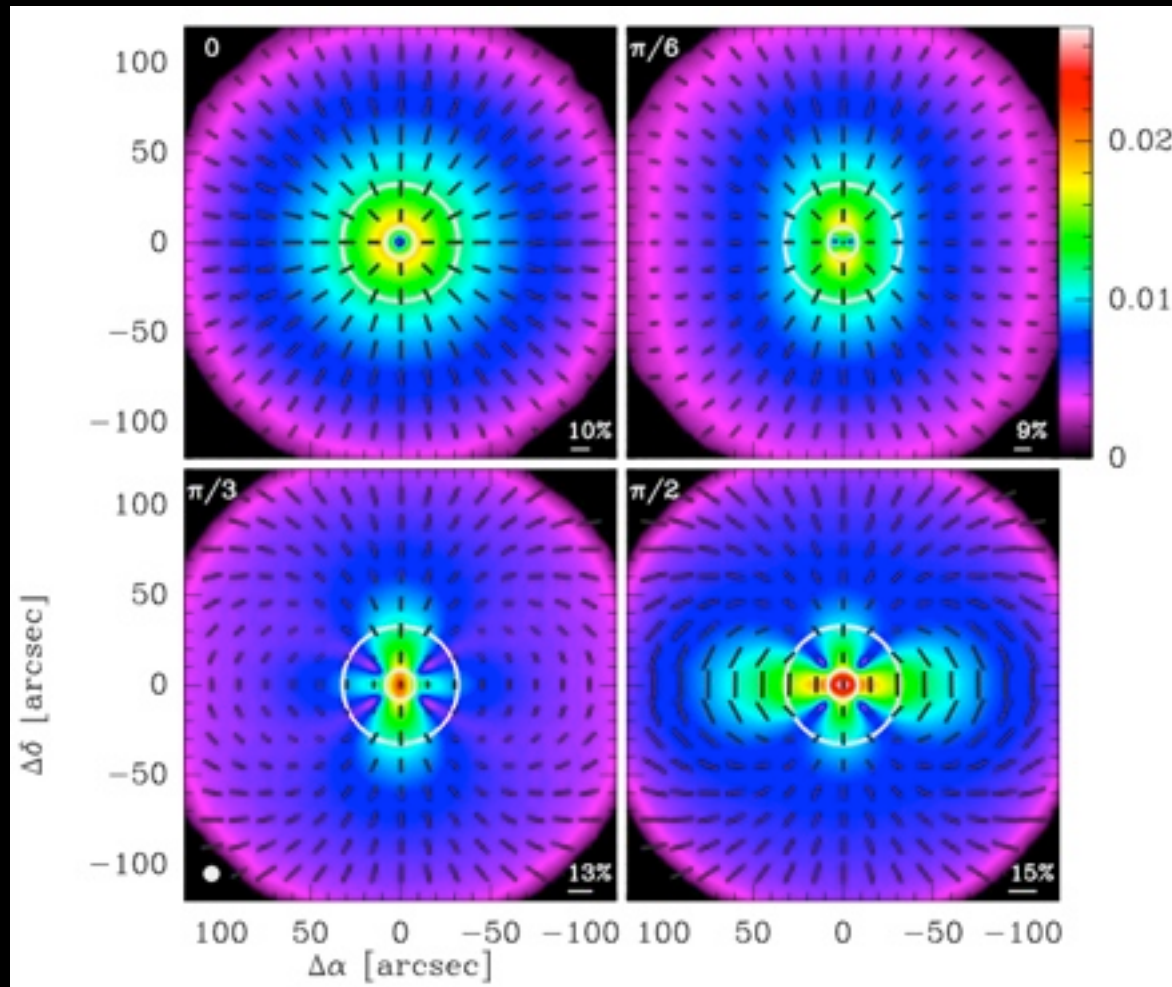
Dustpol (Padovani et al. 2012, in press.)

Calculates Stokes parameters on the basis of Lee & Draine 1985, Padoan 2011

Grain alignment efficiency (function of density/temperature)

3D magnetic field structure

=> Synthetic stokes vectors



Components: Line polarization

Line polarization (Kuiper et al. in prep) is in the testing/benchmarking phase

Full stokes radiative transfer using a modified version of LIME

Goldreich-Kylafis effect (Unequal population of magnetic-substates in an anisotropic velocity/radiation field)

Conclusions

- ALMA will provide breakthrough polarization science
 - while likely throwing up some new puzzles
- Several applications will require:
 - Extended polarization mapping with ACA and TP
 - Stable polarization across primary beam
 - Stable polarization characteristics with time
 - at least $\sim 0.1\%$ accuracy after calibration (preferably better)